# AIRCRAFT ENGINE DESIGN 

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# AIRCRAFT ENGINE DESIGN 

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## PREFACE

This text has been assembled to aid technical students in bridging the gap between the point ( $a$ ) where they have a fairly complete knowledge of the fundamentals of mathematics, mechanics, and machine design and (b) the point where they are sufficiently familiar with the application of these fundamentals to the design of aircraft engines to enable them to be of value to the aircraftengine building industry.

Usually students entering this field of study are totally lacking in the experience so essential to deciding a logical order of procedure of engine design. They also lack the accumulated information upon which experienced designers can call for making the innumerable assumptions that must precede or parallel the analyses of various parts. Hence, an outline of procedure and a considerable accumulation of more or less rational data have been included. However, it is pointed out that although the Suggested Design Procedure is one way of carrying through the analysis, it is not the only way, or even the best possible way in a particular instance. Students are usually encouraged to select a "conventional" type of engine for a first design because there are more "signposts" to guide them, but this should not be misinterpreted as implying a negative attitude toward new ideas and possible improvements over present practice. Rather, it is based on the belief, founded largely on teaching experience, that a student cannot very well design an improved or unconventional engine until he is familiar with the shortcomings and weaknesses of conventional engines.
The author is greatly indebted to the various stated sources for illustrative data, and in each case he has endeavored to give proper credit. The author is also indebted to G. D. Angle, P. M. Heldt, various staff technicians at Wright Field, the NACA, the engine industry, and his associates at l'urdue, particularly Dean A. A. Potter, Prof. G. A. Young, and especially Prof. K. D. Wood for valuable suggestions, criticisms, and assistance.

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Joseph Liston. April, 1942.

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# AIRCRAFT ENGINE DESIGN 

CHAPTER 1<br>REQUIREMENTS, POSSIBILITIES, AND LIMITATIONS

1-1. Sources of Power.-The source of power for all presentday aircraft is the internal-combustion engine. So far, this type of prime mover is the only one that has proved capable of meeting all the exacting requirements of powered flight successfully. Other prime movers such as steam plants have been considered and even tried experimentally in a few instances, but none has, to the writer's knowledge, survived to the production stage.

1-2. Basic Requirements and Limitations.-Some of the more important basic requirements of the airplane engine are

1. Adequate power.
2. Very low weight-power ratio.
3. High specific power output.
4. High thermal efficiency.
5. Compactness.
6. Reliability and long life.
7. Relative ease of maintenance.
8. Reasonable initial cost.
9. Ability to operate under adverse conditions.

Considering these items briefly:

1. Historians now generally agree that the first successes in powered flight were delayed several years because of lack of a suitable engine. Present large aircraft designers are continually clamoring for more and more powerful engines. Reductions in parasite drag have contributed markedly to the improvements in performance attained during the last 10 years, but further improvement from this source appears to be following the law of diminishing returns.

The power necessary for any given proposed airplane is usually determined from an estimate of parasite drag, combined with wing drag and propeller characteristics. This enables the designer to estimate the brake horsepower necessary for the maximum speed at which he desires to fly.

From the fundamental relations of drag, velocity, horsepower, and propeller efficiency, the maximum brake horsepower required for any given airplane may be expressed by

$$
P=\frac{D \times V_{\mathrm{m}}}{375 \eta} \quad C_{D} \frac{\rho}{\cap} S \quad V_{\max }^{3}
$$

where $P=$ brake horsepower needed at $V_{m a x}$.
$D=$ drag, lb.
$C_{D}=$ coefficient of drag (for the entire airplane).
$\rho=$ mass density.
$S=$ a representative area (usually the wing area) corresponding to $C_{D}$.
$V_{\max }=$ maximum speed of the airplane, m.p.h.
$\eta=$ propeller efficiency.
Letting $S=f$, the total equivalent flat-plate area of the airplane ( $=f_{\text {parasite }}+f_{\text {wing profile }}$ ) of $C_{D}=$ unity, assuming standard density, and collecting constants,

$$
\begin{equation*}
P=\frac{f}{\eta}\left(\frac{V_{\max }}{52.8}\right)^{3} \tag{1-1}
\end{equation*}
$$

At maximum speed, the wings will be at or very near an angle of attack at which the wing drag is a minimum. If the corresponding wing-drag coefficient is increased to unity, the drag equation will still hold if $S$ is decreased by the inverse ratio. The new value of area is called flat-plate area of minimum wingprofile drag and may be designated $f_{w p}$. In symbols,

$$
D_{\min }=C_{D \min } \frac{\rho}{2} S V^{2}=C_{D}(=1) \frac{\rho}{2} f_{w p} V^{2}
$$

or

$$
\frac{C_{D \min }}{C_{D}(=1)}=\frac{f_{w n}}{S}
$$

from which

$$
f_{w_{p}}=C_{D_{\min }} \times S
$$

Since the minimum drag coefficient of most airfoils is very near $0.01, f_{w p}=0.01 S$, approximately. Then for estimating power requirements,*

$$
\begin{equation*}
P=\frac{f_{p}+0.01 S}{\eta}\left(\frac{V_{\max }}{52.8}\right)^{3} \tag{1-2}
\end{equation*}
$$

where $P=$ brake horsepower needed at $V_{\text {max }}$.

$$
\begin{aligned}
f_{p} & =\text { square feet of parasite flat-plate area of } C_{D}=1.0 . \\
S & =\text { wing area, sq. } \mathrm{ft} . \\
\eta & =\text { propeller efficiency. } \\
V_{\max } & =\text { maximum speed of the airplane, m.p.h. }
\end{aligned}
$$

Example.-A company plans to develop an engine for military studenttraining planes of the following general characteristics: Well streamlined biplanes with retractable landing gear and cowled engines, 2,500 to $3,500 \mathrm{lb}$. gross weight, wing loadings around 12 to 16 lb . per sq. ft., and top speeds of 130 to $140 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. Approximately what rated engine horsepower should the company design for?

Solution.-Assuming mean values, $S=3,000 / 14=214$ sq.ft., $f_{p}=$ about 6 sq . ft. (Fig. 1-1), and $\eta$ will probably be about 80 per cent. Therefore

$$
\frac{6+0.01 \times 214}{0.8}\left(\frac{140}{52.8}\right)^{3}=189 \mathrm{~b} . \mathrm{hp} .
$$

Correlation of brake horsepower, wing area, and maximum speed for existing planes can be used as a basis of estimating brake horsepower necessary. This has been done for 68 American airplanes (Fig. 1-2). These planes included all types from light sport planes to large flying boats, and as is indicated in the figure, fair correlation exists. The slope of the mean line (Fig. 1-2) is 2.56, and from its equation

$$
\begin{equation*}
P=S\left(\frac{V_{\max }}{155}\right)^{2.56} \tag{1-3}
\end{equation*}
$$

where the symbols are the same as in Eq. (1-2). Equation (1-3) is useful in approximating the maximum brake horsepower, but Eq. (1-2) is more accurate and should be used when $f_{p}$ and $\eta$ are known or can be determined.
2. The weight-power ratio is an important criterion to the value of an engine for airplane use. Figure 1-3 shows the weight-

[^0]power ratios for 36 representative American engines. The position of any given engine with respect to the mean line may be taken as a measure of the degree of excellence of the design. However, excessively low weight-power ratios are usually


Frg. 1-1.-Flat-plate equivalent of parasite drag of airplanes.
Class 1. Cantilever monoplane with retractable chassis, streamline fuselage, well-cowled engine, and no external bracing.

Class 2. (a) Cantilever or wire-braced monoplane with cantilever or wirebraced chassis, wheel pants, streamlined fuselage, engine eowl or ring. (b) Biplane or externally braced monoplane with retractable chassis, streamline fuselage, engine cowl or ring.

Class 3. Biplane or externally braced monophane with streambinc fuselage, engine cowl or ring.

Class 4. Airplanes having excessive parasite drag. (From (ivil Arronautics Manual 04.)
attained either with the aid of very high octane fuels or at a sacrifice in operating life. For example, racing engines have very low weight-power ratios, but they require special fuels and usually have a very short life between overhauls.

Nevertheless, it is essential that the weight be low, as additional plane weight simply means less useful load. Figure 1-4 shows
the weight of engines in terms of gross weight of the plane for 22 American aircraft in the gross weight range between 1,000


Fig. 1-2.-Variation of maximum speed with brake horsepower per square foot of wing area for 68 American airplanes.


Frg. 1-3.-Specific weight for 36 American aireraft engines.
and 4,000 lb . The power loadings for typical American airplanes in the 1,000- to 4,000-ll). class are shown in Fig. 1-5.

The effect of power loading on maximum speed is shown in Fig. 1-6. Points well below the trend line are evidence of ineffective aerodynamic cleanliness. Points far above may be due to unusually good streamlining or to excessive optimism on the part of the manufacturer.
3. From the relation b.hp. $=P_{B} L A N_{e} n / 33,000$, it is apparent that power output is a function of size, speed, and pressure.


Fig. 1-4.-Proportion of engine weight to gross weight for 22 American airplanes in the $1,000-$ to $4,000-\mathrm{lb}$. class.


Fig. 1-5.--Power loadings for 22 American airplanes in the $1,00(1-10$ 4,000-1b. class.

Rigid weight limitations obviously control the size of engine that may be used, and the speed is limited very largely by the propeller efficiency. Reduction gears may be used where the added complexity and cost per horsepower is warranted. With reduction gearing, speed limitations are imposed by the valve gear and by crankpin loadings. Increase in the effective work-
ing pressure is one of the most valuable methods of increasing the specific power output. Some increase in b.m.e.p. $\left(=P_{B}\right)$ can be obtained by increasing the compression ratio (Fig. 1-7A). Greater increases are possible by supercharging (Fig. 1-7B). The


Frg. 1-6.-Power loading vs. maximum speed for 22 American airplanes.


Fig. 1-7A.-Effect of compression ratio on performance. (S.A.E. Journal, Vol. 41, No. 4, October, 1937.)
limits on both of these methods are fixed by the ability of the fuel to withstand detonation, i.e., by the octane number of the fuel to be used, and by the maximum allowable cylinder pressures. Higher maximum pressures mean heavier cylincler construction, hence increased specific weight. This incidentally,
is an important obstacle to successful use of the Diescl-type aircraft engine. Figure $1-8$ shows the b.m.e.p. vs. brake horsepower for 42 American engines. The b.m.e.p.crusisng was taken from manufacturer's data; the b.m.e.p. max was determined (see Table A1-13) from b.m.e.p. $._{\text {max }}=1 / 0.75 \times 0.9 \times$ b.m.e.p.cruieing.


Fig. 1-7B.-Effect of octane number on performance. (S.A.E. Journal, Vol. 41, No. 4, October, 1937.)


Fig. 1-8.-Brake mean effective pressure at cruising horsepower for 42 American aircraft engines. $X$, not supercharged; 0 , supercharged, $\perp-1: 1$ blowor.

The effect of supercharging on b.m.e.p. and horsepower is shown in Figs. 1-9A and 1-9B. Figure 1-10 shows the limitations placed on b.m.e.p. by the octane number. In this figure, points above the mean line $E F$ indicate good combustionchamber and cooling design. Points far below this line indicate either poor design or use of unnecessarily expensive fuels. Specified octane number vs. compression ratio for 23 American aircraft engines is shown in Fig. 1-11.


Fig. 1-9A.-Brake mean effective pressure vs. manifold boost for a $233 \mathrm{cu} . \mathrm{in}$. supercharged engine at 1,000 r.p.m. (Air supplied by a separately driven blower.) (From Snoed, An Investigation of Some of the Fundamentals of Supercharging, S.A.E. Annual Meeting Paper, 1938.)

Fig. 1-9B.-Effect of manifold boost on indicated horsepower. Actual engine data from a $233 \mathrm{cu} . \mathrm{in}$. supercharged engine at $1,000 \mathrm{r} . \mathrm{p} . \mathrm{m}$. (Air supplied by a separately driven blower.) (From Sneed, An Investigation of Some of the Fundamentals of Supercharging,S.S.E. Annual Meeting Paper, 1938.)


Fig. 1-10.-Cruising b.m.e.p. vs. octane number for 47 American and 33 foreign airplane engines.

It should be borne in mind, however, that increase in the manifold pressure, i.e., the amount of supercharge, also is limited by the octane number of the fuel. This largely accounts for the variation in octane-number requirements of different engines having the same compression ratio.


Fig. 1-11.-Octane-number requirements of 23 American aircraft engines.


Frg. 1-12.-Effect of compression ratio on specific: fuel consumption for 22 American aireraft engines.
4. Fuel economy is important in aircraft engines not only from a fuel-cost standpoint but also because the effect is cumulative, since the fuel has to be carried. Fuel rates attained in operation are affected by the percentage of rated power used and by the adjustment of the mixture control. Recently, much attention has been focused on economical mixtures owing in part to the
use of exhaust-gas analyzers as a means of indicating good mixture adjustment. However, limitations are imposed by permissible cylinder temperatures. Higher compression ratios (Fig. 1-12) are a means of improving economy, but this necessitates more expensive fuels or resort to "fuel cooling" by richer mixtures. Currently attained economy of operation is indicated in Fig. 1-13. These values represent manufacturers' guarantees rather than best possible performance, however.
5. Engine compactness is essential to low parasite drag, but for direct cooling (air cooling), limitations are imposed by the necessity of getting rid of a very large amount of heat through

the fins per unit of time. In liquid-cooled engines, the problem is merely shifted from the engine to the radiator. All the heat liberated in the cylinder except that converted into work must ultimately be removed and given up to the surrounding air. Thermal efficiencies vary from 25 to 35 per cent; hence 65 to 75 per cent of the heat energy in the fuel must be disposed of at a rate sufficient to prevent temperature rises above allowable limits. It is apparent that improving the thermal efficiency simplifies the cooling problem. In the larger sizes of engines, cooling becomes a limiting factor to cylinder dimensions.

Weight limitations are also closely related to compactness. Obviously, the more elongated and spread out an engine is, the more difficult it becomes to keep the specific weight within allowable limits. In this respect, radial engines are generally conceded to have some advantage over other types.
6. In commercial operation, reliability is of great importance. Forced landings and crashes with resulting newspaper hearllines are about the best negative publicity an airline can have. More directly, they are tremendously expensive in both equipment and personnel.

In military work, reliability is equally important. Failure of equipment at a crucial moment may mean the difference between victory and defeat. The old saying "Because of a nail the horseshoe was lost, etc., down to the loss of the Army" is just as applicable to the working parts of an airplane engine. In the air, no item, however minor, is entirely unimportant.

Operating life between overhaul periods directly bears on the revenue-producing ability of aircraft engines. For a given schedule of operations, the longer the life between major servicing periods, the fewer reserve engines necessary and the less the nonrevenue-producing investment. Skilled-labor requirements are also a major item of cost in keeping equipment in service.
7. The relative ease of maintenance is determined very largely by the simplicity of design and by the use of standard parts in so far as possible. Manufacture to very close dimensional limits is essential to reliability, but it also aids in permitting the interchangeability of parts on like engines. Reduction in the repair-parts inventory is most desirable.
8. In the ultimate, the usefulness of all commereial products is determined by their cost. Regardless of the perferetion of the design and manufacture, the product cannot compete if it is $t(x)$ costly. In the case of the airplane engine, the raw materials iron, nickel, aluminum, etc., in their initial states are relatively inexpensive. Fabrication is the major item, and that is largely determined by complexity of the design. The simplest design that will meet the requirements is generally the most satisfactory when all items are considered.
9. Ability to operate under adverse conditions is probably more important in the aireraft engine than in any other type of prime mover. In addition to the requirement of unfailing reliability, the engine is called upon to operate in widely varying positions and extreme altitudes. These requirements dictate dual ignition, a dry-sump crankcase, special carburetor design, and numerous other special features that are relatively much less important in engines for land or marine craft.

1-3. Government Requirements.-Primarily for the purpose of maintaining reasonable safety standards, the Federal Civil Aeronautics Authority has been given extensive control over American aviation. In the engine field, the control consists in forbidding the use of engines not approved by the CAA.

To receive approval, an engine must successfully pass a number of exacting tests and meet certain other requirements. Hence, it is important for the designer to know the nature of these requirements. Current requirements for approval of engines are known as Civil Air Regulations, Part 13, "Aircraft Engine Airworthiness." In addition, the CAA has prepared. Civil Aeronautics Manual 13, "Aircraft Engine Airworthiness" which is "intended to interpret, explain and suggest methods of compliance with the regulations. . . ." Both of these publications should be available to the designer.

## References

1. Wood: "Airplane Design."
2. Wood: "Technical Aerodynamics.".

## Problems

1. An airplane of aerodynamic cleanness halfway between class 1 and class 2 (Fig. 1-1), has a gross, weight of $2,250 \mathrm{lb}$., a landing speed of $47 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. with flaps, and a maximum lift coefficient of 2.19. What brake horsepower is developed by the engine when the plane is flying at its maximum speed of 162 m.p.h.? (Assume the propeller efficiency at maximum speed is 83 per cent.)
2. For a wing area of 180 sq. ft., a wing loading of 15 lb . per sq. ft., a propeller efficiency of 81 per cent, and a maximum speed of $150 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. , what equivalent flat-plate area of parasite resistance is implied in Eq. (1-3)? To what class of airplane does this correspond (Fig. 1-1)? If the wing loading were 10 lb . per sq. ft., what class of airplane would be implied?
3. $a$. What values of $f / S$ are implied by Eq. (1-3) at values of $P / S$ of 0.3 , 1.0 , and 3.0 if the propeller efficiency is assumed to be 80 per cent?
$b$. What kinds (classes) of $5,000-\mathrm{lb}$. airplanes do the above (part $a$ ) $P / S$ values represent if the wing loadings are 12 lb . per sq. ft.?
4. a. For values of $f / S$ of $0.015,0.025,0.035$, and 0.045 , find the value of $K$ in the equation $P=S\left(\frac{V_{\max }}{K}\right)^{3}$. Assume $\eta=0.8$.
b. Plot curves of $P=S\left(\frac{V_{\max }}{K}\right)^{3}$ for the values of $K$ found in part $a$ on logarithmic paper using $P / S$ as the ordinate and $V_{\max }$ as the abscissa. Superimpose the mean line in Fig. 1-2 for comparative purposes.
5. Plot Fig. 1-3 on logarithmic paper, and determine an expression for variation of specifice weight with size (i.e., b.hp.).

## CHAPTER 2

## OUTLINE OF THE PROJECT

2-1. Selection of the Potential Market.-The logical first step in designing an airplane engine is to determine the size, i.e., the performance desired. This will, of course, depend upon the use to which the engine will be put and the type, size, and performance of the plane that the engine will power. For practically all engines, with the possible exception of designs for special racing purposes, the ultimate object is to build a unit, that can be sold profitably and that will produce results in competition with other engines sufficient to attract further orders. The decision of first cost vs. operating cost, reliability, and operating life must be made in order to establish a "policy" in selecting materials, dimensions, compression ratios, accessories, etc.
For instance, an engine designed for the low-cost light plane? would incorporate good materials sufficient for reasonable reliability, but the designer could not specify the very best, known high-strength alloys because that would push the rest, above competitive levels. Instead, he would be obliged to use heavier sections of less expensive materials to provide the: necessary strength, and that would increase the weight per horse-power. To keep the cost down, he would be obliged to omit, special features such as superchargers and antomatic: mixture controls and, in extreme cases, possibly reduction gearing or the dry-sump crankease type of lubrication. To mable the purchaser of the engine to use low-cost fuels, the designer will have to keep the compression ratio down, and this will mean a sacrifice in performance.

On the other hand, if an engine is to be designed for a highperformance military plane, first cost (within reason) beeromes secondary and every means at the disposal of the designer should be used to attain maximum power with reasonable ceronomy. For use in a large transport plane, first eost is important, but
not to the extent of a light-plane engine. Low weight per horsepower is essential, and fuel economy is vital. This will mean the use of stronger alloys, higher compression ratios, and greater supercharging. The resulting higher.first cost will be justified by reduced operating and maintenance cost and by the ability to increase the specific pay load.

Obviously the potential market for the engine must be well defined before the design is begun.

2-2. Selection of Rated Power.-The market having been selected, the rated power may be decided upon. Here again cost vs. performance enters. For instance, any given airplane will operate with quite a range of engine sizes. The engine builder must decide whether he can make more money by building an engine that will appeal to the user who is willing to sacrifice high speed for lower operating cost, or vice versa. This decision is in no essential different from that which must be made by the manufacturers of any other product. Essentially, the decision becomes "will the company cater to a large market with small profit per unit or to a more limited market with greater profits per unit?" At best, by the very nature of things, some factors must be left to chance.

2-3. Preliminary Specifications.-Preliminary specifications may now be drawn as indicated in Table 2-1. In general, for each item the decision of what value to use is largely a compromise between the best possible value and the one that will keep costs within allowable limits. Here the accumulated experience of the designer becomes very important.

The fundamental principles of the basic sciences are very useful in the design of complex machines, but derived formulas are either not available or are too complicated to be practical in many of the more intricate parts. Hence, empirical rules based on accumulated experience must be used. Many of these rules are merely the judgment of the designers based on methods that have been found to be satisfactory. To a considerable extent, they are the results of the trial-and-error method.

Unfortunately, progress is slow in the school of experience, and for the beginner, the way forward is anything but clear. Specifically, if the inexperienced designer of airplane engines is to short-cut the long winding road, he must rely heavily upon
landmarks established by others. He must base his decisions regarding the major portion of the items upon the findings and experiences of his predecessors. In proceeding with the design, the student should assume the attitude that his" "company" is going to spend a lot of money on his recommendations. If he departs too widely from convention, he is shifting the projecet from an investment to a gamble.

This recommended adherence to convention should not be: construed as a reactionary attitude toward new methords and progress. Rather, it is based on the belief that improvement, in an existing art cannot very logically be made until current methods, limitations, and shortcomings are thoroughly understood.

2-4. Justification of Values in Example 1.-1, 2. Solection of values for Table 2-1 probably can be best discussed by means

Table 2-1.-General Specifications
Specification Item Example: 1

1. Brake horsepower:
a. Maximum for take-off................... . 125 at sea level
b. Cruising................................ . . . 94
c. Maximum except take-off. .............. . . 125
2. Revolutions per minute:
a. For take-off. . . . . . . . . . . . . . . . . . . . . . . . . 2,000
b. For cruising. . . . . . . . . . . . . . . . . . . . . . . . 1, 800
c. For maximum except take-off hp....... 2,000
3. Octane number of fuel used:
a. For take-off. . . . . . . . . . . . . . . . . . . . . . . . . 73
b. Cruising and maximum except take-off. . 73
4. B.m.e.p., lb. per sq. in.:
a. Maximum for take-off.................... 120
b. Cruising. .................................. . . . 100
c. Maximum except take-off................ 120
5. Compression ratio 5.3
6. Type of cycle (two or four stroke)......... 4
7. Type of cooling. . ........................... . . Air
8. Arrangement of cylinders.................. Radial
9. Number of cylinders and tenative size..... Five $41 / 21$,y 536 in.
10. Connecting rod-crank ( $L / R$ ) ratio........ 4/1
11. Valve arrangement......................... Overhead, inclined, valve in head, rocker arms, and push rods
12. Method of supercharging

None
13. Ignition system

Dual magnetoss
14. Reduction-gear ratio

1:1
of the example. In this particular case, the "engine company" plans to build a unit for the medium-light plane class. Usual power loadings in this class ( 1,500 to $2,500 \mathrm{lb}$. gross weight) range from 10 to 20 lb . per hp. (Fig. 1-5) with a fair average at about 16 for a $2,000-\mathrm{lb}$. plane. Hence the engine will have to develop $2,000 / 16=125 \mathrm{~b} . \mathrm{hp}$. at full throttle and rated speed. This rating is based on sea-level performance since, for the purpose intended, most of the operation will be at relatively low altitudes.

Some engines are given a special horsepower rating for take-off above that which they can safely develop for extended periods. Under these conditions, take-off horsepower is for limited periods of a few minutes only, as the engine would overheat if operated continuously at take-off horsepower. A special take-off highoctane fuel may be used when take-off power is developed. Under these special conditions, item $1 c$ may be considered as the maximum safe horsepower for extended operation. For the example, however, the added cost of providing for extra take-off power, i.e., high supercharge and special fuel, is not considered justifiable, and item $1 a$ is specified as equal to the maximum fullthrottle power for continuous operation.

The specified speed of 2,000 r.p.m. is selected because (a) propeller efficiencies drop rapidly at speeds above this figure and (b) reduction gearing would add too much to the cost of the engine. From Fig. 1-6, the corresponding top speed of the plane may be assumed to approximate $135 \mathrm{~m} . \mathrm{p} . \mathrm{h}$.

There is an increasing tendency in the aviation industry toward designing the engine to fit a specific plane. When potential sales warrant such a procedure, the power of the engine is determined by the particular requirements of the plane. In such cases, sufficient data will be available to permit the use of Eq. (1-2).

The cruising horsepower (Table A1-13) should be about 75 per cent of the take-off horsepower, and the corresponding cruising speed will be about 90 per cent of take-off speed, hence the selection of 94 cruising hp at $1,800 \mathrm{r} . \mathrm{p} . \mathrm{m}$.
3. To avoid the extra cost of premium fuels, an octane number of 73 is specified.
4. Brake mean effective pressures in the $75-$ to $150-\mathrm{hp}$. (cruising) class range around 100 lb . per sq. in. (Fig. 1-8). For a

73 octane number fuel, a higher value might be used (Fig. 1-10), but it might be difficult to attain without supercharging (see item 12, Table 2-1). Since b.m.e.p. may be expressed by the relation

$$
P_{B}=\frac{\mathrm{b} . \mathrm{hp} . \times 33,000}{L A N_{t} n}
$$

the b.m.e.p. for take-off conditions is
$P_{B}($ take-off $)=\frac{\mathrm{b} \cdot \mathrm{hp} . \text { (take-off) }}{\text { b.hp. (cruising) }} \times \frac{\text { r.p.m. (cruising) }}{\text { r.p.m. }(\text { take-off })}$
$\times P_{B}$ (cruising)
or

$$
P_{B}(\text { take-off })=\frac{125}{94} \times \frac{1,800}{2,000} \times 100=120 \mathrm{lb} . \text { per sic. in. }
$$

Referring to Fig. 1-10, it is seen that this value is still within the range of 73 octane number fuel. Hence, a sperial fuel for take-off will not be necessary.
5. Compression ratio is limited by the octane number of the fuel, and for a knock rating of 73, a value of 5.3 for the CH should be satisfactory (Fig. 1-11).
6. Two-stroke-cycle engines for aireraft are still largely in the experimental stage; hence much greater assurance of success will be had by adhering to the more conventional four-strokecycle principle.
7. Direct air cooling climinates the cost of radiators and troublesome piping. The absence of any water-cooled engines in the power class in which this engine falls. (Table A1-1) is good evidence that previous attempts at water or licuid cooling have not been able to meet the competition of the air-cooled engines. Profiting by the experiences of others is a good way $t$, avoid red ink on the ledgers.
8. As regards arrangement of cylinders, Table A1-1 indicates that radials predominate in the power class under consideration. However, the inverted in-line engine is also in considerable evidence, and the flat-opposed or 180 -deg. V-engine has much to recommend it for certain types of installations such as in the wings of bimotored ships. In the final decision, the company designer will probably be influenced by the president's ideas on cylinder arrangement, but for the present purpose, it is of interest, to list some of the important items as follows:

| Item | Air-cooled radial | Air-cooled in-line | Air-cooled opposed |
| :---: | :---: | :---: | :---: |
| Crankcase. | Compact and rigid | Must be heavier for necessary rigidity | Intermediate for same powered engine |
| Cylinders | All equally exposed to cooling air | Careful cowling necessary to cool rear cylinders adequately | Some cowling to deflect air on rear cylinders except in the smallest sizes |
| Crankshaft. | Short and rigid, heavily loaded crankpin. Counterweights necessary | Heavier for necessary stiffness. Usually no counterweights | Intermediate for same powered engine |
| Valve gear | Push rod and rocker arm limit speed of geared engine | Overhead camshaft may be used, less' noisy, - less maintenance, but tends to limit valve size | Push rods and rocker arms or two overhead camshafts |
| Parasite drag. . | Considerable even with cowling, especially in wing engines. Nose engines increase fuselage drag because of slip stream | Less frontal area, but necessary air scoop for cooling adds to total drag | More adaptable for cowling in wing, but cooling-air scoop adds to total drag |
| Visibility in sin-gle-engine tractor-type plane | Relatively obstructed | Excellent for inverted type | Better than radial |

Many other items, varying in importance between the types, will come to mind, but the foregoing comparison is sufficient to indicate that none of the three arrangements of cylinders is outstandingly superior. For example 1, a radial has been selected.
9. Firing order in a single-bank radial very nearly dictates an odd number of cylinders. The greater the number of cylinders, the greater the overlap of power impulses, hence the smoother the torque curve; but fower cylinders means a smaller number of parts and usually lower cost. Increasing the number of cylinders beyond seven in a single-bank radial increases the over-all
diameter and parasite drag. Fewer and larger eylinders are more difficult to cool, since for a given cooling-fin derign, the volume increases as the cube of the dimensions, whereas the surface area of the cylinder increases only as the square. However, this will probably not be a limiting factor so soon as torquecurve variation in the size of engine under consideration. For the example, 5 cylinders have been selected as the compromise of the logical possibilities, 3,5 , or 7 .

From the relation,

$$
\text { b.hp. }=\begin{gathered}
P_{B} L A N_{e} n \\
33,000
\end{gathered}
$$

the displacement per cylinder is

$$
\begin{aligned}
D & =12 L A=\frac{125 \times 33,000 \times 12}{120 \times \frac{2,000}{2} \times 5} \\
& =82.5 \mathrm{cu} . \text { in. for the example }
\end{aligned}
$$

Ratios of stroke to bore vary rather widely (Table A1-1), and they are quite of ten dictated by the desire to increase the number of interchangeable parts in models of similar design but different power output. A low stroke-bore ratio reduces the over-all diameter, hence the parasite resistance, but it increases the distance the 'heat has to flow to escape from the center of the piston. This generally means a heavier piston and a greater weight of reciprocating parts. A stroke-bore ratio of 1.2 is tentatively selected as representing good practice. This will permit the later development of a larger engine in which many of the parts in the present model can be used. The larger unit will doubtless have larger diameter eylinders, but by using a fairly high stroke-bore ratio in the present model, a reasonable stroke-bore ratio can still be had in the larger model with the same crank-arm radius. The cylinder dimensions are found from

$$
\begin{aligned}
D & =S \times d^{2} \times \frac{\pi}{4}=\frac{1.2 \pi}{4} d^{3} \\
d & =\left(\frac{82.5 \times 4}{1.2 \times \pi}\right)^{1 / 3}=4.45 \text { in., bore } \\
S & =1.2 \times 4.45=5.34 \text { in., stroke }
\end{aligned}
$$

As cylinder dimensions are usually specified to the nearest righth of an inch, the bore and stroke may be taken as $4 \frac{1}{2}$ by $53 / \mathrm{x}$ in.

Referring to Table A1-1, it is seen that these values compare favorably with bore and stroke values for similar sizes of engines.
10. Ratios of center-to-center length of connecting rods to crank-arm radii ( $L / R$ ratios) vary from about 3.3 or less to as high as 4.5. The longer the connecting rod in proportion to the crank radius, the less the angularity between the connecting-rod axis and the cylinder center line, hence the less the side pressure, i.e., friction against the cylinder wall. But large values of $L / R$ mean greater over-all transverse dimensions of the engine, hence greater parasite drag. A compromise value of $L / R=4$ has been selected for Example 1.
11. For a radial engine, rocker arms and push rods are about the only feasible means of transmitting the cam-follower motion to the valves. Inclined valves in the head are specified to permit maximum valve port openings and as direct a flow as possible for the gases. To attain the b.m.e.p. specified, a high volumetric efficiency will be necessary, but two intake valves per cylinder would be objectionable because of complexity and cost.
12. Gear-driven centrifugal blowers are conventional for supercharging radial engines, but supercharging is omitted in this example to keep down the cost. To attain equal mixture distribution to the various cylinders in a radial engine, a centrif-ugal-type blower directly connected to the rear end of the crankshaft is desirable. For later more powerful models, this blower may be converted to a supercharger by gearing it for a speed higher than the crankshaft r.p.m.
13. Two magnetos are specified for safety and reliability and to conform with government requirements. Dual ignition will also increase the power output slightly.
14. A reduction gear between the propeller and crankshaft will not be necessary ( $1: 1$ indicates direct drive) as no appreciable loss in propeller efficiency will be had at the crankshaft speed specified.

2-5. Preparation of Design Data and Drawings.-Design data to) be of value must not only be accurate but also be in logical form and neatly prepared. A jumbled array of illegible calculations and incomplete penciled drawings is of little value no matter how accurate. Your employer will judge the quality of your work by its neat appearance in the same general way that you are influenced toward a new car by the appeal of streamlined
contours and glistening finish. In either case, the quality of the product may or may not be high, but to sell it, it must look right. The inner quality will determine the repeat orders.


Fig. 2-1.-Suggested arrangement of title and tahle-of-contents pages.


Fig. 2-2.-American Society of Mechanical Engineers rerommended drawingpaper size and arrangement.

It is recommended that design notes and completed drawings be kept in a standard $81 / 2-$ by $11-\mathrm{in}$. three-ring notebook. The first page of the notebook should be a title sheet, the second a table of contents (Fig. 2-1), and each section of the work should
be identifiable by a small tab attached to the first sheet of the section. This tab should have a title or section number conforming to the title and section number in the table of contents. Subtitles should follow each section title, and their location in the section should be by section page number. Each drawing should be identifiable by a suitable designating letter or number


Fig. 2-3.-Suggested title block for working drawings.


Frg. 2-4.-Suggested method of folding drawings for insertion in design notebook. An alternate method of folding so that the title block shows when folded is standard practice with many companies.
and title both on the drawing and in the table of contents. In all cases, tabulated data, calculations, and graphical constructions should be titled, accompanied by adequate explanations, and, as applies, by sample calculations.

Whenever possible, drawings should be on standard sizes of paper and in all cases properly titled (Fig. 2-3). For insertion in the notebook, drawings should be blueprinted and folded as
indicated in Fig. 2-4. Drawings should be complete. A drawing returned by the production department for lack of adequate dimensions or other data is a direct reflection on the engineering department and the designer. Repeated offenses usually result in the individual's failure to receive "promotion."

## Suggested Design Procedure

1. Select the class of plane for which an engine is to be designed. Tabulate the approximate weight, performance, parasite drag (if available), and other pertinent data.

It is recommended that, for undergraduate students, the seleetion be eonfined to the medium- or light-plane class as large planes require engines of more cylinders, greater complexity, etc., and this greatly increases the detail work necessary in designing the engine without adding proportionately to the fundamental knowledge gained. Also in most undergraduate courses, the time available for the design work is insufficient for those added details.
2. Prepare a table of general specifications similar to Tahle 2-1.

Adhere closely to current practice in deciding upon the type of engine to be designed. Confine the selection to (a) a single-bank radial of preferably not more than seven cylinders, (b) an in-line type of not more than six cylinders, or (c) a V type of not more than eight cylinders.

In limiting the selections to the preceding types, it is not the purpose to suppress originality or potential inventive genius, but rather to require the selection of a problem that the beginner can have a fair chance of completing. As an instance of the pitfalls of allowing unlimited selections, a case is recalled in which a student was permitted, in his first undergraduate course in engine design, to select any type of engine he desired, and, without knowing of the difficulties ahead, he selected a threc-lobe-cam engine. Almost immediately, innumerable questions arose concerning logical values for this detail and proper sizes for that part. Without precedent to guide him, he: soon became hopelessly lost and little was accomplished. The inexperienced designer will have problems enough with a conventional type of engine. Later, when he has acquired experience, he can depart from the conventional if he chooses.
3. Justify each specification item by reference to current pration wherever possible and by reference to the allowable eost decided upon.

Hasty selection of the general specifications is false economy of time, as specifying impossible values may mean the repeating of a great deal of tedious calculation farther on.
4. Make a line layout of (a) a transverse section and (b) a longiturdinal section through the engine at the eylinder center lines. Show the location and desired sizes of the principal parts. Indicate desired dimensions of important parts, positions of center lines, etc., but do not try to make a complete detailed drawing* at this stage of the design. ('herek rlosest powi-

[^1]tion of connecting-rod center line to lower end of cylinder. (Cylinder must extend down approximately as far as the lowest position of the bottom of the piston skirt.) Check all features of desired arrangement to be reasonably certain of adequate mechanical clearance of parts. Inspect available blueprints, drawings, engine parts, etc., of similar designs for assistance in selecting logical sizes for the various parts.

This preliminary layout drawing should be developed with the idea in mind that it is the general arrangement desired. At best, some detail changes will be necessary before the final design is completed, but if too radical an arrangement is attempted, major changes may have to be made. This will greatly increase the work necessary later. Hence, it is very desirable to give careful study to the proposed arrangement. The layout need not be blueprinted at this stage, but it should be to a large enough scale to permit close study and on standard-size paper properly titled (size $D$ or $E$, Fig. 2-2, is recommended).
5. When items 1 to 4 have been completed and put in proper form (Par. $2-5$ ), submit for checking and approval. Keep a record of the man-hours required on each item.
bound the region as accurately as possible and to insert the position of important features such as rivers, lakes, and mountain chains (i.e., major dimensions, center lines, etc.). Obviously, the details will have to be added. gradually as the information becomes available, but it should be borne in mind that unnecessary carelessness or poor judgment in the preliminary layout will result either in doubtful accuracy of the finished product or a great deal of time-consuming revision that might have been partly avoided.

The successful designer also has something in common with the successful artist who, in preparing the layout for a painting, is able to visualize in his mind's eye the appearance of the finished product. It takes years of practice to perfect this ability, but the greatest attainments always have been made by men (engineers as well as artists) who put everything they had into every job at the beginning as well as at the height of their careers.

## CHAPTER 3

## GAS-PRESSURE FORCES

3-1. Forces in the Cylinder.-Forces on the piston represent a combination of gas pressure and inertia forces. These forces are usually determined separately at increment angular positions; of the crankshaft, plotted as unit or total force against crank angle, and then, by adding ordinates, a curve of the net force parallel to the cylinder axis is obtained. As the dimensions of the various parts of the engine are largely determined by the stresses resulting from the maximum forces, it is obviously necessary to investigate the case causing these extreme conditions, i.e., full throttle and highest speed.

3-2. Construction of the Indicator Card.-For the gas-pressure forces, it is necessary to construct an indicator card representing full-throttle conditions. Very elaborate procedures have been developed ${ }^{1,2}$ for analyzing the phenomena in engine cylinders with the idea in mind of more closely approaching actual conditions. However, even with the most complex of these methods, some discrepancies exist and must be accounted for by a "card factor." It is believed that simpler methods of retermining values for the indicator card, although admittedly less rational, are more practical and may be applied just as effectively by using a somewhat larger card factor. In short, instead of endeavoring to account for variable specific heats, dissociation, chemical equilibrium, heat flow back and forth between the gasess and the cylinder, and then applying a small card factor, use valuss for the exponents of compression and expansion consistent with actual measured results from engines that have been indicated, calculate the pressures and volumes by the older and much simpler thermodynamic relations of the modified "air-standard" cycle, and then apply a slightly larger card factor. The valuess for plotting may be found as follows:

Determine the i.m.e.p. from

$$
\begin{equation*}
\text { i.m.e.p. }=\frac{\text { b.m.e.p. }}{e_{m}} \tag{3-1}
\end{equation*}
$$

where i.m.e.p. $=$ indicated mean effective pressure, lb . per sq. in.
b.m.e.p. $=$ brake mean effective pressure at maximum horsepower ( $=$ take-off horsepower), lb. per sq. in.
$e_{m}=$ mechanical efficiency at take-off horsepower. The absolute pressure at the end of expansion may be found from ${ }^{3,4}$

$$
\begin{equation*}
P_{D}=\frac{(n-1)(R-1)}{R^{n}-R} \times \frac{\text { i.m.e.p. }}{F_{D}}+P_{A} \tag{3-2}
\end{equation*}
$$

where $P_{D}=$ pressure at end of expansion, lb. per sq. in. abs.
$n=$ exponent of the compression and expansion curves.
$R=$ compression ratio.
$F_{D}=$ card factor representing the ratio of actual to theoretical card areas.
$P_{A}=$ pressure at the beginning of compression, lb. per sq. in. abs.

$$
\begin{align*}
& P_{C}=P_{D} \times R^{n}  \tag{3-3}\\
& P_{B}=P_{A} \times R^{n} \tag{3-4}
\end{align*}
$$

where $P_{c}=$ pressure at the beginning of expansion, lb. per sq. in. abs.
$P_{B}=$ pressure at the end of compression, lb. per sq. in.
Cylinder volumes corresponding to the foregoing pressures may be found by combining the relations

$$
\begin{align*}
V_{A}-V_{B} & =D  \tag{3-5}\\
\frac{V_{A}}{V_{B}} & =R \tag{3-6}
\end{align*}
$$

where $V_{A .}=$ cylinder volume at the beginning of compression, cu. in.
$V_{B}=$ clearance volume, cu. in.
$D=$ piston displacement for one cylinder, cu. in.
Also

$$
V_{A}=V_{D} \quad \text { and } \quad V_{B}=V_{C}
$$

where $V_{D}=$ cylinder volume at the end of expansion, cu. in.
$V_{c}=$ cylinder volume at the beginning of expansion, cu. in.

Intermediate pressures along the compression line may be found from

$$
\begin{equation*}
P_{1,2,3, \text { etc. }}=\frac{P_{B} V}{V_{1,2,3, \text { etc. }}^{n}} \tag{3-7}
\end{equation*}
$$

$V_{1,2,3}$, etc. being found by measuring along the abscissa or volume line to scale. Similarly, intermediate pressures along the expansion line may be found.

An alternate method of finding intermediate pressures is to plot points $\cdot P_{A} V_{A}, P_{B} V_{B}, P_{C} V_{C}$, and $P_{D} V_{D}$ on logarithmic crosssectional paper and connect successive points by straight lines. Pressures corresponding to any intermediate volumes may be read directly from the ordinate scale.


Fig. 3-1.-Graphical construction of a $P V^{n}=$ constant line.
A graphical method of plotting compression and expansion lines is illustrated in Fig. 3-1. For instance, to construct a compression line, lay off coordinates $O V$ and $O P$ and locate point $P_{A} V_{A}$. Select $\alpha$ and $\beta$ such that $(1+\tan \alpha)^{n}=1+\tan \beta$. Draw $O H$, making the angle $\alpha$ with $O V$, and $O L$, making the angle $\beta$ with $O P$. Erect a line perpendicular to $O V$ at $V_{A}$. Construct angle $O V_{A} a$ equal to 45 deg. Erect a line through $a$ perpendicular to $O V$. Construct $P_{A} b$ perpendicular to $O P$. Construct angle $b P_{1} O$ equal to 45 deg. Draw a line through $P_{1}$ parallel to $O V$. The intersection of the perpendicular line through $a$ and the horizontal line through $P_{1}$ locates point $P_{1} V_{1}$. Construct angle $O V_{1} c$ equal to 45 deg. Frect a line through $c$ perpendicular to $O V$. Extend the horizontal line through $P_{1}$ to $l$. (ionstruct
angle $d P_{2} O$ equal to 45 deg . Draw a line through $P$ datadfete $O V$. The intersection of the perpendicular line throught $c$ and the horizontal line through $P_{2}$ locates point $P_{2} V_{2}$. Proceed in the same way to locate points $P_{3} V_{3}, P_{4} V_{4}$, etc., and connect the points thus located with a smooth curve. The equation of the curve is $P V^{n}=$ a constant.

3-3. Example.-Construct an indicator card for the engine selected in Example 1, Table 2-1.

Procedure.-The b.m.e.p. for take-off horsepower represents maximum conditions. Mechanical efficiency will be that for full load and speed. For


Fig. 3-2.-Logarithmic plot for determining indicator-card data.
these conditions, the mechanical efficiency may be taken as equal to 85 per cent (Fig. A1-2). Then

$$
\text { i.m.e.p. }=\frac{120}{0.85}=141 \mathrm{lb} . \text { per sq. in. }
$$

The average exponent of compression and expansion may be taken as $n=1.3$, the card factor $F_{D}=0.9$, and the pressure at the beginning of compression, $P_{A}=90$ per cent of atmospheric pressure (for a nonsupercharged engine $)^{3,4}$. Then, for the example,

$$
P_{D}=\frac{(1.3-1)(5.3-1)}{53^{1.3}-5.3} \times \frac{141}{n 9}+0.9 \times 14.7=72.7 \mathrm{lb} . \text { per sq. in. abs. }
$$

Let $P_{D}=73 \mathrm{lh}$. per sq. in. abs.
$P_{C}=73 \times 5.3^{1.3}=635 \mathrm{lb}$. per sq. in. abs.
$P_{B}=13.2 \times 5.3^{1.3}=115 \mathrm{lb}$. per sq. in. abs.

The displacement per cylinder is

$$
D=4.5^{2} \times 0.785 \times 5.375=85.5 \mathrm{cu} . \mathrm{in} .
$$

Hence

$$
\begin{aligned}
& V_{B}=85.5 \quad 19.9 \mathrm{cu} . \mathrm{in} .=V_{C} \\
& V_{A}=85.5+19.9=105.4 \mathrm{cu} . \mathrm{in} .=V_{D}
\end{aligned}
$$

Plotting the four points thus determined on logarithmic paper and connecting gives Fig. 3-2. Table 3-1 is obtained by seleeting intermediate volumes and reading the corresponding pressures. The completed indicator card

Table 3-1.-Yndigator-card Data from Figi. 3-2

| Volumes, <br> cu. in. | Compression-line <br> pressures, lh. per <br> sq. in. abs. | Expansion-line <br> pressures, lh. per <br> sq. in. abs. |
| :---: | :---: | :---: |
| 105.4 | 13.2 | 73 |
| 100 | 14 | 76 |
| 95 | 14.95 | 82 |
| 90 | 16 | 87.5 |
| 85 | 17.1 | 94 |
| 80 | 18.4 | 100 |
| 75 | 20 | 110 |
| 70 | 22 | 121 |
| 65 | 24.5 | 132 |
| 60 | 27 | 148 |
| 55 | 30 | 165 |
| 50 | 34.5 | 187 |
| 45 | 39 | 215 |
| 40 | 46 | 250 |
| 35 | 55 | 295 |
| 30 | 66 | 365 |
| 25 | 85 | 460 |
| 22 | 100 | 5.50 |
| 19.9 | 115 | 63.5 |

(Fig. 3-3) is constructed from the data in Table 3-1. The area of this card to the scale drawn is 6.23 sc . in., the length is 4.1 in ., and the spring seale is 100 lb . per in. of ordinate, hence

$$
\text { i.m.e.p. (theoretical) }=\frac{6.23 \times 100}{4.1}: 1: 2 \mathrm{lh} \text {. per siq. in. }
$$

The i.m.e.p. for the assumed actual conditions was 141 lb . per sis. in. Therefore, the card factor should be

$$
F_{D}=141 / 152=0.925
$$

This value checks the originally assumed value of 0.9 reasonably well.
In superimposing the actual card by rounding the corners of the theoretical card, $P_{\max }$ may be taken as about 75 per cent of $P_{c^{3,4}}$. Actually, maximum cylinder pressures vary over a considerable range and depend upon numerous factors, including ignition timing, air-fuel ratio, etc. When a low-octane fuel is used, the maximum pressures are much higher owing to detonation of a part of the charge. In extreme cases of knocking, these pressures can cause serious damage in an engine.


Fig. 3-3.-Indicator card for Example 1 (Table 3-1).
The pressure near the end of the expansion line will drop owing to opening the exhaust valve before bottom dead center (point E.V.O., Fig. 3-3). Usually the pressure will not have expanded to exhaust-stroke pressure until the piston has moved an appreciable distance on the exhaust stroke. This justifies rounding the "toe" of the card.

If the spark occurs too early, the pressure will rise above the compression line before top dead center is reached. This is undesirable, but a greater loss will oecur due to $P_{\text {max }}$ being farther from top dead center if the spark is retarded too much. Hence, some rounding of the card near the end of the compression stroke should be made.

The area of the superimposed "actual" card is 5.73 sq. in. for the example, and

$$
F_{1}, \quad \frac{5.73}{6.23}=0.92
$$

This again checks the originally assumed value reasonably well.
3-4. Gas-pressure-Crank-angle Diagrams.-To utilize the gas-pressure data from the indicator card, it is necessary to convert to a pressure-crank-angle basis. This may be done most conveniently by a graphical construction as illustrated in Fig. 3-4. With reference to this figure, the constructed indicator card is tacked to a drawing board and the atmospheric line or a line


Fig. 3-4.-Graphical method of converting the pressure-volume rard to : pressure-crank-angle basis.
parallel to it is extended as shown. The length of the card parallel to the atmospheric line is directly proportional to the stroke of the piston. Hence, by using this length as a base, all other dimensions may be scaled down accordingly. The atmospheric line may be considered as the center line of the cylinder, and the extension will pass through the center of the crankshaft.* The location of this center may be found by scaling down the connecting-rod length to the scale of the card using the relation

[^2]\[

$$
\begin{equation*}
\frac{S}{S^{\prime}} \quad \frac{L}{L^{\prime}} \tag{3-8}
\end{equation*}
$$

\]

where $S=$ length of indicator card, in.
$S^{\prime}=$ piston stroke, in.
$L^{\prime}=$ center-to-center length of the engine connecting rod, in.
$L=$ center-to-center length of the connecting rod to the scale of the card, in.
Point $O$, Fig. 3-4, is distant from point $P_{E} V_{E}$ by the amount $L+R$ where $R=S / 2$. By using $O$ as a center, construct a


Fig. 3-5.-Gas-pressure-crank-angle diagram for Example 1 (Table 2-1).
circle of radius $R$ and divide the upper half into 10-deg. increments with the aid of a protractor. Set a compass to length $L$, and using the $10-\mathrm{deg}$. increment points $y, y_{1}, y_{2}$, etc., strike arcs intersecting the atmospheric line on the card at $x, x_{1}, x_{2}$, etc. The $x$ points represent piston positions corresponding to crankpin positions $y$. Erect ordinates at the $x$ points, and read the pressures at the intercepts with the card lines directly from the ordinate scale. Convert the pressures to total force by multiplying each by the area of the piston, and plot against crank angle as an uniformly spaced abscissa. As atmospheric pressure is at all times acting on the under side of the piston, the effective gas pressure thrust on the piston is represented by the gage pressure. Hence, it is necessary to convert the ordinate-scale readings to
gage readings. This is most easily done by shifting the ordinate: scale.

3-5. Example.-Construct a gas-foree-crank-angle diagram for the engine selected in Example 1, Table 2-1.

Procedure.-Before locating crank-angle positions on the card (Fig. 3-3), it is necessary to determine the (scale) center-to-center length of the emmecting rod from the $L / R$ ratio. By using the selected value of $L / R=. f$ (Table 2-1), scaling down as explained in Par. 3-4, and making the graphieal construction, the crank-angle positions were located as shown on Fig. 3-3. Ordinates erected to the compression and expansion lines from these prints gave the data from Table 3-2, and these data were used to construct Fig. 3-5.

Table 3-2.-Gas-prmssure, Crank-angie Forees fhom Fig. 3-3
Area of Piston $=15.9 \mathrm{sq} . \mathrm{in}$.


## References

1. Univ. Ill., Eng. Expt. Sta., Bull. 160.
2. Hersey, Eberhardt, and Hottel: Thermodynamic Properties of the Working Fluid in Internal Combustion Engines, S.A.E. Jour., Vol. 39, No. 4, October, 1936.
3. A.S.I.C. 421.
4. Angle: "Engine Dynamics and Crankshaft Design."

## Suggested Design Procedure

1. For the engine selected for your design, construct a full-throttle-fullspeed theoretical indicator card.

If the design is to be supercharged, the effects of the altered inlet pressure must be considered in following the preceding examples.
2. Round the corners of the theoretical card to form the actual card, and determine the card factor.
3. From the actual card thus obtained, determine the indicated horsepower of the engine. Apply the assumed mechanical efficiency, and check the brake horsepower obtained with the originally assumed value of brake horsepower. If a reasonably close agreement is not had, recheck the work for errors.
4. Using data obtained from the actual card, construct a total net gas-force-crank-angle (uniform angular spacing) diagram.
5. When items 1 to 4 have been completed and put in proper form, submit for checking and approval. Keep a record of the man-hours required for each item.

## Problems

1. Using the basic relations of thermodynamics as applied to the modified air standard $O$ Otto cycle, prove that the pressure at the end of the expansion stroke will be as in Eq. (3-2).
2. Referring to Fig. $3-1$, prove that when $(1+\tan \alpha)^{n}=(1+\tan \beta)$ the resulting curve has the equation $P V^{n}=$ a constant.

## CHAPTER 4

## ANALYSIS OF THE CRANK CHAIN

4-1. Forces Due to the Reciprocating Parts.-In converting the reciprocating motion of the piston into the rotating motion of the crankshaft, the inertia forces of the reciprocating parts play an important part in determining the net turning effort. These parts must be started from rest, accelerated to high velocity, slowed to rest, accelerated again, and stopped a second time during each revolution. At the speed at which airplane-engine crankshafts turn, this process causes quite high inertia forces. Analysis of these forces will be first considered for a singlecylinder engine.

## 4-2. Piston Velocity and Acceleration.*

In Fig. $4-1, P$ represents the piston-pin center, $C$ is the rankpin center, $M$ is the center of crankshaft, $L$ is the center-to-center


Fic. 4-1.-Arrangement of crankehain.
length of the connecting rod in inches, and $R$ is the crank radius in inches ( $=1 / 2$ the stroke). For any given displacement ( $\mathcal{S}$ ) in inches from head-end dead center:

$$
\begin{aligned}
S & =L+R-L \cos \phi-R \cos \theta \\
C D & =L \sin \phi=R \sin \theta \\
\sin \phi & =\frac{R}{L} \sin \theta \\
\cos \phi & =\sqrt{1-\sin ^{2} \phi}=\sqrt{1-\frac{R^{2}}{L^{2}} \sin ^{2} \theta}=\frac{1}{L} \sqrt{L^{2}-R^{2}} \sin ^{2} \theta
\end{aligned}
$$

[^3]Therefore

$$
\begin{equation*}
S=L+R-\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}-R \cos \theta \tag{4-1}
\end{equation*}
$$

The velocity corresponding to $S$ is

$$
\begin{aligned}
& V=\frac{d S}{d t}=\frac{1}{2}\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{1 / 2} \times 2 R^{2} \sin \theta \cos \theta \frac{d \theta}{d t}+R \sin \theta \frac{d \theta}{d t} \\
& V=R \sin \theta \frac{d \theta}{d t}+\left[\frac{R^{2} \sin \theta \cos \theta}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}}\right] \frac{d \theta}{d t} \\
& V=R \sin \theta\left[1+\frac{R \cos \theta}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}}\right] \frac{d \theta}{d t}
\end{aligned}
$$

In any practical engine, for a given condition of operation, the angular velocity of the crankshaft is very closely uniform. Therefore, $d \theta / d t=2 \pi N$ where $N$ is in revolutions per minute. Substitution of $2 \pi N$ in the preceding expression gives $V$ in inches per minute. Dividing by $12 \times 60$ gives velocity in feet per second.

$$
\begin{align*}
& V_{\text {t.p.s. }}=\frac{2 \pi N R \sin \theta}{12 \times 60}\left[1+\frac{R \cos \theta}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}}\right] \\
& V_{\text {t.p.s. }}=0.00873 N R \sin \theta\left[1+\frac{R \cos \theta}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}}\right] \tag{4-2}
\end{align*}
$$

The acceleration in feet per sec. ${ }^{2}$ corresponding to $V_{\text {f.p.s. }}$ is

$$
\begin{aligned}
& A=\frac{d V}{d t}=0.00873 N R\{\sin \theta \\
& \left(L^{2}-R^{2} \sin ^{2} \theta\right)^{1 / 2}\left(-R \sin \theta \frac{d \theta}{d t}\right)-\frac{1}{2} R \cos \theta\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{-3} . \\
& \left(-2 R^{2} \sin \theta \cos \theta\right. \\
& L^{2}-R^{2} \sin ^{2} \theta \\
& \left.+\left[1+\frac{R \cos \theta}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{1 / 2}}\right] \cos \theta \frac{d \theta}{d t}\right\} \\
& A=0.00873 N R\left\{\begin{array}{l}
-R \sin ^{2} \theta \frac{d \theta}{d t} \\
\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}
\end{array}+\frac{R^{3} \sin ^{2} \theta \cos ^{2} \theta \frac{d \theta}{d t}}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}}\right. \\
& \left.+\cos \theta \frac{d \theta}{d t}+\frac{R \cos ^{2} \theta \frac{d \theta}{d t}}{\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{1 / 2}}\right\}
\end{aligned}
$$

but $\cos ^{2} \theta-\sin ^{2} \theta=\cos 2 \theta$,

$$
\begin{aligned}
& \sin ^{2} \theta \cos ^{2} \theta=\frac{2(\sin \theta \cos \theta) 2(\sin \theta \cos \theta)}{4} \\
& \frac{d \theta}{d t}=2 \pi N \text { radians per min. } 2 \theta \\
& \frac{2 \pi N}{60} \text { radians per sec. }
\end{aligned}
$$

Therefore,

$$
\left.\begin{array}{rl}
A=0.000914 N^{2} R[ & \cos \theta+\begin{array}{c}
R \cos 2 \theta \\
\left(L^{2}-R^{2} \cos ^{2}\right.
\end{array} \\
& \left.+\frac{R^{3} \sin ^{2} 2 \theta}{4\left(L^{2}\right.}-R^{2} \sin ^{2} \theta\right)^{\overline{3 n}} \tag{4-3}
\end{array}\right] \mathrm{ft} . \text { per sec. }{ }^{2} .
$$

The preceding formulas for velocity and acceleration [Eqs. (4-2) and (4-3)] would be cumbersome to use, and the following substitutions can be made without appreciable error:

Let

$$
\begin{gathered}
L=\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2} \\
Z=\frac{R}{L}
\end{gathered}
$$

Then,

$$
\begin{aligned}
V_{\text {f.D.s. }} & =0.00873 N R \sin \theta(1+Z \cos \theta) \\
& =0.00873 N R\left(\sin \theta+Z \frac{2 \sin \theta \cos \theta}{2}\right)
\end{aligned}
$$

but $2 \sin \theta \cos \theta=\sin 2 \theta$.
Therefore,

$$
\begin{equation*}
V_{\text {t.D.s. }}=0.00873 N R(\sin \theta+1 / 2 Z \sin 2 \theta) \tag{4-4}
\end{equation*}
$$

The term $(\sin \theta+1 / 2 Z \sin 2 \theta)$ is called the piston-velocity factor. In determining the piston velocity at various erank positions, the calculations may be simplified considerably by taking the value of the piston-velocity factor from Table 4-1.

For the acceleration,

$$
A=0.000914 N^{2} R\left(\cos \theta+Z \cos 2 \theta+\frac{1}{4} Z^{3} \sin ^{2} 2 \theta\right)
$$

But the last term $1 / 4 Z^{3} \sin ^{2} 2 \theta$ is small and can be neglected without appreciable error.
Therefore,

$$
\begin{equation*}
A=0.000914 N^{2} R(\cos \theta+Z \cos 2 \theta) \mathrm{ft} \text {. per see. }{ }^{2} \tag{4-5}
\end{equation*}
$$

The term $(\cos \theta+Z \cos 2 \theta)$ is called the pistom-acceleration. factor. Table 4-2 is a convenient aid in determining the piston acceleration at various crank angles.

Table 4-1.-Tangential-forge and Piston-velocity Factors
Values for $(\sin \theta+1 / 2 Z \sin 2 \theta)$

| $\theta$ | $1 / Z$ |  |  |  |  | $\theta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3.50 | 3.75 | $\cdot 4.00$ | 4.25 | 4.5 |  |
| 0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 360 |
| 5 | 0.112 | 0.110 | 0.109 | 0.108 | 0.107 | 355 |
| 10 | 0.223 | 0.219 | 0.216 | 0.214 | 0.212 | 350 |
| 15 | 0.330 | 0.326 | 0.322 | 0.318 | 0.314 | 345 |
| 20 | 0.434 | 0.428 | 0.422 | 0.417 | 0.413 | 340 |
| 25 | 0.532 | 0.525 | 0.518 | 0.513 | 0.508 | 335 |
| 30 | 0.624 | 0.616 | 0.608 | 0.602 | 0.596 | 330 |
| 35 | 0.708 | 0.699 | 0.691 | 0.684 | 0.678 | 325 |
| 40 | 0.784 | 0.774 | 0.766 | 0.759 | 0.752 | 320 |
| 45 | 0.850 | 0.840 | 0.832 | 0.825 | 0.818 | 315 |
| 50 | 0.907 | 0.897 | 0.889 | 0.882 | 0.875 | 310 |
| 55 | 0.954 | 0.945 | 0.937 | 0.930 | 0. 924 | 305 |
| 60 | 0.990 | 0.982 | 0.974 | 0.968 | 0.962 | 300 |
| 65 | 1.016 | 1.008 | 1.002 | 0.997 | 0.992 | 295 |
| 70 | 1.032 | 1.026 | 1.020 | 1.015 | 1.011 | 290 |
| 75 | 1.037 | 1.032 | 1.028 | 1.025 | 1.022 | 285 |
| 80 | 1.034 | 1.031 | 1.028 | 1.025 | 1.023 | 280 |
| 85 | 1.021 | 1.019 | 1.018 | 1.017 | 1.016 | 275 |
| 90 | 1.000 | 1.000 | 1.000 | 1.000 | 1.000 | 270 |
| 95 | 0.971 | 0.973 | 0.975 | 0.976 | 0.977 | 265 |
| 100 | 0.936 | 0.939 | 0.942 | 0.945 | 0.947 | 260 |
| 105 | 0.894 | 0.899 | 0.903 | 0.907 | 0.910 | 255 |
| 110 | 0.848 . | 0.854 | 0.859 | 0.864 | 0.868 | 250 |
| 115 | 0.797 | 0.804 | 0.811 | 0.816 | 0.821 | 245 |
| 120 | 0.742 | 0.750 | 0.758 | 0.764 | 0.770 | 240 |
| 125 | 0.685 | 0.694 | 0.702 | 0.709 | 0.715 | 235 |
| 130 | 0.625 | 0.635 | 0.643 | 0.650 | . 0.657 | 230 |
| 135 | 0.564 | 0.5.4 | 0.582 | 0.589 | 0.596 | 225 |
| 140 | 0.502 | 0.512 | 0.520 | 0.527 | 0.533 | 220 |
| 145 | 0.439 | 0.448 | 0.456 | 0.463 | 0.469 | 215 |
| 150 | 0.376 | 0.384 | 0.392 | 0.398 | 0.404 | 210 |
| 155 | 0.313 | 0.321 | 0.327 | 0.333 | 0.338 | 205 |
| 160 | 0.250 | 0.256 | 0.262 | 0.267 | 0.271 | 200 |
| 165 | 0.187 | 0.192 | 0.196 | 0.200 | 0.203 | 195 |
| 170 | 0.125 | 0.128 | 0.131 | 0.134 | 0.136 | 190 |
| 175 | 0.062 | 0.064 | 0.066 | 0.067 | 0.068 | 185 |
| 180 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 180 |

Table 4-2.-Piston-acceleration and Inertia Factors Values for $(\cos \theta+Z$ cos $2 \theta)$

| $\theta$ | $1 / 7$ |  |  |  |  | $\theta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3.5 | 3.75 | $4.0{ }^{*}$ | 4.25 | 4.5 |  |
| 0 | 1.286 | 1.267 | 1.250 | 1.235 | 1.222 | 360) |
| 5 | 1.277 | 1.259 | 1.242 | 1.22\% | 1.215 | 35\% |
| 10 | 1.253 | 1.235 | 1.220 | 1.20f | 1.19.4 | 350 |
| 15 | 1.213 | 1.197 | 1.182 | 1.170 | 1.159 | 3.45 |
| 20 | 1.159 | 1.144 | 1.131 | 1.120 | 1.110 | $3 \cdot 10$ |
| 25 | 1.090 | 1.078 | 1.067 | 1.058 | 1.049 | 335 |
| 30 | 1.009 | 0.999 | 0.991 | 0.984 | 0.977 | 330) |
| 35 | 0.917 | 0.911 | 0.905 | 0.900 | 0.895 | $32 \%$ |
| 40 | 0.816 | 0.813 | 0.810 | 0.807 | 0.805 | 320 |
| 45 | 0.707 | 0.707 | 0.707 | 0.707 | 0.707 | 315 |
| 50 | 0.593 | 0.596 | 0.599 | 0.6022 | 0.604 | 310 |
| 55 | 0.476 | 0.482 | 0.488 | 0.493 | 0. 498 | 305 |
| 60 | 0.357 | 0.367 | 0.375 | 0.382 | 0.3809 | 3(k) |
| 65 | 0.239 | 0.251 | 0.262 | 0.271 | 0. $2 \times 0$ | 20\% |
| 70 | 0.123 | 0.138 | 0.151 | 0.162 | 0.172 | 2(\%) |
| 75 | 0.011 | 0.028 | 0.042 | $0.05 \%$ | 0.0 (fic | $2 \times 5$ |
| 80 | -0.095 | -0.077 | -0.061 | -0.0.48 | - 10.035 | 280 |
| 85 | -0.194 | -0.175 | -0.159 | -0.145 | -0.1332 | 275 |
| 90 | -0.286 | $-0.267$ | -0.250 | -0.235 | - 0.2222 | 270 |
| 95 | -0.368 | -0.350 | $-0.333$ | -0.319 | $-0.3065$ | 265 |
| 100 | -0.442 | -0.424 | -0.409 | -0.395 | -0.3883 | 260 |
| 105 | -0.506 | $-0.490$ | -0.475 | -0.46:3 | -0.451 | 25\% |
| 110 | -0.561 | -0.547 | -0.534 | -0.522 | -0.5.512 | 250 |
| 115 | -0.606 | -0.594 | -0.583 | -0.57.4 | -0. 0.36 | 215 |
| 120 | $-0.643$ | -0.633 | -0.625 | -0.618 | -0.611 | 280 |
| 125 | -0.671 | -0.665 | -0.659 | -0.65\% 4 | -0.6.00 | 23:35 |
| 130 | -0.692 | -0.689 | -0.686 | $-0.688$ | -0.681 | 2:30 |
| 135 | -0.707 | $-0.707$ | $-0.707$ | $-0.707$ | $-0.707$ | 225 |
| 140 | -0.716 | $-0.720$ | -0.723 | $-0.72 \%$ | -0.727 | 220 |
| 145 | -0.722 | $-0.728$ | -0.734 | -0.739 | -0.743 | 215 |
| 150 | $-0.723$ | $-0.733$ | $-0.741$ | -0.748 | -0.75 | 210 |
| 155 | $-0.723$ | $-0.735$ | $-0.746$ | -0.75\% | -0.76.3 | 205 |
| 160 | -0.721 | $-0.735$ | -0.748 | $-0.760$ | -0. 769 | $2(\mathrm{~N})$ |
| 165 | -0.718 | $-0.735$ | $-0.749$ | $-0.762$ | -0 773 | 195 |
| 170 | -0.717 | -0.734 | $-0.750$ | $-0.76 .4$ | -0.77i | $1(\mathrm{~K})$ |
| 175 | $-0.715$ | -0.734 | $-0.750$ | $-0.76 .4$ | -0.777 | $1 \times 5$ |
| 180 | -0.714 | $-0.733$ | $-0.750$ | -0.765) | -0.77\% | IXI) |

Table 4-3.-Piston-travel Factors
Values for $\left(1-\cos \theta+1 / 2 Z \sin ^{2} \theta\right)$

| $\theta$ | $1 / Z$ |  |  |  |  | $\theta$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 3.5 | 3.75 | 4.0 | 4.25 | 4.5 |  |
| 0 | 0.000 | 0.000 | 0.000 | 0.000 | 0.000 | 360 |
| 5 | 0.005 | 0.005 | 0.005 | 0.005 | 0.005 | 355 |
| 10 | 0.020 | 0.019 | 0.019 | 0.019 | 0.018 | 350 |
| 15 | 0.044 | 0.043 | 0.043 | 0.042 | 0.042 | 345 |
| 20 | 0.077 | 0.076 | 0.075 | 0.074 | 0.073 | 340 |
| 25 | 0.119 | 0.118 | 0.116 | 0.115 | 0.114 | 335 |
| 30 | 0.170 | 0.167 | 0.165 | 0.163 | 0.162 | 330 |
| 35 | 0.228 | 0.225 | 0.222 | 0.220 | 0.217 | 325 |
| 40 | 0.293 | 0.289 | 0.286 | 0.283 | 0.280 | 320 |
| 45 | 0.364 | 0.360 | 0.355 | 0.352 | 0.348 | 315 |
| 50 | $0.441^{\text { }}$ | 0.435 | 0.430 | 0.426 | 0.422 | 310 |
| 55 | 0.522 | 0.516 | 0.510 | 0.505 | 0.500 | 305 |
| 60 | 0.607 | 0.600 | 0.594 | 0.588 | 0.583 | 300 |
| 65 | 0.695 | 0.687 | 0.680 | 0.674 | 0.669 | 295 |
| 70 | 0.784 | 0.776 | 0.768 | 0.762 | 0.756 | 290 |
| 75 | 0.874 | 0.866 | 0.858 | 0.851 | 0.845 | 285 |
| 80 | 0.965 | 0.956 | 0.948 | 0.941 | 0.934 | 280 |
| 85 | 1.055 | 1.045 | 1.037 | 1.030 | 1.023 | 275 |
| 90 | 1.143 | 1.133 | 1.125 | 1.118 | 1.111 | 270 |
| 95 | 1.229 | 1.220 | 1.211 | 1.204 | 1.197 | 265 |
| 100 | 1.312 | 1.303 | 1.295 | 1.288 | 1.282 | 260 |
| 105 | 1.392 | 1.383 | 1.375 | 1.369 | 1.363 | 255 |
| 110 | 1.468 | 1.460 | 1.452 | 1.446 | 1.440 | 250 |
| 115 | 1.540 | 1.532 | 1.525 | 1.519 | 1.514 | 245 |
| 120 | 1.607 | 1.600 | 1.594 | 1.588 | 1.583 | 240 |
| 125 | - 1.669 | 1.663 | 1.657 | 1.652 | 1.648 | 235 |
| 130 | 1.727 | 1.721 | 1.716 | 1.712 | 1.708 | 230 |
| 135 | 1.779 | 1.774 | 1.770 | 1.766 | 1.763 | 225 |
| 140 | 1.825 | 1.821 | 1.818 | 1.815 | 1.812 | 220 |
| 145 | 1.866 | 1.863 | 1.860 | 1.858 | 1.856 | 215 |
| 150 | 1.902 | 1.899 | 1.897 | 1.895 | 1.894 | 210 |
| 155 | 1.932 | 1.930 | 1.928 | 1. 927 | 1.926 | 205 |
| 160 | 1.956 | 1.955 | 1.954 | 1.943 | 1.953 | 200 |
| 165 | 1.976 | 1.975 | 1.974 | 1.973 | 1. 973 | 195 |
| 170 | 1.989 | 1.989 | 1. 989 | 1. 988 | 1.988 | 190 |
| 175 | 1.997 | 1.997 | 1. 997 | 1. 997 | 1.997 | 185 |
| 180 | 2.000 | 2.000 | 2.000 | 2.000 | 2.000 | 180 |

With reference to Eq. (4-1), by expanding the radical

$$
\left(L^{2}-R^{2} \sin ^{2} \theta\right)^{3 / 2}
$$

by means of the binomial theorem and neglecting the unimportant terms, the piston travel may be written as

$$
\begin{equation*}
S=R\left(1-\cos \theta+1 / 2 Z \sin ^{2} \theta\right) \tag{4-6}
\end{equation*}
$$

The term $\left(1-\cos \theta+1 / 2 Z \sin ^{2} \theta\right)$ is called the piston-travel factor. Values of this factor for different crank angles may be calculated, but it is more convenient to use Table 4-3.

4-3. Example.-Determine the velocity and acceleration for the masterrod piston in Example 1, Table 2-1.

Procedure.-For this example, $N=2,000$ r.p.m., $R=5.375 / 2=2.6875 \mathrm{in}$. and $L / R=4$. Hence, from Eq. (4-4),

$$
V_{\text {f.p }} \quad: 0.00873 \times 2,000 \times 2.6875(\sin \theta+1 / 2 Z \sin 2 \theta)
$$

By using values of the piston-velocity factor as found in Table 4-1, the values of $V$ for increment crank angles are found (Table 4-4).

Table 4-4

| $\theta$ | $V_{\text {f.p.s. }}$ | $\theta$ | $V_{\text {f.p.s. }}$ | $\theta$ | $V_{\text {f.p.s. }}$ | $\theta$ | $V_{\text {f.s.... }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 0 | 100 | 44.3 | 190 | 6.15 | 280 | 48.3 |
| 10 | 10.17 | 110 | 40.4 | 200 | 12.3 | 290 | 48 |
| 20 | 19.85 | 120 | 35.6 | 210 | 18.4 | 300 | 45.75 |
| 30 | 28.6 | 130 | 30.2 | 220 | 24.4 | 310 | 41.7 |
| 40 | 36 | 140 | 24.4 | 230 | 30.2 | 320 | 36 |
| 50 | 41.7 | 15.0 | 18.4 | 240 | 35.6 | 330 | 28.6 |
| 60 | 45.75 | 160 | 12.3 | 250 | 40.4 | 340 | 19.85 |
| 70 | 48 | 170 | 6.15 | 260 | 44.3 | 350 | 10.17 |
| 80 | 48.3 | 180 | 0 | 270 | 47 | 360 | 0 |
| 90 | 47 |  |  |  |  |  |  |

The acceleration from Eq. (4-5) is

$$
A=0.000914 \times \overline{2,000}^{2} \times 2.6875(\cos \theta+Z \cos 2 \theta)
$$

By using values of the piston-acceleration factor, the values of $A$ for inerement crank angles are found (Table 4-5).

It is also of interest to determine the piston travel. By using Eq. (4-6) and proceeding as above, the values vs. crank angle are found (Table 4-6).

Table 4-5

| $\theta$ | A, ft. <br> per sec. ${ }^{2}$ | $\theta$ | $A, \mathrm{ft}$. <br> per sec. ${ }^{2}$ | $\theta$ | $A, \mathrm{ft}$. <br> per sec. ${ }^{2}$ | $\theta$ | $A, \mathrm{ft}$. <br> persec. ${ }^{2}$ |
| ---: | ---: | ---: | ---: | :---: | :---: | :---: | :---: |
| 0 | 12,280 | 100 | $-4,005$ | 190 | $-7,350$ | 280 | -599 |
| 10 | 12,000 | 110 | $-5,240$ | 200 | $-7,340$ | 290 | 1,482 |
| 20 | 11,110 | 120 | $-6,140$ | 210 | $-7,280$ | 300 | 3,680 |
| 30 | 9,730 | 130 | $-6,740$ | 220 | $-7,100$ | 310 | 5,875 |
| 40 | 7,950 | 140 | $-7,100$ | 230 | $-6,740$ | 320 | 7,950 |
| 50 | 5,875 | 150 | $-7,280$ | 240 | $-6,140$ | 330 | 9,730 |
| 60 | 3,680 | 160 | $-7,340$ | 250 | $-5,240$ | 340 | 11,110 |
| 70 | 1,482 | 170 | $-7,350$ | 260 | $-4,005$ | 350 | 12,000 |
| 80 | -599 | 180 | $-7,350$ | 270 | $-2,455$ | 360 | 12,280 |
| 90 | $-2,455$ |  |  |  |  |  |  |

Table 4-6

| $\theta$ | $S$, in. | $\theta$ | $S$, in. | $\theta$ | $S$, in. | $\theta$ | $S$, in. |
| :---: | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 0 | 0 | 100 | 3.48 | 190 | 5.35 | 280 | 2.55 |
| 10 | 0.0511 | 110 | 3.91 | 200 | 5.25 | 290 | 2.062 |
| 20 | 0.202 | 120 | 4.29 | 210 | 5.1 | 300 | 1.596 |
| 30 | 0.444 | 130 | 4.61 | 220 | 4.89 | 310 | 1.158 |
| 40 | 0.77 | 140 | 4.89 | 230 | 4.61 | 320 | 0.77 |
| 50 | 1.158 | 150 | 5.1 | 240 | 4.29 | 330 | 0.444 |
| 60 | 1.596 | 160 | 5.25 | 250 | 3.91 | 340 | 0.202 |
| 70 | 2.062 | 170 | 5.35 | 260 | 3.48 | 350 | 0.0511 |
| 80 | 2.55 | 180 | 5.375 | 270 | 3.025 | 360 | 0 |
| 90 | 3.02 |  |  |  |  |  |  |

Graphical representations of Tables 4-4, 4-5, and 4-6 are shown in Fig. 4-2.

4-4. Piston Displacement, Velocity, and Acceleration for . Articulated Rods.-When articulated rods are used as in the case of radial engines and in many V-engines, the path of the link-pin center is not a true circle, and the preceding formulas for displacement, velocity, and acceleration of the piston are somewhat in error. Formulas for the articulated system can be derived, but they are too complex for practical use, and a graphical analysis is preferable.

Since $V=d S / d t$, the velocity may be found by drawing tangents to the piston-travel curve at increment positions and measuring the slope. For instance, in Fig. 4-2 at 50 deg. the
piston travel is at the rate of 3.2 in . in 78 deg. of crank travel. At a speed of 2,000 r.p.m., the time in seconds corresponding to 78 deg. is $60 / 2,000 \times 78 / 360=0.0065$ sec., and the velocity is $3.2 /(0.0065 \times 12)=41 \mathrm{ft}$. per sec., which closely checks the value determined by calculation. Similarly, the acceleration at 50 deg. is $38 / 0.0065=5,850 \mathrm{ft}$. per sec. ${ }^{2}$ By taking a sufficient number of points, velocity and acceleration curves may be plotted.


Frg. 4-2.-Piston travel, velocity, and acceleration curves for Example 1.
Figure 4-3 illustrates a methorl of finding the path of the linkpin center. In this figure, which is based on the dimensions of a Curtiss Conqueror engine, $P_{M}$ is the master-rod pistom-pin center, $C_{M}$ is the crankpin center, $C_{L}$ is the link-pin conter ${ }^{2}$ located at 2.406 in . from $C_{M}$, and $P_{L}$ is the link-rorl piston-pin center.

Center-to-center length of master rod $=10 \mathrm{in}$. ('rnter-tocenter length of the link rod is 7.594 in. Obviously, angle $C_{L} C_{M} P_{M}$ is fixed by the design of the master roct.

Plotting the path of the link-pin center consists in locating $C_{M}$ at increment angles and finding the corresponding position of $C_{L}$. The link-rod piston positions are then found by setting
the compass to the link-rod length and striking ares intercepting the link-rod cylinder axis. The corresponding piston-travel


Fig. 4-3.-Graphical construction for finding the path of the link-pin center for a Curtiss V-1570 Conqueror engine.


Fig. 4-4.-Piston travel vs. crank angle for a Curtiss V-1570 Conqueror engine.
positions may be found by measuring the distances from the extreme position of the piston pin to these intercepts.

Figure 4-4 shows the piston travel of the master-rod and articulated-rod cylinders for the Curtiss V-1570 engine. As the
slope of the articulated-rod curve is nowhere very different from the slope of the master-rod curve, the velocity and acceleration curves will also be closely similar (Fig. 4-5). This fact justifies the usual simplifying procedure of assuming that the acceldration of the articulated-rod pistons may be taken as erqual to that of the master-rod pistons. It should be noted, howerer, that the farther the link-pin center is from the master-rod crater, the greater will be the discrepancy. It is also of importance tos note that increasing this distance increases the stroke of the


Frg. 4-5.-Piston displacement, velocity, and acecleration for the ('urtiss V-1570 Conqueror engine at 2,400 r.p.m. (From S.A.E. Journul, Vol. 2!, No. 4, April, 1931.)
articulated-rod piston with conseciuent results on comprewsion ratio, tendency to detonate, ete.

4-5. Inertia Forces Due to Reciprocating Parts.-. The forces necessary to accelerate the piston, rings, wrist pin, and the upper end of the connecting rod are directly proportional to the wright of these parts, and in consequence, it is clesirable to keep their weights to a minimum consistent with the other functions that they perform. When the aecelerations are known, the inertia forces may be calculated from

$$
\begin{equation*}
F=M A=\frac{W}{g} A \tag{1-7}
\end{equation*}
$$

where $F=$ inertia force, lb.
$M=$ mass of reciprocating parts.
$W=$ weight of reciprocating parts, lb.
$A=$ acceleration, ft. per sec. ${ }^{2}$

$$
g=32.2
$$

It is convenient, in calculating inertia forces, to combine Eqs. (4-5) and (4-7), thus

$$
\begin{equation*}
F_{R}=0.0000284 N^{2} W R(\cos \theta+Z \cos 2 \theta) \tag{4-8}
\end{equation*}
$$

where $F_{R}=$ inertia force of the reciprocating parts, lb .
$N=$ r.p.m.
$W=$ weight of reciprocating parts, lb.
$R=$ crank radius, in.
The term $(\cos \theta+Z \cos 2 \theta)$ is called the inertia factor. It is most conveniently found from Table 4-2.


Fig. 4-6.-Gas pressure, inertia, and resultant forces (in respect to direction).
(Method from Angle, "Engine Dynamics and C'rankshaft Design.")
In the analysis of an engine, the weight of the reciprocating parts must be known to determine the inertia forces. For a new unit, this involves practically a complete design of the reciprocating parts. But this is difficult without a knowledge of the stresses involved. Obviously, a preliminary weight estimate is necessary to determine the forces, and an intelligent estimate necessitates a reference to previous attainments. Figures A1-3 and A1-4 are of assistance in this respect.

4-6. Example.-Estimate the inertia foree due to reciprocating parts :at increment angles through 360 deg . for 1 cylinder of Example 1, Table 2-1.
Procedure.-By using the data of Example 1, and referring to Figs. A1-3 and A1-4, the probable weight of the reciprocating parts will be 0.25 Ib . per sq. in. of piston area, or a total of $0.25 \times 4.5^{2} \times 0.785=4 \mathrm{lh}$. per cylinder, approximately. This weight may be substituted in Ecq. (4-8), but inasmuch as the accelerations have already been found (Table 4-i), the foreres may be found from $F=\frac{4}{32.2} A$ for the various crank angles. Results of these calculations are shown in Table 4-7.


Fig. 4-7.-Resultant forces of gas pressure and inertia (in resperet to work). (Method from Angle, "Engine Dynamics and ('rankshaft Design.")

For combining with the gas-pressure forces, inertia forces may be plotted in either of two ways (Figs. 4-6 and 4-7).

4-7. Torque or Turning Effort per Cylinder.-The part of the force along the cylinder axis which does useful work is the rom-

TABLIE 4-7

| $\theta$ | $F$, lh. | $\theta$ | $F^{\prime}, \mathrm{lh}$. | $\theta$ | $F, \mathrm{lb}$. | $\theta$ | $F_{,}, \mathrm{lh}$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 1,525 | 100 | -498 | 190 | -912 | $2 \times 0$ | $-74,5$ |
| 10 | 1,491 | 110 | -650 | 200 | -911 | 290 | 184 |
| 20 | 1,381 | 120 | -761 | 210 | -905 | 300 | 457 |
| 30 | 1,210 | 130 | -836 | 220 | -881 | 310 | 730 |
| 40 | 988 | 140 | -881 | 230 | -836 | 320 | 988 |
| 50 | 730 | 150 | -905 | 240 | -761 | 330 | 1,210 |
| 60 | 457 | 160 | -911 | 250 | -650 | 340 | 1,381 |
| 70 | .184 | 170 | -912 | 260 | -498 | 350 | 1,491 |
| 80 | -74.5 | 180 | -912 | 270 | -325 | 360 | 1,525 |
| 90 | -325 |  |  |  |  |  |  |

ponent tending to rotate the crankshaft. This turning force may be expressed in terms of the force parallel to the cylinder axis. Referring to Fig. $4-8, P$ is the piston-pin center, $C$ is the crankpin center, and $M$ is the axis of the crankshaft.


Fig. 4-8.-Crank-chain diagram illustrating the method of determining the torque.

In the figure, the force parallel to the cylinder axis is $F_{C A}$ and the force in the connecting rod is $P B\left(=F_{C R}\right)$. From the diagram,
(1) $D E=C E \cos (\theta+\phi)=H$, the component tending to bend the crankshaft.
(2) $C D=C E \sin (\theta+\phi)=T$, the component tending to rotate the crankshaft.
(3) $C E=P B=\frac{F_{C A}}{\cos \phi}$.

Subsituting (3) in (1),

$$
H=F_{C A} \times \cos \phi(\theta+\phi)
$$

and substituting (3) in (2),

$$
T=\underset{\cos \phi}{F_{C A}} \times \sin (\theta+\phi)
$$

If $F_{C A}$ is in pounds and $R$ is in inches, the torque $Q$ is

$$
Q=T R=R \times F_{c A} \frac{\sin (\theta+\phi)}{\cos \phi} \text { in pound-inches }
$$

However, it is best to have the equation for $T$ in terms of $\theta$ only as $\phi$ is difficult to determine; hence

$$
T=F_{C A} \frac{\sin (\theta+\phi)}{\cos \phi}=F_{C A} \frac{\sin \theta \cos \phi+\cos \theta \sin \phi}{\cos \phi}
$$

but

$$
\cos \phi=\sqrt{1-\frac{R^{2}}{L^{2}} \sin ^{2} \theta}=\sqrt{1-Z^{2} \sin ^{2}}
$$

and

$$
\sin \phi=\frac{R}{L} \sin \theta=Z \sin \theta
$$

substituting

$$
T=F_{C A} \frac{\sin \theta \sqrt{1-Z^{2} \sin ^{2} \theta}+\cos \theta Z \sin \theta}{\sqrt{1-Z^{2} \sin ^{2} \theta}}
$$

$$
T=\dot{F}_{C A} \sin \theta\left(1+\frac{Z \cos \theta}{\left.\sqrt{1-Z^{2} \sin ^{2}} \theta\right)}\right.
$$



Fig. 4-9.-Single-cylinder torque curve for Example 1.
The expression $\left(Z^{2} \sin ^{2} \theta\right)$ is small and may be neglected without appreciable error. Then

$$
\begin{aligned}
T & =F^{\prime} \cos \sin \theta(1+Z \cos \theta) \\
& =F^{\prime} \cos (\sin \theta+Z \sin \theta \cos \theta)
\end{aligned}
$$

but $2 \sin \theta \cos \theta=\sin 2 \theta$
Therefore,

$$
\begin{equation*}
T=F_{C A}^{\prime}\left(\sin \theta+\frac{Z}{2} \sin 2 \theta\right) \tag{4-9}
\end{equation*}
$$

The term $[(\sin \theta+(Z / 2 \sin 2 \theta)]$ is called the tangrntial-force factor, and it is most conveniently found from Table 4-1.

The torque,

$$
\begin{equation*}
Q(\text { in lb. } \mathrm{ft} .)=T^{\prime}(\mathrm{in} \mathrm{lb} .) \times R(\mathrm{inft}) \tag{4-10}
\end{equation*}
$$

4-8. Example.-For the engine selected in Example 1, plot a curve of torque per cylinder against crank angle through one comaplete cycle.

Procedure.-Values of $F_{C A}$ ( $=$ the net or resultant force parallel to cylinder axis) are read from Fig. 4-6. The resultant turning effort and torque at increment crank angles obtained from Eqs. (4-9) and (4-10) are given in Table 4-8. The torque per cylinder is shown graphically in Fig. 4-9.

Table 4-8

| $\theta$ | $\begin{gathered} F \\ \text { (lb.) } \end{gathered}$ | $\begin{gathered} T \\ \text { (lb.) } \end{gathered}$ | $\underset{(\mathrm{lb} .-\mathrm{ft}:)}{Q}$ | $\theta$ | $\begin{gathered} F^{\prime} \\ (\mathrm{lb} .) \end{gathered}$ | $\begin{gathered} T \\ (\mathrm{lb} .) \end{gathered}$ | $\begin{gathered} Q \\ (\mathrm{lb} .-\mathrm{ft} .) \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 620 | 0 | 0 | 370 | -1,488 | -321 | $-71.9$ |
| 10 | 4,309 | 930 | 208 | 380 | -1,354 | $-571$ | -128.0 |
| 20 | 5,220 | 2,200 | 493 | 390 | $-1,183$ | $-720$ | -161 |
| 30 | 5,230 | 3,180 | 712 | 400 | -961 | $-736$ | -165 |
| 40 | 4,172 | 3,200 | 716 | 410 | -703 | -625 | -140 |
| 50 | 3,360 | 2,980 | 667 | 420 | $-430$ | -419 | -93.8 |
| 60 | 2,768 | 2,690 | 603 | 430 | $-157$ | -160 | $-35.8$ |
| 70 | 2,436 | 2,480 | 555 | 440 | 48 | 49.4 | 11 |
| 80 | 2,255 | 2,320 | 520 | 450 | 352 | 352 | 78.9 |
| 90 | 2,155 | 2,155 | 482 | 460 | 471 | 444 | 99.5 |
| 100 | 2,038 | 1,920 | 430 | 470 | 677 | 582 | 130 |
| 110 | 2,000 | 1,720 | 385 | 480 | 734 | 556 | 124.5 |
| 120 | 1,980 | 1,500 | 336 | 490 | 809 | 520 | 116.5 |
| 130 | 1,956 | 1,258 | 284 | 500 | 834 | 434 | 97.1 |
| 140 | 1,880 | 978 | 219 | 510 | 878 | 344 | 77.0 |
| 150 | 1,747 | 684 | 153 | 520 | 884 | 232 | 52.0 |
| 160 | 1,610 | 422 | 94.5 | 530 | 885 | 116 | 26.0 |
| 170 | 1,468 | 192 | 43.0 | 540 | 888 | 0 | 0 |
| 180 | 1,230 | 0 | 0 | 550 | $-893$ | $-117$ | $-26.2$ |
| 190 | -1,119 | -146 | $-32.7$ | 560 | -897 | $-235$ | $-52.6$ |
| 200 | -990 | -259 | $-58.0$ | 570 | -894 | -350 | $-78.4$ |
| 210 | -953 | $-374$ | $-88.7$ | 580 | -884 | -460 | -103.0 |
| 220 | -902 | $-469$ | $-105$ | 590 | -841 | $-541$ | $-121.0$ |
| 230 | -857 | -558 | -125 | 600 | -808 | -613 | $-137$ |
| 240 | -782 | $-593$ | -133 | 610 | -730 | -627 | $-140$ |
| 250 | -677 | -582 | $-130$ | 620 | -620 | $-584$ | $-131$ |
| 260 | -519 | -489 | -109.5 | 630 | -468 | -468 | -105 |
| 270 | -352 | -352 | $-78.8$ | 640 | -297 | -305 | -68.3 |
| 280 | -95 | -97.6 | $-21.9$ | 650 | -118 | -120.4 | $-27.0$ |
| 290 | 163 | 166 | 37.2 | 660 | 75 | 73 | 16.3 |
| 300 | 436 | 424 | 95.0 | 670. | 205 | 182 | 40.8 |
| 310 | 709 | 630 | 141.0 | 680 | 207 | 159 | 35.6 |
| 320 | 967 | 740 | 166.0 | 690 | 178 | 108.4 | 24.3 |
| 330 | 1,189 | 722 | 162.0 | 700 | $-50$ | $-21.1$ | $-4.72$ |
| 340 | 1,360 | 574 | 128.5 | 710 | $-430$ | $-93$ | $-20.8$ |
| 350 | 1,470 | 318 | 71.2 | 720 | -620 | 0 | 0 |
| 360 | 1,504 | 0 | 0 |  |  |  |  |

4-9. Torque Reaction.-The reaction to the torque force is the piston side thrust. Referring to Fig. 4-8, the side thrust is represented by the force vector $F_{S T}$ and from the diagram $F_{S T}=F_{C A} \tan \phi$, but

$$
\tan \phi=\frac{\sin \phi}{\cos \phi} \quad \frac{R / L \sin \theta}{\sqrt{1-\left(R^{2} / L^{2}\right) \sin ^{2} \theta}}-\frac{\sin \theta}{\sqrt{(L / R)^{2}-\sin ^{2} \theta}}
$$

hence

$$
\begin{equation*}
F_{S T}=\frac{F_{C A} \sin \theta}{\sqrt{(L / R)^{2}-\sin ^{2} \theta}} \tag{4-11}
\end{equation*}
$$

It should be noted that the shorter the connecting-rod length


Fig. 4-10.-Variation of piston side thrust for a typical aircraft engine. (From Angle, "Engine Dynamics and Crankshaft Design.") $L$ in proportion to the crank radius $R$, the less the overall dimensions of the engine but the greater the side-thrust, component and hence the relative friction and wear in the cylinder.

An example of variation of piston side thrust with crank angle is shown in Fig. 4-10.

4-10. Total Engine Torque. For the purposes of design, it, may be assumed that the torque curves for all cylinders will be the same. Hence, to determine the total turning effort,


Fig. 4-11.-Usual crank-arm arrangement for four cylinder in-line engines.

Cylinder Numbers

|  | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| ¢ 180 | P | $C^{\prime}$ | $E$ | $I$ |
|  | $E$ | P | I | ( |
| 总 360U゙540 |  |  |  |  |
|  | I | $E$ | $C^{\prime}$ | P |
|  |  |  |  |  |
|  | $C$ | I | P | E |

Fig. 4-12. - Diagram for determining firing orders in conventional four-rylinder inline engimes.
of the engine, it is merely necessary to space the individual cylinder curves properly with respect to crank angle and add the
ordinates. To determine the angular spacing, it is necessary to know the arrangement of the crankshaft crank arms and the firing order in the cylinders.


Frg. 4-13.-Usual crank-arm arrangement for six-cylinder in-line engines.


Fici. 4-14.- I iagram for determining firing orders in conventional six-cylinder in-line engines.
For four-cylinder in-line engines, the usual method of arranging the crank arms is shown in Fig. 4-11. The firing order may
be found from a diagram such as Fig. 4-12. In this figure, the firing order is 1-2-4-3. The other possible firing order for four-cylinder in-line engines having the conventional crank arrangement shown in Fig. 4-11 is 1-3-4-2.

The usual crank arrangement for six-cylinder in-line engines is illustrated in Fig. 4-13.

A method of determining the firing order for six-cylinder engines is illustrated in Fig. 4-14. In this figure, the firing order is 1-5-4-6-2-3. Other firing orders are 1-2-3-6-5-4, 1-2-4-6-5-3, and 1-5-3-6-2-4. The firing order 1-5-3-6-2-4 is usually considered best as no two adjacent cylinders fire in succession.

The firing order for conventional single-bank radial engines is 1-3-5-7-9-2-4-6-8 for nine-cylinder engines, and the same procedure applies for a lesser number of cylinclers. The reason for using an odd number of cylinders is obvious.

American airplane engines are usually designed to rotate clockwise when viewed from the end opposite the propeller. Customary methods of numbering the cylinders are:

1. For in-line engines:

2. For V-engines:


However, numbering of cylinders is largely arbitrary, and many engines differ from the preceding method of numbering.
3. For single-bank radial engines, the cylinders are numbered in the direction of rotation.

4-11. Example.-Determine the firing order, and plot a rurve of total engine torque for Example 1, Table 2-1.

Procedure.-In a five-cylinder single-hank radial, the firing order will necessarily be 1-3-5-2-4. The angular spacing of the colinder centor lines is $36 \%=72$ deg. In spacing the individual torque rurves with No. 1 cylinder starting expansion at 0 deg., No. 3 will start at 14.4 deg., No. $\overline{3}$ will
start at 288 deg., No. 2 will start at 432 deg., and No. 4 will start at 576 deg.
Individual torque curves for the five cylinders and the curve of resultant torque for the engine are shown in Fig. 4-15.

The mean torque is found by taking the area under the resultant engine torque curve and dividing by the length. The mean-torque line is located at a height above the zero line equal to the quotient.


Fig. 4-15.--Torque variation per cycle for Example 1. Ratio of max $Q /$ mean $Q=2.14$.

A check on the work is possible at this stage, for the mean value of torque as found is the indicated torque of the engine; hence

$$
\text { i.hp. }=\frac{2 \pi N Q}{33,000}=\frac{2 \pi \times 2,000 \times 410}{33,000}=156
$$

For the assumed mechanical efficiency of 85 per cent (Par. 3-3) the brake horsepower is

$$
\text { b.hp. } \max ^{\max }=156 \times 0.85=133
$$

The originally assumed brake horsepower was based on a cylinder displacement of 82.5 cu . in. (Par. 2-4), but the torque was based on a cylinder displatement of $4.5^{2} \times 0.785 \times 5.375=85.5 \mathrm{cu}$. in. Hence the horsepower hased on the original displacement will be about $(82.5 / 85.5) \times 133=128$. This is within less than 2.5 per cent of the originally assumed value of 125 b.hp., and therefore indicates that no serious errors have been made in the calculations.

4-12. Torque Variation with Number of Cylinders and Cylinder Arrangement.-In a one-cylinder engine, the torque is negative, i.e., against rotation, for a large portion of the cyrle. Hence to keep the engine turning, it is necessary to use a relatively heavy flywheel. This is obviously not practical for airplane engines, and, although the propeller arts to a considerable extent as a flywheel, because of its mass, it is desirable to use several cylinders to reduce the torque variation as well as increase the total power output. Figure $4-16$ shows the effect of number of cylinders and arrangement on torque variation and ratio of maximum to mean torque.


Fig. 4-16.-Wffect of number of cylinders and arrangement on forque variatim. (From Angle, "Engine Dynamics and ('rankshaft Design."),

## Suggested Design Procedure

Important. Make all constructions and curves to a large (rnough seal. to permit accurate readings of values. Size 13 or larger drawing paper is recommended. Keep a record of the man-hours required on wath item.

1. For the engine selected for your design, construct rurvers of piston travel, velocity, and aceeleration through 360 deg. of rankshaft travel for one eylinder).
2. Estimate the weight of reciprocating parts, and construct a curve of reciprocating inertia force vis. crank angle through 720 derg. of aramh-hatit travel).
3. Superimpose the gas-force curve (see Suggested Design Procedure, page 35 ; item 4) on the reciprocating inertia-force-curve (see item 2 above) coordinates, and plot a curve of resultant force parallel to the cylinder axis.
4. Construct a single-cylinder torque curve (through 720 deg . of crankshaft travel), and draw a line on the diagram representing the mean torque. Determine the ratio of maximum to mean torque, and place the value found on the diagram.
5. Construct a curve of piston side thrust vs. crank angle (through 720 deg . of crankshaft travel).
6. Determine the firing order to be used, plot a curve of total engine torque vs. crank angle (through 720 deg. of crankshaft travel), and draw a line on the diagram representing the mean engine torque. Determine the ratio of maximum to mean torque, and place the value found on the diagram.
7. By using the mean engine torque value found in item 6 , determine the indicated horsepower and brake horsepower for your engine. If the brake horsepower thus determined does not agree within 5 per cent of the originally assumed value of brake horsepower (Suggested Design Procedure, page 24, item 2), recheck the work for errors.
8. When items 1 to 7 have been completed and put in proper form, submit for checking and approval.

## References

1. Angle: "Engine Dynamics and Crankshaft Design."
2. Huebotter: "Mechanics of the Gasoline Engine."
3. Cousins: "Analytical Design of High Speed Internal Combustion Engines."

## CHAPTER 5

## ANALYSIS OF BEARING LOADS

5-1. Crankshaft-bearing Loads.-Before the necessary sizes of the various crankshaft bearings can be determined, it is essential to know the loads to which they will be suhjected, and before all these loads can be determined, it is necessary to know approximately the dimensions, i.e., the mass of the moving parts. Obviously, this knowledge necessitates the making of assumptions based on the past experience of the designer or, in the


Fig. 5-1.-Method of determining the resultant force on the crankin for an engine having one cylinder per crankpin.
case of students, of other designers. Only by utilizing the results: of previous successful experience can an exhorbitant amomint, of trial-and-error effort be avoided:

5-2. Resultant Force on the Crankpin.-The resultant forme on the crankpin may be found most readily by rombining graphically the resultant foress along the connecting-rod axes with the centrifugal forces due to the weight of the lower and of the connecting rod.
Referring to Fig. 5-1, $F_{c A}$ is the resultant forre along the cylinder axis and $F_{C}$ is the centrifugal force due to the rotating weight of the connecting rod.
The acceleration toward the axis of a rotating hody neressary to keep the body moving in a circle is $v^{2} / r$; hence the centrifugal force on the body is

$$
F_{C}=M A=M \frac{v^{2}}{r}=\begin{gathered}
W_{C v^{2}} \\
g r
\end{gathered}
$$

where $F_{C}=$ centrifugal force, lb .
$M=$ mass.
$A=$ acceleration.
$v=$ linear velocity, ft. per sec.
$r=$ radius (crank arm), ft.
$W_{C}=$ centrifugal weight, lb . (= the rotating weight on the crankpin for the case under consideration).
$g=$ acceleration of gravity ( $=32.2 \mathrm{ft}$. per $. \mathrm{sec} .^{2}$ ).
But

$$
v=2 \pi r n=\frac{2 \pi R N}{12 \times 60}
$$

where $n=$ r.p.s.

$$
N=\text { r.p.m. }
$$

$R=$ crank arm, in.
Hence, by combining and reducing

$$
\begin{equation*}
F_{C}=0.0000284 W_{C} N^{2} R \tag{5-1}
\end{equation*}
$$

The centrifugal force is laid off to scale along the crank arm from the crankshaft axis $M . F_{C R}$ is the component of $F_{C A}$ along the connecting rod axis. From the diagram,

$$
F_{C R}=\begin{gathered}
F_{C A} \\
\cos \phi
\end{gathered}
$$

but from Par. 4-2,

$$
\cos \phi=\sqrt{1-\left(\frac{R}{L}\right)^{2} \sin ^{2} \theta}
$$

Therefore

$$
\begin{equation*}
F_{C R}=\frac{F_{C_{A}}}{\left[1-(R / L)^{2} \sin ^{2} \theta\right]^{1 / 3}} \tag{5-2}
\end{equation*}
$$

Vector $F_{C R}$ is laid off from the end of vector $F_{c}$ and parallel to the axis of the connecting rod. The resultant $F_{R}$ closes the force triangle.

Angle $\alpha$ represents the direction of the resultant force with respect to the cylinder axis, $\beta$ with respect to the crank arm, and $\gamma$ with respect to the connecting rod. Resultant forces on the crankpin are usually plotted as polar diagrams. Figure 5-2a
shows polar diagrams for ( $A$ ) an automotive engine and ( $B$ ) an aircraft engine each plotted with respect to the erlinder axis. Figure 5-2b shows the data of Fig. 5-2a (diagram $B$ ) plotted with respect to the crank-arm axis. The effect of engine sipeed and


Fis. 5-2 (a).-Polar diagrams of resultant forces on in-line engine crankenins with respect to the eylinder center lines. (A) Small-hore high-speral antomotiver engine with relatively heavy piston. (13) Larger-bore aireraft engine with relatively lightweight piston.
of relative magnitude of gas pressure and reciprocating inertia forces is readily apparent.

When more than one connecting rod is attached to a given
 shows the method of finding the resultant forere on the reankpin for a V-type engine. Figure 5-4 shows polar diagrame with
respect to (a) the engine axis, (b) the crank arm, and (c) the left connecting rod for the engine in Fig. 5-3.

When many connecting rods are attached to one crankpin through link pins, the determination of crankpin bearing loads


Fig. 5-2(b).-Polar diagram of resultant forces on an in-line engine crankpin with respect to the crank arm. This diagram corresponds to ( $B$ ) in Fig. 5-2 (a). The diagram is most easily constructed by assuming that the crank arm remains fixed and the cylinders rotate backward at increment angles.
may be simplified somewhat by assuming that the forces in the articulated rods pass through the center of the crankpin. This assumption is not strictly correct, but it gives results sufficiently accurate for preliminary design purposes.


Frg. 5-3.-Method of finding the resultant force on the crankpin of a V-type engine. (From Angle, "Engine Dynamics and Crankshaft Design.'')


Frg. 5-4.(a) Polar diagram of resultant foree on "゙-typr angine erankpin with respect to the engine axis. (From Anule, "Eugitu I)llnamics and ('rankeshaft I)e:sion.'")


420
Fig. 5-4 (b).-Polar diagram of resultant force on V-type engine crankpin with respect to crank arm. (From Angle, "Engine Dynamics and Crankshaft Design.')


Fici. 5-4(c).--Polar diamram of rexultamt fore on V-type angine wankpin with respect toleft commedingrod. Ifrom Anfle "E'ngina: Dynamics and (ranlistuift Design.")

5-3. Example.-Construct a polar diagram of crankpin bearing loads for the engine selected in Example 1, Table 2-1.

Procedure.-From Fig. A1-5, the probable rotating weight per crankpin for a $125-\mathrm{hp}$. engine of five cylinders will be about 10 lb . For a speed of $2,000 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and a crank radius of 2.6875 in., the centrifugal force will be [from Eq. (5-1)]

$$
F_{C}=0.0000284 \times 10 \times \overline{2,000}^{2} \times 2.6875=3,050 \mathrm{lb} .
$$

The component of force along the connecting-rod axis $F_{C R}$, varies with the value of $F_{C A}$ and $\theta$. Table 5-1 shows, for the example, values of $F_{C R}$ at increment angles. It is to be seen from this table that values of $F_{C R}$ do not differ greatly from values of $F_{C A}$. For many purposes, these differences are small enough to be neglected, and values of $F_{C A}$ may be used directly in plotting the polar diagram.

Table 5-1

$$
10 \quad \stackrel{11}{(=7)}
$$

$F_{C A} \quad \sin ^{2} \theta \quad$ ت

| 0 | 800 |  | 0 |  | 1.0 | 1.0 | 800\| |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 20 | 5,300 | 0. 342 | 0.117 | 0.0072 | 0.9928 | 0.996 | 5,320 | 380 | -1,400 | 0.996 | -1,405 |
| 40 | 4,000 | 0.6428 | 0.413 | \|0.0254 | 9746 | 0.987 | 4,050 | 400 | -1,000 | 0.987 | -1,013 |
| 60 | 2,650 | 0. 866 | 0.751 | 0.0462 | 0.9538 | 0.977\| | 2,710 | 420 | -450 | 0.977 | 461 |
| 80 | 2,200 | 0.9848 | 0.969 | 0.0591 | . 9409 | 0.971 | 2,265 | 440 | 50 | 0.971 | 51. |
| 100 | 2,050 | 09848 | 0.969 | 0.0591 | . 9409 | 0.971 | 2,110 | 460 | 450 | 0.97 | 464 |
| 120 | 2,000 | 0.866 | 0.751 | 0.0462 | 9538 | \|0.977 | 2,045 | 480 | 750 | 0. | 768 |
| 140 | 1,800 | 0. 6428 | 0.413 | 0.0254 | 9746 | 0.987 | 1,825 | 500 | 00 | 0.98 | 811 |
| 160 | 1,600 | 0. 342 | 0.117 | 0.0072 | 0.9928 | 0.996 | 1,607 | 520 | 825 | 0.99 | 828 |
| 180 | 1,200 | 0 | 0 | 0 | 1.0 | 1.0 | 1,200 | 540 | 850 | 1.0 | 850 |
| 200 | 1,050 | 0. 342 | 0.117 | 0.0072 | 0.9928 | \|0.996 | 1,054 | 560 | 850 | 0.996 | 54 |
| 220 | 900 | 0. 6428 | 0.413 | 0.0254 | 0.9746 | 0.987 | 912 | 580 | 850 | 0.987 | 861 |
| 240 | 800 | 0. 866 | 0.751 | 0.0462 | 0.9538 | 0.977 | 819 | 600\| | 825 | 0.977 | 5 |
| 260 | 600 | 0.9848 | 0.969 | 0.0591 | . 9409 | 0.971 | 617 | 620 | 650 | 0.971 | 670 |
| 280 | 200 | 0. 9848 | 0.969 | 0.0591 | 9409 | 0.971 | 206 | 640 | 300 | 0.971 | 309 |
| 300 | -350 | 0866 | 0.751 | 0.0462 | 0.9538 | 0.977 | -358 | 660 | 75 | 0.977 | -77 |
| 32 | -850 | 06428 | 0.413 | 0.0254 | 0.9746 | 0.987 | -862\| | 680 | -200 | 0.987 | -202 |
| 340 | -1,300 | 0342 | 0.117 | 0.0072 | . 9928 | \|0.996| | -1,305 | 700 |  | 0.996 | 52 |
| 360 | -1,500 |  | 0 | $\bigcirc$ | . 0 | 1.0 | -1,500 | 0 |  | 1 | 800 |

For example, five connecting rods are attached to the crankpin, and although the variation of resultant foree ( $l_{C A}^{\prime}$ ) per eycle (Fig. 4-6) is assumed to be the same in each cylinder, for any given angular position of the crank arm, the force along each individual connecting rod will be different owing
to the fact that the various eylinders are operating on different parts of the cycle. Further, some of the connecting rods will be under compression and others will be under tension. An effort to combine graphially these forces is likely to result in some confusion if a system of kerping things straight is not used. Figure 5-5 shows a system that has heen prepared for the example, and a similar figure may casily be aranged for any other congine.

In this figure, the force in the connecting rod $F_{C R}$ is plot ted agnamst rank angle. Forces downward along the cylinder axis are taken as prsitive; upward forces are considered negative. The angular spacing of the evlinder axes is $360 \%=72$ deg.; hence with No. 1 eylinder just starting $\cdot x$ mansion,

 (enter line) for any cylinder of Example 1 at any position of the ramk arm with respect to the center line of No. 1 eylinder.

No. 3 (the next to fire) will be on the first part, of the compreseinn whent. Number 3 is 144 deg. ahead of No. 1 ; hencests angular ponition for Nin. 1 at
 Call this 36-deg. point 0 for No. 3 evlinder, and lay off the rank-angle scale as indicated. Similarly, the 0 point may be found for the of her revinders and scales laid off as shown.

To illustrate the use of the scale, suppose No. 1 (.ylimber is :t the sol-dig. point and it is desired to find the foreres in carh of the comnering rests. The solution consists in reading up to the curve from the siothere penint for atoh eylinder and taking the forees direetly from the ordinate soale.
 $M$ at their proper angular relation. Then, with $M$ thererank-haft aste an a center, the crank circle (radius $R$ ) and the contrifugal-form Fe (irele.
are constructed to the dimension and force scales, respectively. These circles are divided into the desired angular segments ( 20 deg . in this instance).

To determine the resultant force on the crankpin at any given angular position of the crank arm, say 100 deg. in the direction of rotation past the beginning of expansion in No. 1 cylinder, the procedure is as follows. (a) Set the compass to the length of the master connecting rod (dimension scale), and with $C$ (the 100-deg. position on the crank circle) as a center,


Fig. 5-6.-Polar diagram of resultant force on a five-cylinder radial-engine crankpin (Example 1).
strike arcs intercepting all the cylinder center lines (designated $P_{1}, P_{2}, P_{3}$, etc., in Fig. 5-6). Lines connecting these intercepts with $C$ represent the center lines of the various connecting rods. (b) For a crank angle of 100 deg ., read the values of $F_{C R}$ for the various cylinders from Fig. 5-5. (c) With the $100-\mathrm{deg}$. intercept on the $F_{C}$ circle as a starting point, lay off force vector $F_{C R_{1}}$ parallel to No. 1 cylinder connecting rod $P_{1} C$ and in the direction*consistent with Fig. 5-5. From the end of $F_{C R 1}$, lay off $F_{C R 2}$ parallel to $P_{2} C$ and in the proper direction. Continue this procedure until all connecting-rod forces are laid off. The resultant force on the crankpin is represented by a
vector connecting the erankshaft center (A) and the culd of the last con-necting-rod vector. The direction of this resultant with resperet to the center line of cylinder No. 1 is $\alpha$ and with respect to the crank arm is $\beta$.

By connecting the ends of resultant force vectors determined at increment crank angles through 720 deg ., the polar diagram (Fig. 5-6) was obtained. When constructed to a large enough seale to permit close accuracy, polar diagrams for radial-engine crankpins are symmetrical.

It should be noted that the maximum foree from the diagram is considerably greater than the maximum value of $F_{c, c}$ (Fig. $5-5$ ).


- 800 Thertia
-1600 force, $F_{1}$

 Cyl. No. $3 \quad 160200240 \quad 280320360400440480520560600640680 \quad 0 \quad 40 \quad 80 \quad 120$ Cyl. No. $4 \quad 600640680 \quad 0 \quad 40 \quad 80 \quad 120160200240280320360400440480520560$ Cyl. No. $5 \quad 320360400440480520560600640680$ o $4080 \quad 120 \quad 160200240280$ Crank angle, deg.
Fig. 5-7.-Method for determining $F_{I}$ (the incortia force along the rylinder axis $\approx$ the inertia component in the romnecting rod) and $F_{\text {; }}$ (the gats forere along the cylinder axis $\approx$ the gas force in the connecting rod) for any (evinular of Example 1 at any position of the crank arm with respect to the rentre line of No. 1 cylinder.

Alternate Procedure.-Construction of polar diagrams for ramkpints of multicylinder radial engines is at best somewhat tedious, but some simplification of the foregoing procedure may be made by ronsidering the reeiprocating inertia, gas, and centrifugal inertia forees separately.

It has already been observed that the foree on the arankpin dus to the weight of the rotating part of the commeting rock is constant (for any given engine speed) and that it always acts along the crank-arm rentrer line. Hy reproducing Fig. 4-6 in Fig. 5-7 and locating the positions of all the celinders by the same method used for Fig. 5-5, the resultant forers $F_{i f i}$, due to gatspressure forces, and the resultant forces $F_{1 R}$, due to inertia of the reripro-
cating parts, may be found separately. Figure $5-8$ shows the method of determining the $F_{I R}$ forces. The procedure in making this construction is the same as that for Fig. 5-6 except that inertia forces along the cylinder axes are used (obtained from Fig. 5-7) instead of the total force, i.e., gas force + inertia force. It is seen from Fig. 5-8 that the resultant force on the crankpin due to the inertia of reciprocating parts ( $F_{I R}$ ) is a constant*


Fig. 5-8.-Construction showing that for radial engines the resultant of the reciprocating inertia forces is constant in magnitude (for a given engine speed) and that it always acts along the crank-arm center line. (Values apply only to Example 1.)
(for a given engine speed) and that it always acts parallel to the crank arm. Hence the construction need include only one determination of $F_{I R}$ to obtain the force due to incrtia of reciprocating parts for any angular position of the crank arm. In Fig. 5-8, the forces due to reciprocating inertia are added graphically to $F_{C}$, i.e., construction is started from the end of the $F_{C}$ vector. Hence the end of the $F_{I R}$ vector is distant from $M$ an amount equal to the total inertia force $F_{I T}$.

* Except for three-cylinder radials.

The resultant force on the crankpin clue to gas-pressure fores is found hy the construction shown in Fig. 5-9. In this figure, the gas forme in the various eylinders at any erank position are obtained from Fig. i-7 and summed vectorially in the same way as for Figs. 5-6 and 5-8. 'Thr gasforce vectors are started from the end of the total inertia-foree vertor $F_{I}$; hence a line connecting $M$ and the end of the $F_{\text {(iN }}$ (resultant gas foreer verofor will give the magnitude and direction of the total resultant forer $F$ wh the


Fig. 5-9.-Altornate mothod of constructing a polar diagram of restitant foreme on a five-tylinder radial-engine erankpin (Example 11 .
crankpin. Determination of $F_{a}$ by the procedures illustrated in Fig- a-s
 for only one crank-arm position, and heeanse the gas foreres during most of the exhaust, intake, and the first part of the compression stroks are waghible. This last reduces the number of vectors to bersmmmed in finding $F_{i}, \ldots$.

If carried through 720 deg. of increment-angle construction, Fig. S-9 would give the same polar diagram as was ohtained in Fig. E-fi. Howrorer, for obtaining the usual information desired, i.e., the maximmm amb m:an forces on the crankpin, this procedure is unneressary ats the erele is repe:ated $n / 2$ times during each revolution, $n$ being the number of eylinders. For ther
five-cylinder engine in Example 1, construction at increment angles through $360 / 2.5=144$ deg. is all that is necessary to determine the maximum and mean resultant forces on the crankpin. However, for beginners in polardiagram construction, it is advisable to carry the construction through at least twice this number of degrees of crank travel [i.e., $360 /(n / 4)$ ] to provide more of a check on the work and to understand more completely the details of construction. Polar diagrams of forces on crankpins are frequently constructed with respect to the crank-arm axis (Fig. 5-4b). For radial engines, the construction is illustrated in Fig. 5-10. In this construction, the total inertia-force vector $F_{I T}$ is laid off to scale as indicated in Fig. 5-10, the starting point being considered as the crankpin center $C$ (corresponding to $M$ in Fig. 5-9). From the end of the $F_{I T}$ vector, resultant gas force vectors $F_{G R}$ (determined by the construction illustrated in Fig. 5-9) are laid off at angles $\delta$ to the $F_{I T}$ vector ( $\delta$ also equals the angle of the gas-force resultant


Fic. 5-10.-Polar diagram of the resulting force on a five-cylinder radialengine crankpin with respect to the crank-arm axis (Example 1).
to the crank-arm center line) for increment crank angles through at least $360 /(n / 2)$ deg. By connecting the ends of the $F_{G R}$ vector at the various rrank angles, a polar diagram of gas forces with respect to the crank-arm center line is obtained. A line connecting the crankpin center $C$ and the end of the $F_{G R}$ vector at any of the given crank angles designated on the polar diagram gives the magnitude and direction $(\beta)$ with respect to the crank-arm axis of the resultant force $F_{R}$ on the crankpin at that crank angle. As the $F_{i R}$ vector will retrace the polar diagram loop $n / 2$ times per revolution, values and directions of $F_{R}$ will also repeat $n / 2$ times per revolution. Hence, one loop is sufficient for determining the maximum and mean forces on the crankpin.

The forees due to reciprocating and rotating weights, $F_{1 R}$ and $F_{C}$, vary as the square of the engine speed [Fqs. (4-8) and (5-1)]. Hence, the effect of cngine speed on crankpin loadings may readily be found from Fig. 5-10. For instance, the maximum force $F_{R}$ on the crankpin is $6,500 \mathrm{lb}$. for an engine speed of 2,000 r.p.m., and it is desired to know the maximum force at $2,400 \mathrm{r} . \mathrm{p} . \mathrm{m}$. Assuming that the gas forces remain the same,

$$
F_{R}(2,400 \text { r.p.m. })=6,500 \frac{\overline{2,400}^{2}}{\overline{2,000}^{2}}=9,300 \mathrm{lb} . \text { (approximately) * }
$$

From this, it is apparent that very high crankpin loadings are likely to occur in power dives, and even in closed-throttle dives when the gas-foree vector is negligible, the inertia load $F_{I T}$ will rise to high values. Loration of engine r.p.m. points along the crank-arm axis (Fig. 5-10) adds materially to the information conveyed by the diagram.

5-4. Crankpin Bearing Loads.-The unit loadings on bearings are based upon the force per square inch of projected bearing area, i.e., the diameter of the crankpin (or journal) times its length. Numerous factors affect the allowable loadings such as distortion of the journal or connecting rod, condition of the lubricant, relative characteristics of the journal and hearing metal, and rubbing velocity. On the assumption of sufficient rigidity to the shaft and adequate lubrication, usual mean bearing pressures range from 750 to $2,000 \mathrm{lb}$. per sci. in. or more of projected area, and maximum pressures range up to $5,000 \mathrm{ll}$. per sq. in. (Tables A1-5 and A1-8). $\dagger$

Rubbing velocity is the relative speed with which a point on the crankpin or journal moves by a point on the inner surface of the bearing. It may be calculated as follows:

$$
\begin{equation*}
V=\frac{\pi D}{12} \times \frac{N}{60} \tag{5-3}
\end{equation*}
$$

where $V=$ rubbing velocity, f.p.s.
$D=$ crankpin or journal diameter, in.
$N=$ engine speed, r.p.m.
Rubbing velocities (Table A1-5) range from 15 to 25 or more feet per second, but in more recent high-powered engines, 30 to 50 or more feet per second is proving quite satisfactory.

Rubbing factor, or PV factor as it is sometimes callerd, is the product of mean bearing load in pounds per sequare inch of projected bearing area and rubbing velocity in fect per seeond. $P V$ factors are usually considered to be an indication of bearing capacity. Values range up to 50,000 or more with 20,000 to

[^4]35,000 (depending on the size of the engine) being a limit recommended by some authorities. Actually, many details of design contribute in determining allowable values.

The ratio of rubbing velocity to unit bearing load is sometimes used as a still further criterion in determining allowable bearing loads. Lubrication engineers frequently express the conditions in a bearing by the relation ${ }^{7} Z N / P$ where $Z$ is the absolute viscosity ${ }^{6}$ of the lubricant in centipoises, $N$ is the speed of the journal in revolutions per minute, and $P$ is the bearing load in pounds per square inch of projected area. . Since $V$ is a function of $N$ [Eq. (5-3)], some engineers consider $V / P$ as a better expression of bearing conditions than $P V$. Meyer ${ }^{8}$ recommends using a value of $V / P>0.016$.

5-5. Example.-For the engine selected in Example 1, determine the projected crankpin area, diameter, and length if the allowable maximum bearing load is not to exceed $1,200 \mathrm{lb}$. per sq. in. of projected area, the $P V$ factor (based on mean loads) is not to exceed $20,000, V / P>0.016$, the rubbing velocity is not to exceed 20 f.p.s., and the ratio of length to diameter of the crankpin is to fall within the usual range for radial engines of 1.2 to 1.6 (Table A1-5).

Solution.-From Par. 5-3, the maximum force on the crankpin was found to be $6,500 \mathrm{lb}$. and the mean force was $5,245 \mathrm{lb}$. The smallest permissible projected crankpin area is $6,500 / 1,200=5.4$ sq. in., and the corresponding mean pressure is $5245 / 5.4=970 \mathrm{lb}$. per sq.in. For the allowable rubbing velocity of 20 f.p.s., $P V=970 \times 20=19,400<20,000$, the allowable rubbing factor, and $V / P=20970=0.0206>0.016$. From Eq. (5-3),

$$
\begin{aligned}
D & =\frac{720 \mathrm{~V}}{\pi N}=\frac{720 \times 20}{\pi \times 2,000}=2.3 \mathrm{in.} \\
L & =\frac{A}{D}=\frac{5.4}{2.3}=2.35 \mathrm{in}
\end{aligned}
$$

and

$$
\frac{L}{D}: \frac{2.35}{2.3} \quad 1.02
$$

This $L / D$ ratio would very likely be entirely satisfactory, but it is below the desired range. It is an indication that little difficulty will be had in meeting the bearing requirements, however. Assume $L / D=1.25$, and to reduce $V$ below its allowable limit, let $I$ ) 2.25 in . Then

$$
\begin{aligned}
& L=1.25 \times 2.25=2.82 \mathrm{in} . \\
& A=2.25 \times 2.82=6.35 \mathrm{in} .
\end{aligned}
$$

the mean pressure $\frac{5,245}{6.35}=825 \mathrm{lb}$. per sq. in.

$$
V=\frac{\pi \times 2.25 \times 2,000}{12 \times 60}=19.65
$$

the maximum pressure $=\frac{6,500}{6.35}=1,025 \mathrm{lb}$. per scq. in.

$$
\begin{aligned}
P V & =825 \times 19.65 \quad 16,200 \\
\bar{V} & =\frac{19.65}{825} \quad 0.0238
\end{aligned}
$$

As far as bearing requirements are concerned, for the example, a rankpin diameter of 2.25 in . and an effective bearing length of 2.82 in . $\pm$ should be: easily satisfactory.

5-6. Crankshaft Dimensions.-To perform its functions properly, an engine crankshaft must (a) be strong enough to withstand the forces to which it is subjected, (b) be rigid enough to prorent appreciable distortion, (c) have sufficient mass properly distributed so that it will not vibrate critically at the usual spereds at which it is operated, (d) have sufficient bearings of adeciuate. size to handle the loads with available lubricants, and (r) for aircraft engines, have the shaft as light as possible. ()lwiously, some of these requirements are more severe than othors, and in meeting the difficult requirements, usually the less difficult will be taken care of automatically. For instance, to mocot thr rigidity and vibration requirements, it is usually neressary to make the shaft much heavier and stronger than would be neressary for (a). Hence, a tedious stress analysis is gronerally unnecessary and seldom made on modern high-speed-engine: shafts.

The present purpose (d) is to investigate main bearing loads and determine the necessary main bearing sizes. To do this, it, is necessary to know the crankpin bearing loads, the position of the main bearings with respect to the crankpins, and the inertia loads due to unbalanced partso of the rankshaft. Therse last two items necessitate resort to past experience, if a great deal of trial-and-crror effort is to be avoided. Vnfortumately, all too few data have been assembled on crankshaft, details, hut. some assistance may be found in Tables A1-5, A1-fi, A1-7, A1-8, and A1-9.

5-7. In-line and V-engine Crankshafts.-Typiral remmples of in-line and opposed-engine crankshafts are shown in Figs. $5-11$, 5-12, and 5-13. For air-cooled engines, rankshafts will usuatly. have to be proportionally longer than for water-cooled engints
because of the greater over-all diameter (including cooling fins) of the cylinders. This may necessitate increasing the shaft sections to provide sufficient stiffness and rigidity. To avoid excessive weight, this in turn sometimes necessitates the use of main bearings between all crank arms (Fig. 5-12). To



$$
i_{16}{ }^{16} * \gamma^{\prime \prime} \left\lvert\, \frac{l^{\prime \prime \prime}}{16}=1\right.
$$

Fig. 5-11.-Continental A-40 crankshaft-four-cylinder opposed, two main bearings.


Fig. 5-12.- -Four-cylinder in-line crankshaft. Tank-70, five main bearings.


Fic. 5-13.- Continental A-50 crankshaft-four-eylinder opposed, three main bearings.
permit the necessary axial spacing of crankpin centers, the $L / D$ ratio of bearings may be increased or the crank arms may be ret at an angle. To keep down weight, it is obviously desirable to space the cylinder center lines as closely as cooling fins and other requirements will permit. Also for the same reason, for small in-line and V-type aircraft-engine crankshafts, counter-
weights are sometimes omitted. This last increases the main bearing loads due to inertia forces from unbalanced crank arms and crankpins and is a questionable saving.


Fig. 5-14.-Diagram illustrating a method for finding the unbalaned woight to apply in determining main bearing loads in in-line and V-engines.

5-8. Example. - With reference to Fig. 5-14, determine the added load on main bearings $A$ and $B$ due to the unbalanced weight of the crank. Assume 2,000 r.p.m. and a density of shaft material of 0.28 lb . per eu. in.

Solution.
Volume of crankpin $=0.785(4-1) 3=7.06 \mathrm{cu} . \mathrm{in}$.
Weight of crankpin $=7.06 \times 0.28=1.98 \mathrm{lb}$.
Distance to center of gravity $=3 \mathrm{in}$.
Volume of unbalanced part of crank arms

$$
=2 \times 1 \times 3 \times 2.5-0.785 \times 1^{2} \times 2=13.43 \text { (u. in. }
$$

Weight of unbalanced part of crank arms $=13.43 \times 0.28=3.76 \mathrm{lh}$.
Distance to center of gravity $=3 \mathrm{in}$.
Total weight of unbalanced parts $=1.98+3.76=5.74 \mathrm{I} \mathrm{h}$.
Distance to center of gravity of crankpin and unbalanced parts of erank arms $=3 \mathrm{in}$.
The centrifugal force on the unbalanced crank is [from Ea, (i)-1)]

$$
F_{C}=0.0000284 \times 5.74 \times \overline{2,000}^{2} \times 3=19.99 .6 \mathrm{lb}
$$

This load may be assumed to he divided equally betwern the two adjarent main bearings; hence each bearing will be subjected to a load of 979.8 Ib . This load is, of course, in addition to that imposed by the forees acting on the crankpin.

The use of chamfered and rounded crank arms (Fig. 5-15) aids materially in reducing main bearing loads by reducing the unbalanced weight and distance to the conter of gravity. Theser refinements are usually possible without sacrifiee of arankshaft strength or stiffness. Chamfering at the main bearing and of the crank arm serves principally to reduce the weight. of the shaft

5-9. Radial-engine Crankshafts. Although the adden weight, is undesirable, it is always necessary to counterbalance radial-
engine crankshafts to attain static balance and to reduce the unbalanced loads on the main bearings. These loads are much greater in a radial engine due to the greater number of connecting rods attached to the crankpin. The determination of the size of counterweights will be considered later; their only effect in connection with the present consideration of main bearing loads is in permitting the assumption that the inertia forces are completely balanced by the counterweights. ${ }^{4}$ Hence, the sum of the main bearing loads at any crank angle is represented by the gas-load vector $F_{G R}$, (Figs. 5-9 and 5-10) at that angle.

The principal dimensions of several radial-engine crankshafts are


Fig. 5-15.-Crank arm details for noncounterweighted in-line and V-type aircraft-engine crankshafts. ( $A$ ) Methods used in chamforing engine crankshaft arms. ( $B$ ) Typical crank-arm contours. (From Angle, "Engine Dynamics and Crankshaft Design.") given in Table A1-9. General arrangement of details is indicated in Fig. 5-16.


Fig. 5-16.-General arrangement of typical radial-engine crankshafts. (A) General arrangement of the Pratt and Whitney Wasp two-piece crankshaft. (B) General arrangement of the Wright Whirlwind two-piece crankshaft. (C) General arrangement of the LeBlond one-piece crankshaft.

5-10. Resultant Forces on Main Bearings.-Load distribution on erankshaft main bearings cannot be determined exactly because of uncertainty as to the effects of crankshaft and crankcase distortion, misalignment of bearings, bearing clearanees, etc., but the following procedure is in common use and has proven satisfactory for conventional designs.

In in-line and V-engines where there is a main bearing on earh side of the crankpin, the forces acting on the crankshaft bearings are obtained by considering the force at the crankpin, tugether with the centrifugal force due to the unbalanced part of the rank arms and crankpin (when counterweights are not used), to be equally divided between the two crankshaft bearings at ach side of the crankpin. The load on end main bearings may be taken as one-half of the load on the adjacent crankpin bwaring plus (vectorially) one-half of the centrifugal load due to the crank (when the shaft is not counterbalanced). The loads on intermediate and center main bearings may be taken as the vector sum of onchalf the loads due to ach adjacent rank, i.e., one-half of each adjacent crankpin load phas (vertorially) one-half of each of the unbalanced adjacent crank-irm loads.

To illustrate the procedure, assume that Fig. 5-2a (A) represents a crankpin polar diagram for a conventional six-relindor in-line engine having crank arms arranged as in Fig. 4-13 and a firing order of 1-5-3-6-2-4. Figure 5-17 shows a mothoul of finding the resultant forces on the main bearings. In this figure, $F_{R_{1}}$ is the resultant foree on crankpin 1 at $\theta_{1}(=30$ deg. of crank angle from the beginning of the power stroke). The magnitude and direction ( $\alpha_{1}$ ) of $F_{R_{1}}$ is found in Fig. 5-2a (A). $F_{C S_{1}}^{\prime}$ (Fig. 5-17) is the centrifugal forec due to the unbalaneral weight of crank 1. (This force is constant for a given angine speed and always acts along the crank-arm axis.) The rewnltant force on main bearing 1 is $F_{R, M_{1}}=F_{k c_{1}} 2$ (Fig. 5-17), and its direction with respect to the congine axis is $\sigma_{1}$.

The resultant force on main bearing 2 is determined hy taking one-half the vector sum of the resultant fores at ranks 1 and 2. Referring again to Figs. 5-17 and 5-2a (A), $F_{k_{2}}$ is the reviltant force on crankpin 2 when crank 1 is at $\theta_{1}$ deg. from the breginning of the power stroke in No. 1 revinder. $F_{r=s}$ is the erentrifugal force due to the unbalanced part, of rank $2, F_{\text {me }}$ is the verefor

and $F_{R C_{2}}$. The resultant force $F_{R M_{2}}$ on main bearing 2 is equal to one-half of $F_{R C_{1,2}}$, and its direction with respect to the engine axis is $\sigma_{2}$.

An alternate method, which in some cases simplifies the construction of main-bearing polars, is to divide each vector


Fig. 5-17.-Method of finding resultant forces on the main bearings of in-line engines. (Six-cylinder crankshaft illustrated.)
component by 2 before applying it in the construction. The resultant vectors are then $F_{R M_{1}}, F_{R M_{2}}$, etc., directly.

In finding $F_{R_{1}}$ and $F_{R_{2}}$, it is necessary to take account of the firing order as well as the angular relation of the crank arms. To reduce the confusion in doing this, the system illustrated in Fig. 5-18 is useful. For instance, suppose crank 1 is 30 deg . $\left(=\theta_{1}\right)$ past the beginning of the power stroke and it is desired to know the value and direction of $F_{R_{2}}$. From Fig. 5-18, crank 2

Cylinder Numbers



Fig. 5-18.-Method of determining the effect of crank angularity and firius order in constructing polar diagrams for main bearing. (Six-revinder in-line engine illustrated.)
will be on the exhaust stroke and at the $270-\mathrm{deg}$. position in terms of crank 1. Hence, from Fig. 5-2a (A), $F_{R_{2}}$ is the resultant force at the $270-\mathrm{deg}$. position, and its direction is $\alpha_{2}$ deg. with respect to the center line of the cylinders. Similarly, $F_{R_{5}}$ may be found for any position of crank 4, etc. Figure 5-18 applies only to the crankshaft and firing order given, but a similar chart may be readily constructed for any other engine.


Fig. 5-19.-(A) End-main-bearing and (B) intermediate-main-bearing polar diagrams for a $41 / 2-\mathrm{in}$. by $53 / 8-\mathrm{in}$. six-cylinder in-line aircraft engine having a crankshaft and firing order as in Fig. 5-18. Angles in parentheses () are relative positions of crank arm on opposite end of main bearing under consideration.

Figures 5-19 and 5-20 show end-, intermediate-, and center-main-bearing polar diagrams for a six-cylinder in-line aircraft engine. The data are based on crankpin loadings as shown in Fig. 5-2a ( $B$ ) in which the cylinder dimensions, gas-pressure forces, and reciprocating weights are the same as for Example 1. The rotating weight has been taken as 2.5 lb . per crankpin, and the speed is 2,000 r.p.m. The unbalanced weight of each crank arm is assumed to be 6.835 lb . at crank radius distance from the center of the crankshaft.

In single-bank radial engines, it is usually assumed that the inertia forces are completely balanced by the crankshaft counterweights and that the sum of the main bearing loads at any angular
position of the crankshaft, is represented hy the gas-load vector $F_{G R}$ (Figs. 5-9 ard 5-10) at that angle. ${ }^{4}$ In keepping with the preceding method for in-line and V-engine shafts, it would be logical to assume that each main bearing took one-half of this load. However, experimental evidence indieats that the londs are more nearly distributed as 40 per cent to the roar main

 cylinder in-line aircraft engine having a crankshaft, and firing owh as in fir. 5-18. Angles in parentheses () are relative positions of rank arm con whurit. end of main bearing under consideration.
bearing, 75 per cent to the front main bearing, and 15 per (efnt radial load in the opposite direction on the thrust braring in tha nose of the crankcase (Table A1-10).

5-11. Example.-1. Construct polar diagrams for the main hearings of the engine in Fxample 1, using a load distrihution of fo fror ernt th the rear main bearing and 75 per eent to the front main bearing.
2. By assuming plain bearings, a maximum unit bearing land wi 1.010 fl . persq. in. of projected area, an allowable rubhing velority of 20 f.f.e., and :
 and length of main bearings necessary.
3. By assuming ball or roller bearings, determine the sizes necessary.

Procedure 1.-On the assumption that the inertia forces are completely balanced, the gas loads are most conveniently obtained from either Fig. 5-9 or 5-10. In Fig. 5-10, $\delta$ represents the direction of the gas-force resultant $F_{G R}$ with respect to the center line of the crank arm. If $\theta_{1}$ represents the crank-arm position with respect to No. 1 cylinder center line, the direction of the $F_{G R}$ vector is $\theta_{1}+(180-\delta)$ with respect to No. 1 cylinder. Values of $F_{G R}$ and $\delta$ for various values of $\theta$ have been scaled directly from Fig. 5-10 and arranged for convenience in Table 5-2.

Table 5-2

| $\theta$ | $\delta$ | (180- $\delta$ ) | $\theta+(180-\delta)$ | $F_{G R}$ | $0.4 F_{G R}$ | $0.75 F_{G R}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | 16 | 164 | 164 | 1,500 | 600 | 1,128 |
| 20 | 28 | 152 | 172 | 6,100 | 2,440 | 4,580 |
| 40 | 52.5 | 127.5 | 167.5 | 4,600 | 1,840 | 3,450 |
| 60 | 71 | 109 | 169 | 2,900 | 1,160 | 2,180 |
| 80 | 92.5 | 87.5 | 167.5 | 1,700 | 680 | 1,278 |
| 100 | 104 | 76 | 176 | 750 | 300 | 562 |
| 120 | 27 | 153 | 273 | 450 | 180 | 338 |
| 140 | 15 | 165 | 305 | 1,250 | 500 | 938 |
| 160 | 25 | 155 | 315 | 5,850 | 2,340 | 4,390 |
| 180 | 48 | 132 | 312 | 5,200 | 2,080 | 3,000 |

Values of $0.75 F_{G R}(A)$ and $0.4 F_{G R}(B)$ for the various values of $\theta$ are plotted with respect to the center line of No. 1 cylinder as shown in Fig. 5-21.


Fic. 5-21.- (A) Front- and ( $B$ ) rear-main-bearing polar diagrams for a fivecylinder single-bank radial engine (Example 1).

As $F_{1 ; R}$ (Fig. 5-10) repeats $n / 2$ times per revolution ( $n=$ number of (rlinders), the main-bearing polars will also repeat $n / 2$ times per revolution. Ifence, one loop is sufficient for maximum and mean force data. However,
the completed diagram may be quickly drawn by shifting the tracing paper angularly the proper amount for each loop. The complete polar is useful in showing the positions and directions of critical loadings on main-bearing supports and for relative wear studies. The relatively high ratio of maximum to mean force in radial-engine main bearings as compared with in-lineengine main bearings and the high rate of change of force (shock loadings) should be noted.

Procedure 2.-For the front main bearing, the projected bearing area will be

$$
\frac{4,580}{1,000}=4.58 \text { sq. in. }
$$

From Eq. (5-3),

$$
D=\frac{720 \times V}{\pi \times N}=\frac{720 \times 20}{\pi \times 2,000}=2.3 \mathrm{in}
$$

To reduce $V$ below the allowable limit, let $D=2.25 \mathrm{in}$. Then

$$
\begin{aligned}
& L=\frac{4.58}{2.25}=2.04 \mathrm{in} . \\
& V=\frac{2.25 \times \pi \times 2,000}{720}=19.6 \mathrm{f.p.s}
\end{aligned}
$$

The mean force is $1,807 \mathrm{lb}$., hence

$$
P V=\frac{1,807}{4.58} \times 19.6=7,750
$$

For the rear main bearing, the projected area will be

$$
\frac{2,440}{1,000}=2.44 \text { sq. in. }
$$

and by assuming the same diameter as for the front main

$$
L=\frac{2.44}{2.25}=1.085 \mathrm{in}
$$

Procedure 3.-For the front main bearing [Fig. 5-21 (A)], the average forere is $1,807 \mathrm{lh}$., the maximum foree is $4,580 \mathrm{lb}$., and the speed is $2,000 \mathrm{r} . \mathrm{p} . \mathrm{m}$. On the assumption that ball bearings are to be used (Table Al-22), $L=1,807$ lb., $Z=0.88$ for an assumed bearing life of $2,500 \mathrm{hr}$. and $K=2.0$, or 2.5 say 2.25. Then

$$
C=1,807 \times 0.88 \times 2.25=3,580 \mathrm{lb}
$$

The diameter of the main bearings should not be less than the diameter of the crankpin, and the front main bearing for direet drive will have to be greater in diameter than the largest, diameter of the S.A.E. stamdard whaft end that is to be used. The crankpin diameter (Par. 5-5) is 2.25 in., amb from Fig. A1-6, the logical propeller-shaft end will be S.A.E. taper type

No. 1. From Table A1-20, the maximum diameter of a taper type S.A.E. No. 1 shaft end is 2.05 in . Hence a front main bearing base diameter of 2.25 in. should be about adequate. From Table A1-22D, S.A.E. bearings 212,312 , and 412 are adequate in bore diameter, but from Table A1-22E, it is seen that at 2,000 r.p.m. the ratings are too low. From Tables A1-22F and A1-22G, it is evident that S.A.E. bearing 413 having a bore of 2.5591 in . or bearing 314 having a bore of 2.7559 in. could be used. Use of a shock factor of $K=2$ or of a bearing life of $2,000 \mathrm{hr}$. would permit the use of S.A.E. bearing 412, but at the expense of a reduction in the factor of safety or life of the engine.

For the rear main bearing $L=962 \mathrm{lb} ., Z=0.88$, and $K=2.25$. Then

$$
C=962 \times 0.88 \times 2.25=1,900 \mathrm{lb}
$$

From Tables A1-22D and A1-22E, S.A.E. bearing 212 having a bore diameter of 2.3622 in . could be used, or if it was desirable to have the same front and rear bearing bore diameters, bearings 213 or 214 could be used.

If roller bearings are desired (Table A1-23) for the front main, $L=1,807$ lb., $Z=0.64$, and $K \approx 1.5$. Then

$$
C=1,807 \times 0.64 \times 1.5=1,735 \mathrm{lb}
$$

From Tables A1-23B and A1-23C, bearings RLS-16-L or RLS-16-LL would be adequate. For the rear main, $L=962 \mathrm{lb} ., Z=0.64$, and $K \approx 1.5$. Then

$$
C=962 \times 0.64 \times 1.5=925 \mathrm{lb}
$$

From Table A1-23D, bearing RXLS - 2.25 would be adequate.
5-12. Relative Wear Diagrams.-For the purpose of determining the best location of the oilhole for crankpin bearings having force-feed lubrication, relative wear diagrams are useful. A method of constructing such diagrams follows: ${ }^{3,2}$

The bearing pressure is assumed to be evenly distributed over an arc of 180 deg. on the crankpin. The magnitude and direction of the force with respect to the crank arm is obtained at equal intervals throughout a complete cycle from a polar diagram of resultant forces on the crankpin. These forces are plotted as a series of half rings having their radial thicknesses proportional to the magnitude of the force and their mid-points falling on a line through the center of the crankpin in the direction of the application of the force considered. The summation of these rings produces an area which is termed the comparative wear on the crankpin. The best location for the oilhole is that point on the crankpin where the radial thickness of this resulting area is a minimum.


Fig. 5-22.-Diagram illustrating a method of constructing relative wear diagrams for crankpins. [Data from Fio. 5-2 (a) (B).]

 421 and Angle, "Engine Dynamics and 'rankstuft Dessith.";

As an example of the construction, let Fig. 5-2 (a) (B) represent a polar diagram for a crankpin in which the best location for the oilhole is desired. By measuring to scale radially out to the curves [Fig. 5-2 (a) (B)] at increment crank angles, values of force in the direction of the crank-arm axis are found (Table 5-3). Plotting these forces as explained above gives Fig. 5-22.

Table 5-3

| $\theta$ | Forces in direction <br> of crank-arm axis | Total force in direction <br> of crank-arm axis |
| ---: | :---: | :---: |
| 0 | 2,250 | - |
| 20 | 1,150 | 2,250 |
| 40 | 900 | 1,150 |
| 60 | 780 | 900 |
| 80 | 790 | 780 |
| 100 | 870 | 790 |
| 120 | 1,040 | 800 |
| 140 | 1,320 | 1,040 |
| 160 | $1,550,2,500,3,700$ | 1,320 |
| 180 | $1,600,1,950$ | 7,750 |
| 200 | $1,540,1,680$ | 3,550 |
| 220 | $1,300,1,370$ | 3,220 |
| 240 | $1,000,1,010$ | 2,670 |
| 260 | 800,840 | 2,010 |
| 280 | 710,720 | 1,640 |
| 300 | 730,7730 | 1,430 |
| 320 | 800,840 | 1,460 |
| 340 | $500,1,240$ | 1,640 |
| 360 | 2,250 | 1,740 |

A relative wear diagram for a V-type engine is shown in Fig. 5-23.

For radial engines, the polar diagram with respect to the crankarm axis (Fig. 5-10) should be used to construct the relative wear diagram for the crankpin.

This method of determining the oilhole location has been criticized by some sources on the grounds that it does not take into account the effect of centrifugal force on the oil in the crankpin. Thus they maintain that the oilhole should be located on the outer side of the crankpin regardless of what the wear diagram might show. Such a location would undoubtedly
be satisfactory in most engines and would save considerahle tedious construction.

## Suggested Design Procedure

Important. Make all constructions and diagrams to a large enough seale to permit accurate work. Size B or larger drawing paper is recommended. Keep a record of the man-hours required on each item.

1. For the engine selected for your design, construct polar diagrams of forces on the crankpin (a) with respect to the engine axis and (b) with respect to the crank-arm center line.

For in-line and V-engines, construct the diagrams through 720 deg. of crank travel. For radials, construct the diagrams through a suffieient number of degrees of crank travel to accurately define the shape and spacing of the lobes. Then, for part $a$, complete the diagram through $720 \mathrm{~d} \cdot \mathrm{~g}$. by shifting the tracing paper.

For part $b$ of radial-engine polars, locate two or more higher r.p.m. peints on the crank-arm axis.
2. Determine the maximum and mean forees, and locate values found on the diagrams constructed in item 1.
3. By using bearing loads, rubbing factors, ete., within the ranges given in Appendix 1, determine crankpin dimensions that will be adequate for bearing purposes.
4. Lay out to scale the general arrangement of crankshaft desired. Estimate the unbalanced weight per crank arm and the distance to the centar of gravity.*

Refer to available sectional blueprints, specimen crankshafts, cte., for assistance in making the layout. Do not try to include details other than those necessary to the determination of unbalanced-weight data. For radials, this item is unnecessary at this point.
5. Construct main-bearing polar diagrams for all differently loaded main bearings.

For in-line and V-engines, construct the diagrams through 720 deg. of crankshaft travel.

For radials, construct the diagrams through a sufficient number of degreos of crankshaft travel to define accurately the shape and spacing of the lohes. Then complete the diagrams through 720 deg. by shifting the tracing paper.
6. Determine the maximum and mean forces, and locate valum found on the diagrams constructed in item 5 .
7. By using bearing loads, rubbing factors, ete., within the range. given in Appendix 1, determine main-bearing dimensions that will be adequate: for bearing purposes.
8. Construct a relative wear diagram for the rankpin of yome rngine, and show the best oilhole location, or locate hole on outside of rankpin in plane of crank arms.

* When this distance is not equal tos the crank radins, as is usually the case, it is frequently the custom to use an equimalent unbalaneod woight, that is considered to act at crank radius from the center of rotation.

9. When items 1 to 8 have been completed and put in proper form, submit for checking and approval.

## References

1. Heldt: "Automotive Engines."
2. Angle: "Engine Dynamics and Crankshaft Design."
3. A.S.I.C. 421.
4. S.A.E. Jour., Vol. 28, No. 4, April, 1931.
5. S.A.E. Jour., Vol. 29, Nos. 4 and 5, October, November, 1931.
6. Mark's "Handbook," 2d ed., p. 279.
7. S.A.E. Jour., Vol. 35, No. 6, December, 1934.
8. Unpublished design notes of A. J. Meyer.
9. Design of Engine Bearings, Automotive Ind., Aug. 1, 1939.
10. Willi: Engine Bearings from Design to Maintenance, S.A.E. Jour., Vol. 45, No. 6, December, 1939.

## CHAPTER 6

## DESIGN OF RECIPROCATING PARTS

6-1. Design Requirements and Limitations.-The design of any machine element can be of reasonably certain effectivencons only when the designer ( $a$ ) is fully aware of and properly eonsiders the functions that the clement must perform, and (b) is cognizant of the capabilities and limitations of the materials that can be used for the element. Hence, in procecding with the design of individual parts of the engine, it is adrisahle to consider briefly the requirements, possibilities, and limitations of those parts in somewhat the same way that was done with the unit as a whole (Chap. 1).

6-2. Functions of the Piston.-Aircraft-engine pistons are called upon to satisfy a rather formidable list of requirements. Most, but not necessarily all, of these requirements aro listed as follows:

The piston must

1. Take the gas-force load without appreciable distortion.
2. Fit closely enough in the cylinder to prevent fiston slip, excessive blow by, or oil pumping.
3. Be capable of conducting away a large portion of the heat, generated in the combustion chamber.
4. Have a coofficient of expansion surh that the piston will not be too loose in the cylinder when cold or too tight when hot.
5. Have cross sections and a coefficient of heat flow wifficient to conduct away the heat absorbed hy the head at a rate that will prevent hot spots and a resulting increased tembency of the furl to detonate.
6. Have skirt dimensions sufficient to conduct a considerable portion of the heat absorbed by the head to the celimder walls and to provide adequate bearing area to take the side thrust.
7. Be capable of giving up some of the heat abserthed to the lubricating oil without raising part of the oil to a temperature that might impair its lubricating qualities.
8. Provide adequate support for the piston rings.
9. Have adequate bearing area for the piston pin and support-ing-pin bosses rigid enough to prevent excessive localized pinbearing pressures.
10. Be as light in weight as possible.
11. Have adequate resistance to wear.

At best, some of these items are directly conflicting, and the designer is faced with the ever-present problem of judging where to strike a proper compromise. If he strives to reduce reciprocating inertia forces by reducing the piston weight to a very low value, he usually will have to sacrifice section thicknesses to a point where heat-flow characteristics will be impaired. Quite often the attainment of close piston fits in the cylinder necessitates the use of a denser metal to get the proper coefficient of expansion characteristics, and this is apt to mean a heavier piston. Many other conflicting problems requiring compromise solutions will occur to the student.

6-3. Piston Materials.-In keeping with the preceding requirements, an aircraft-engine piston should have

1. Adequate mechanical strength at working temperatures.
2. A low coefficient of linear expansion.
3. A high coefficient of thermal conductivity.
4. A low density.
5. A high resistance to abrasion.

By far the most common metals used for pistons are aluminum and cast iron. Important properties of these two metals are given in Table 6-1. Obviously neither of these metals is superior from every standpoint. However, owing partly to improved characteristics imparted by small quantities of other metals and partly to improved fabrication technique, almost all modern aircraft engines use aluminum-alloy pistons. Usually they are cast in permanent molds or forged.

The most commonly used aluminum alloys for pistons are S.A.E. 34 (Aluminum Co. designation 122), S.A.E. 321 (Aluminum Co. designation A132), and the so-called Y-alloy (Aluminum Co. designation 142). Important properties of these alloys as given by the Aluminum Company of America are listed in Tables A2-1 to A2-5. Alloy A132 is recommended by the Aluminum Co. as being particularly desirable for aircraft-
engine pistons because of its low coefficient of expansion and low specific gravity.

6-4. Piston Dimensions.-Detailed dimensions of pistons are to a very considerable extent a matter of enginecring judgment. The functions of the piston are so numerous and the heat flow, stresses, etc., are so involved that a rational approach is too complex to be of practical value. However, useful aids may be had from a study of previous designs (Table A1-14) and from empirical rules.

Table 6-1.-Properties of Piston Memala*


* Pure metals, not the alloys.

Huebotter and Young, ${ }^{2}$ following extensive tests on automotiver pistons, have drawn the following conclusions relative to piston design:

1. A deep section at the center of the head is very effective in lowering the maximum temperature. For this reason a liberal center-hole boss is recommended.
2. If ribs are used to reinforce the piston-pin bosses, they should extend to the center of the head.
3. The aluminum alloy piston has a wide margin of safety over the gray iron piston on a temperature basis.
4. The ring belt dissipates about 60 per cent as much heat from a given initial temperature as that . . . from the pistom skirt.

Temperature gradients for a typical aluminum-alloy and a gray-iron piston are shown in Figs. (j-1 and (i-2. Although not,
geometrically identical, these two pistons are sufficiently similar in section to show the decided thermal advantage of aluminum. The relative weights of the two pistons are also of interest.

Typical aircraft-engine pistons are shown in Fig. 6-3. Current practice indicates the desirability of three or four rings above the pin bosses, frequently one ring near the bottom of the skirt,


Fig. 6-1.-Temperature gradients in an aluminum-alloy piston. Weight $=$ 2.635 lb . Cylinder diameter $=4.5 \mathrm{in}$. (From Huebotter and Young, Flow of Heat in Pistons. Purdue University Engr. Exp. Sta. Bull. 25).


Fig. 6-2.-Temperature gradients in a gray-iron piston. Weight $=5.853$ lb. Cylinder diameter $=4.5$ in. (From Huebotter and Young, Flow of Heat in Pistons. Purdue University Engr. Exp. Sta. Bull. 25.)
ribs under the head for rigidity and better cooling, and amply supported pin bosses.

Piston clearance must be adequate to prevent " hot seizure" and small enough to prevent "cold slap." Customary practice for automotive engines has been

For gray iron, clearance $=0.001 \times$ bore in inches. For solid-skirt aluminum, clearance $=0.0006 \times$ (bore) ${ }^{2}$.in inches.

These rules should not be applied to special types such as Invar or steel-strut and flexible-skirt cam-ground pistons.

Aircraft pistons may be fitted with greater clearance as they operate nearer rated load most of the time (see Table A2-3 for
coefficients of expansion). Clearance and other datat on current. automotive pistons will be found in Table Al-3. Swan ${ }^{4}$ sug-


Fig. fi-3.-Typical aireraft-engine pistoms.
gests the following piston clearances for $Y$ and similar almminum alloys:

| Top of head. | (1) Off) |
| :---: | :---: |
| Bottom of head. | 0.00 .4 |
| Top of skirt. | 0. 01025 |
| Bottom of skirt. | 0.0615 |

Piston-ring and groove dimensions have beren standardized by the Socicty of Automotive Engineers (ere T:able Al-1fi), but many aircraft engines are equipped with rings that do mot. conform to these standards.

Locate the piston pin approximately halfway befwern the lower ring groove above piston bosses and the and of the piston
skirt. Current practice on relative diameter-length ratios of pistons and other details may be observed from Table A1-14. The piston skirt below the upper ring belt is usually considered to take the side thrust, i.e., act as the bearing area between the piston and cylinder wall. This area is the equivalent of the crosshead bearing area in engines using that type of construction. Angle suggests using about 1 sq. in. of bearing surface for each 50 lb . of average side pressure. From the piston side thrust (see Par. 4-9 and Fig. 4-10), the average side thrust may be determined. Then the necessary length of piston skirt will be

$$
\begin{equation*}
P_{L}=\frac{T_{S A}}{D \times 50} \tag{6-1}
\end{equation*}
$$

where $T_{S A}=$ average side thrust against the cylinder wall, lb . $D=$ cylinder diameter, in.
$P_{L}=$ length of the piston skirt.
The total length of the piston will be $P_{L}$ plus the width of the upper ring belt. However, if the value of $P_{L}$ as found from Eq. (6-1) is appreciably greater or less than current practice, the length of the skirt should be altered to fall within the range of values for similar engine pistons.

As there is very little side pressure on the piston in the direction of the piston-pin axis, a reduction in piston weight may be made by cutting away the skirt below the ends of the pin. However, it is doubtful if the gain in reduced inertia forces offsets the added complexity of construction and probable increased lubrication or oil-pumping problems except in very high-speed racing engines.

- 6-5. Piston Rings.-Piston rings should be (a) sufficiently elastic to exert the necessary side pressure against the cylinder walls and to permit insertion of the ring in its groove by sliding it over the piston, and (b) soft enough to prevent excessive wear on the cylinder walls. Close-grained cast gray iron is almost universally used for piston rings.

Special shapes and types of piston rings are sometimes used to permit closer control of the lubricant, more rapid seating, and to reduce blow by of the combustion gases (see reference 3). However, as it is quite common practice to purchase piston rings from companies specializing in their manufacture, the engine designer will probably do well to merely specify over-all
S.A.E. standard dimensions (Table A1-16) and follow the speecific: recommendations of the ring specialists on details.

End clearance on rings should be great enough to prevent any possible binding from heat expansion but small enough to prevent excessive gas leakage. A gap clearance of 0.003 in. per inch of bore is commonly specified ${ }^{3}$ by automotive-engine manufacturers. Butt, diagonal, and lap-joint ring ends (Fig. 6-4) are most common. Side clearance of rings in piston grooves


Fig. 6-4.-Common types of piston-ring joints. should be about 0.001 in. to minimize leakage through the piston groove behind the ring (Table A1-16).

6-6. Piston or Wrist Pins.-Piston pins, the connecting links between the piston and connecting rods, may be cither clamped in the piston, clamped in the connecting rod, or full floating. This last method permits the pin to turn gradually so that wear is more evenly distributed, but it requires some form of snap ring or soft metal button to prevent the end of the hard pin from coming in contact with and scoring the cylinder wall.

The average distance between the pin bosses for the pistons in Table A1-14 is about 48 per cent of the piston diameter, and by allowing for end clearance on the small end of the commerting rod, the length of the piston-pin bearing in the connecting rod will be about 45 per cent of the piston diameter. For fullfloating pins (after allowing for end buttons), this will permit about equal bearing areas in the upper end of the conneeting rod and in the piston. Hence the piston-boss length may he made approximately one-fourth of the piston diameter, and the length of the pin bearing in the connecting rod may be made. 45 per cent of the diameter.

The diameter of the piston pin will be determined by the maximum allowable bending moment and the allowable hearing pressure. Maximum stress in the pin will orerur at full-throttle low-speed (low inertia) conditions, and the pin may br assumed to take the full force of the explosion pressure in the combustion chamber. Maximum gas pressures were assumed to be about, 75 per cent of the theoretical pressures (Par. 3-3). Hence the
maximum force on the piston pin in pounds is

$$
P_{\max }=\frac{0.75 \pi D^{2} P_{c}}{4}=0.59 \dot{D}^{2} P_{c}
$$

where $D=$ cylinder diameter, in.
$P_{c}=$ calculated theoretical maximum pressure, lb. per sq. in. abs. [Eq. (3-3)].
The projected bearing area in the upper end of the connecting $\operatorname{rod}$ is

$$
S=d L=0.45 D d
$$

where $d=$ diameter of the piston pin, in.
$L=$ effective length of the piston pin, in.
$D=$ cylinder diameter, in.
Because of the low rubbing velocities, much higher bearing pressures may be used for piston pins than for crankpins provided suitable bearing metals such as phosphor bronze (Table A2-8) are used for connecting-rod bushings and the crankpins are casehardened.

Heldt ${ }^{3}$ suggests an average piston-pin pressure of $3,200 \mathrm{lb}$. per sq. in. as representative of automotive practice, but values of 10,000 to 15,000 are not uncommon in high-powered aircraft engines. Thus

$$
\frac{0.59 D^{2} P_{c}}{0.45 D d}=B_{p}
$$

where $B_{p}=3,000$ to 15,000 , with 5,000 to 10,000 probably being a safe range for small aircraft engines of good design. Hence the piston-pin diameter may be found from

$$
\begin{equation*}
d=\frac{D P_{c}}{K} \tag{6-2}
\end{equation*}
$$

where $K=4,000$ to 8,000. Data in Table A1-14 indicate that piston-pin diameters are usually about 25 per cent of the piston diameters.

The piston-pin diameter as determined by Eq. (6-2) is that necessary for adequate bearing area. However, the piston pin must also be strong enough to withstand the stresses involved and as light in weight as possible. Reduction in weight may be made by using a hollow piston pin, the size of the hole in the pin
being determined by the maximum bending moment and the allowable stress.

For determining the diameter of the hole in the piston pin $d_{1}$ (Fig. 6-5), it may be assumed that the gas-force load $l_{\text {max }}$ is
 equally divided betwern the pin bosses and acts as a concentrated load at the mid-point of their lengths. The reaction load in the: connecting-rod bearing may be assumed as equally distributed over the length of the bearing. ${ }^{3,4}$ Then from Fig. (i-5 ( $B$ ), the maximum bending moment (at, the midpoint along the piston pin) will he:

(B)

Fra. 6-5.-Average location and magnitude of forces on aircraftengine piston pins.

$$
\begin{aligned}
M & =\frac{P_{\max }}{2} \times \frac{0.75 I)}{2}-\frac{P_{\max }}{2} \\
& \times \frac{0.45 D}{3}=0.1125 I I_{\max } \quad((1--3)
\end{aligned}
$$

$$
\text { where } M \text { maximum bembing }
$$ moment, in.-ll.

$P_{m a x}=\operatorname{maximum}$ gas fore on the piston, 1 ).
$D=$ diameter of the piston, in.

For equilibrium conditions, this moment [Eq. (6-3)] mast "rual the internal moment. ${ }^{5}$

$$
\begin{equation*}
M=S \frac{I}{C} \tag{ti-1}
\end{equation*}
$$

where $S=$ maximum allowable stress, lt. per sa. in.
$I=$ moment of inertia of the piston-pin ceros seretion.
$C=$ onc-half the diameter of the piston pin.
For hollow piston pins, the section modulus is

$$
\begin{equation*}
\frac{I}{C^{r}} \quad \stackrel{\pi}{32 d i}\left(l^{4} \quad d_{i}^{4}\right) \tag{j}
\end{equation*}
$$

where $d=$ diameter of the piston pin, in.

Expressing $P_{\text {max }}$ in terms of $P_{c}$,

$$
\begin{equation*}
d_{i}=\left(d^{4}-0.675 \frac{d D^{3} P_{c}}{S}\right)^{0.25} \tag{6-7}
\end{equation*}
$$

where the symbols are the same as above.
Piston pins may be made of plain carbon steel casehardened (S.A.E. 1020), nickel steel (S.A.E. 2315, 2320, or 2515), or chrome nickel steel (S.A.E. 3120, 3215, or 3220).* An allowable stress of $25,000 \mathrm{lb}$. per sq. in. may be used with the carbon steel, and $35,000 \mathrm{lb}$. per sq. in. with the alloy steels. S.A.E. 2315 steel is one of the most commonly used materials for aircraftengine piston pins.

6-7. Knuckle or Link Pins.-Dimensions of knuckle or link pins for attaching the articulated rods to the master rod may be calculated in much the same way as those of piston pins. Owing to the greater mass of inertia-producing parts between the link pins and the gas force on the piston, link pins may be made somewhat smaller than piston pins. Probably the easiest way to determine the size is to use the same fundamental formulas that were used for the piston pins and assume higher allowable bearing loads and bending stresses. Meyer ${ }^{6}$ suggests as an allowable bending stress 30,000 to $50,000 \mathrm{lb}$. per sq. in. Unit bearing loads may be somewhat higher than for piston pins because link pins have more positive force-feed lubrication. Link pins may be made of the same materials that are used for piston pins. For severe service, nickel chromium steel (S.A.E. 3125) may be used. For very severe service, such as very highly supercharged racing engines or Diesels, nickel molybdenum steel (S.A.E. 4615) may be advisable.

Link pins should be locked securely in place to prevent any endwise movement and resulting damage from contact with adjacent parts. A rather common method of securing link pins in one-piece master rods is to use small locking plates that are bolted to the outside of the master-rod flange between the link pins [Fig. 6-6 (A)]. The ends of the link pins are flared and either cut away or beveled, and the locking plates extend over their edges to prevent movement of the pins. When twopiece master rods are used, the cap bolts may be so located that

[^5]they pass through milled slots* in the sides of the link pins, thus securing them positively (see Fig. (i-14).

Link pins are commonly lubricated by pressure feed through holes in the master-rod-flanges and a passageway inside the pin [Fig. 6-6 (B)].

Link pins should be located as close to the crankpin center as clearance and structural dimensions will permit ( 1 'ar. 4-4). This


Fig. 6-6.-(A) Method of holding link pins in place, and ( $B$ ) sertion through the crankpin and a link pin of a Lyoming Type R-fiso ninerevinder radial engine showing the means provided to lubricate the link-pin bearing.
makes it desirable to keep the diameter of the pins as small as bearing loads and strength requirements will allow. When six or eight articulated rods are attached to one mastrer rol, care must be observed in providing ardecuate dearaner between adjoining rods.

6-8. Connecting-rod Shank Stresses.-('onnerting rods are subjected to

1. Compression stresses due to combined gas and inertia forees.

* Angle patent owned by Pratt and Whitney.

2. Tension stresses due to inertia forces.
3. Tension and compression stresses due to "whipping lateral acceleration of the rod.
4. Master rods in articulated systems are subjected to an additional bending stress owing to the axes of the articulated rods not passing through the center of the crankpin.

Considering these conditions in order:

1. Compression stresses are most severe at full-throttle lowspeed (low-inertia) conditions, and as the connecting rod is of intermediate length in proportion to its cross-sectional area, the slenderness ratio $L / k$ ( $=$ center-to-center length of the connecting rod divided by the least radius of gyration) usually falls


Fig. 6-7.-Connecting-rod shank sections.
within the range in which Rankine's column formula is most applicable. Hence critical compressive stresses may be found from

$$
\begin{equation*}
\frac{t_{\max }}{A} \quad \frac{S_{c}}{1+q(L / k)^{2}} \tag{6-8}
\end{equation*}
$$

where $P_{\text {max }}=$ maximum gas force on the piston, lb .
$A=$ cross-sectional area of the connecting rod at the mid-point in its length, sq. in.
$S_{c}=$ allowable stress, lb. per sq. in.
$L=$ center-to-center length of the connecting rod, in.
$k=$ least radius of gyration of the mid-section.
$q=$ coefficient depending upon the arrangement of the column ends.
Connecting-rod shank sections used in aircraft engines are most often a modified form of I or H section, but tubular sections are frequently used in articulated rods, and sometimes, when oil is supplied under pressure to the piston-pin bearing, a hollow I section [Fig. 6-7 (C)] is used. In any event, the desired end is a rod of adequate strength and stiffness with a minimum weight.

In determining the shank dimensions, account should be taken of the fact that the end supports for the connecting rods are essentially free in the plane of rotation but fixed in the plane containing the crankpin and piston-pin axes. With free ends, the deflection of the rod under load will be as in Fig. 6-8 (A), whereas with fixed ends the deflection of the rod will be as in Fig. 6-8 ( $B$ ). As the distance hetween the two inflection points $m$ and $n$, Fig. $6-8(B)$, is one-half of $L$ and since the stress in the rod varies as $L^{2}$, the rod must be four times as strong in the plane of rotation as in the plane of the crankpin and piston-pin axes.

For carbon-steel rods, $S_{c}$ should not, exceed $25,000 \mathrm{lb}$. per sq. in.; for alloysteel rods, $S_{c}$ should be held to less then $35,000 \mathrm{lb}$. persq. in. For aluminum-alloy rods, $S_{c}$ should be about $12,000 \mathrm{Ib}$. per sq. in.

Values of $q=1 / 10,000$ (for free ends) and $q=1 / 40,000$ (for fixed ends) may be used. Values for moment, of inertia and radius of gyration for several useful geometric shapes will be found in Table A3-1.

For I and H sections, a small draft angle ( 7 to 10 deg.) must be provided to permit forging, although this will be removerl when the rods are machined all over, and usually all corners are rounded with fillets. These details make it difficult to determine the moment of inertia of the section, and to simplify the procedure, an equivalent section without draft or fillet.is is frefuently used for determining over-all dimensions. Relative propertions of equivalent shank sections useful for this purpose are shown in Fig. 6-9.
2. Greatest tension in the connecting rod will orrur (for normal operation) at highest speed at the begiming of the surtion stroke. Still more severe conditions can exist in high-spered closedthrottle dives. Maximum tension may be found by means of Eq. (4-8). By using conservative values of sterss, $i . e$., values the same as for column effect in the rod (rase 1 abower) and investi-
gating for rated speed, usually the strength will be sufficient for any diving condition encountered. Ordinarily, a rod strong enough as a column is adequately strong in tension.
3. Whipping stresses are obviously greatest at highest speeds. These stresses are due to centrifugal force on the body of the connecting rod, and, as the forces act parallel to the crank arm, they tend to bend the connecting-rod shank. Magnitude of the maximum bending moment may be found from methods outlined in references 4,9 , and 11 , but ordinarily, whipping stresses need not be investigated in aircraft engines as they are well below the maximum stresses due to the gas force on the piston. ${ }^{3}$ Hence, a connect-ing-rod shank section adequate for column conditions (case 1 above) will be strong enough to


Fig. 6-9.-Equivalent mid-length connect-ing-rod shank sections representing usual proportions in aircraft-engine practice. withstand the maximum whipping stresses. This may not be true for very high-speed automobile racing engines, however.
4. Bending stresses in the master rod of an articulated-rod system due to the forces in the link rods not passing through the center of the crankpin are ordinarily not critical because of the small distance between the line of these forces and the crankpin axis. The conventional practice of tapering the master-rod shank, i.e., increasing the cross section toward the crankpin, usually provides an adequate safeguard against critical stresses in the master rod owing to forces in the articulated rods. In cases where extremely light weight is desired, it may be advisable to investigate these bending stresses, however. The method suggested in reference 4 may be used for this purpose.

In general, for conventional aireraft engines, a connecting-rod shank section adequate for case 1 above will be amply strong in tension, whipping, and bending due to articulated rods. In tapering the shank seetion, care should be taken to avoid reducing the section near the piston pin to a point where it becomescritical.

6-9. Connecting-rod Cap Bolts.-When a one-piece crankshaft is used (Figs. $5-11,5-12,5-13$, and $5-16 c$ ), the big end of the connecting rod must be made in two pieces in order to get it onto the crankpin. In place, the two parts are held together by two or four bolts usually called cap bolts. These bolts are subjected to tensile stresses when the rod is under tension. The maximum tension occurs at maximum speed at the start of the suction stroke. This tensile force is due to the inertia of the reciprocating parts plus the centrifugal force due to the rotating parts, since these forces act in the same direction at the start of the suction stroke. The reciprocating inertia force may be found by means of Eq. (4-8), and the centrifugal force may be calculated by Eq. (5-1). The reciprocating weight may be taken as the sum of the weights of the piston, piston rings, piston pin, and onethird of the weight of the connecting rod, or the value found in item 2, Suggested Design. Procedure, p. 56, (from Figs. A1-3 and A1-4) may be used. The centrifugal weight may be taken as two-thirds of the weight of the connecting rod minus the weight of the cap, or (for radials) the rotating weight may be the value you have used in calculating bearing loads (Fig. A1-5).

The diameter of the cap bolts may be found by using an allowable tensile stress of about $20,000 \mathrm{lb}$. per sq. in. Connecting-rod bolts should conform to S.A.E. standard dimensions and materials whenever possible (see Table A1-17). S.A.E. 2330 steel is one of the most commonly used aircraft-engine connecting-rod capbolt materials.

6-10. Connecting-rod Ends.-Connecting-rod ends provide the necessary backing for the bearing metal and transmit the loads to the bearing pins. In addition, they conduct away some of the heat generated in the bearing.

To avoid excessive localized bearing pressures, rod ends should be as free from distortion as possible. To provide this necessary rigidity and at the same time keep the weight, to a minimum, designers frequently incorporate stiffener ribs in the bearing cap and flare the rod shank where it joins the rod end. These ends and caps are somewhat similar to curved beams, and for much the same reasons as with more conventional beams, they should have a high section modulus ( $I / C$ ). In view of the shapes and loadings, the exact bending momentes and streesees at any given section are difficult to determine, but, a knowledge of beam
characteristics will aid greatly in deciding upon detail arrangements. The somewhat vaguely defined ability known as engineering good judgment is of great value in detail design such as this, and, although, like personality, it is inherent in widely varying degrees in different individuals, it can be developed to a considerable extent by alert observation and clear thinking. Specifically, in the design of many machine parts, exact stresses either cannot be calculated or the calculations are so involved as to be impractical, but a correlation of the problem with simpler structures of similar characteristics usually aids in the intelligent selection of detail dimensions.


(B)

Fig. 6-10.-Aircraft-engine connecting-rod big ends. (A) Poor design that was subject to frequent crankpin-bearing failures. (B) Later design that eliminated the failures. (From Ricardo, "High Speed Internal Combustion Engines.')

Figure $6-10$ is a case in point. Connecting $\operatorname{rod}(A)$ was found to cause frequent bearing trouble, and, although the exact stresses in the cap and rod end resulting from tightening the cap bolts and from inertia forces would be very difficult to determine, it is quite evident that such tightening and inertia forces would cause the cap and rod ends to buckle inward at the joint between them. Bearing failures very often start from high localized pressures, hence the logical solution to the problem $(B)$ is quite apparent without even an approximate knowledge of the stresses in the parts. Intelligent avoidance of critical situations is just as important in the design of aircraft engines as in the flying of them.

Reentrant corners and abrupt changes of cross section almost invariably cause high localized stresses. In complex machine parts, it is usually impossible or impractical to calculate these stresses, but they can be avoided by using large fillets and gradual
changes of section. The result of flaring the end of the con-necting-rod shank where it joins the big end of the rod cannot readily be expressed mathematically, but even casual thought on the matter will show that it will reduce rod-end deflection (i.e., tendency to high localized bearing pressures) in much the same way that distributing a concentrated load will reduce the deflection of a simple beam.

Innumerable other instances of this sort will occur as the design proceeds, and as the habit is formed of referring complex and


Fig. 6-11.-H-section master connecting rod. (Wright.) formally insoluble problems to simple cases that are similar, in time that invaluable asset, good engineering judgment, will develop.

To reduce weight and to some extent to avoid the reentrant corners at the cap-bolt heads, studs are sometimes forged integral with the connerting rod. However, this may increase the cost of the connecting rod as it tends to complicate the forging.

Typical connecting rods for different arrangements of eylinders are shown in Figs. (j-11 to $6-15$. All these rods are from successful engines and will merit careful study.

Many radial engines use two-piece crankshafts, and this permits the use of one-piece connecting rods (Fig. (i-15). The advantage of a one-piece master rod lies mainly in the aroidance of highly stressed cap bolts and, to some extent, interference with the location of the link pins. This last, of course, becomes increasingly important as the number of eylinders per crankpin is increased. The obvious disadvantage is a more complex crankshaft.

6-11. Articulated Rods.-Articulated, or link, rods are sub)jected to the same general types of stresses as mastor connecting rods except that they are not subjected to bending stressess due to forces in other rods, item 4, Par. 6-8. Link-rod shanks should be designed according to the same general procedure as
used in master rods. They usually are not tapered, however. Detailed data on articulated rods from several well-known makes of engines are given in Table A1-18.

6-12. Connecting-rod Materials.-Aircraft-engine connecting rods may be made of the following materials:
S.A.E. steels: 1040, 2315, 2340, 3140, 3240, 3250, 6135, and 6140.

Aluminum alloy: 25 S (Tables A2-1 to A2-5).


NOTE: Bearings must be square with rod and paralle/ with each other in both planes with in $0.001^{\prime \prime}$ per inch offer line reaming;-..-------.

NOTE: Limits on machined dimensions $\pm 0.01^{\prime \prime}$ unless otherwise specified
$0.502^{\prime \prime}$ Ream ${ }^{2}$ in rod
NOTE: Max. variations in weight of rods in one engine 2 oz .

Fis. 6-12. Connecting rod for a 4 - by $5-\mathrm{in}$. in-line engine. (From Huebotter, "Mechanics of the Gasoline Engine.")

Chrome nickel steel (S.A.E. 3140) is one of the most commonly used materials for aircraft-engine connecting rods. Duralumin (25S) properly heat-treated, may be used for in-line engine rods and radial-engine articulated, or link, rods. For light or medium loadings, this aluminum alloy may be used without rod end bushings provided the piston and link pins are sufficiently hard. Nitralloy pins are satisfactory for this purpose, according to the Aluminum Company of America.

6-13. Bearings and Bearing Metals.-In general, there should be as great a difference as possible between the hardness of the
bearing metal and the pin or journal. So-called white bearing metals or babbitts (Table A2-7) are very commonly used where the loads are not too great. These babbitts may be either in direct contact with the supporting metal of the connecting rod


Frg. 6-13.-Master and articulated connecting rod used in thi Parkard 2500) airplane engine.
or, more commonly, bronze or steel backed. This last permits, replacement of the bushings without replacing or rehabhitting the connecting rod, but the path for heat flow from the bearing may be less positive. Very thin (1/16 in. or less) storel-barked babbitt-lined replaceable bushings are in quite general use. For
higher bearing pressures, copper-lead (Table A2-7) or cadmium alloys may be used. For piston and link-pin bushings, bronze bearing metals (Table A2-8) are commonly used.


Frg. 6-14.-LeBlond five-cylinder radial-engine two-piece master-connecting-rod assembly.

Aluminum alloys have fair bearing qualities, so that the common practice of allowing the piston pin to bear directly on the inner surfaces of the piston bosses is satisfactory. Bronze bearing shells in the small ends of the connecting rods and in the link-pin ends of articulated rods may be designed for a wall thickness of $1 / 16$ to $1 / 4 \mathrm{in}$.


Fig. 6-15.-Master connecting rod used in the Wright 1820 Cyelone engine.

## Suggested Design Procedure

Important. Give references for all formulas and empirical factors used. All drawings should be on standard-size paper, and completf in all defails including dimensions, elearances, material sperifications, amb mumber required. Drawings (except as noted) should be blueprinted and properly folded (Fig. 2-4) for insertion in the design notebook. Keep a reeord of the man-hours required on each item.

1. Solect materials and make all neressary caloulations for the piston and piston pin.
2. Make a detailed drawing of the piston (at least two seretional virwsh.
3. Make a detailed drawing of the piston pin and end buttons wr equivalent parts used to hold the pin in place.).
4. Determine all necessary dimensions for the piston ringes, and sperify the S.A.F. standard size or sizes to be used.
5. a. Select materials, and make all neesesmary ealenlations for the mastor connecting rod and end bushings.
b. Same procedure for articulated rod, bushings, and link pin when used.
6. Check selected dimensions of connecting rod or rods with layout drawings (Suggested Design Procedure, page 24, item 4) to make certain of adequate clearance at all points. Alter layout drawings as necessary
7. a. Make a detailed drawing of the master connecting rod (at least two views). Show bushings in place.

- b. Same procedure for articulated rod and link pin when used.

8. Determine the weight of each of the reciprocating parts, and show in tabular form (a) name of part or item, (b) actual weight of parts, (c) weight of parts assumed in calculating bearing loads (Chap. V), (d) percentage increase or decrease of actual weights over assumed weights, (e) estimated change in maximum bearing loads due to $d,(f)$ estimated change in mean bearing loads due to $d$.

Check the new bearing loads with values given in the tables of Appendix 1. If these loads are very far outside the usual ranges of loadings, etc., alterations in the design should be made to bring them back within the ranges of proven values. These changes may be made either by altering the weights of the parts or (when possible) by using bearing materials that will withstand the increased loads. If the loads are well below the assumed values, the specific weight of the engine is apt to be unnecessarily high.
9. Make an assembly drawing of the reciprocating parts on the layout drawings of Suggested Design Procedure, page 24, item 4. Show parts in section whenever such sectioning increases the clarity or legibility of the drawing. Include only principal over-all dimensions. Identify each part of the assembly drawing by a reference number corresponding to the detailed drawing or reference number of that part. When the detailed drawing contains more than one part, identify each part by the detailed drawing number and a letter. Do not blueprint the assembly drawings at this stage.
10. When items 1 to 9 have been completed and put in proper form, submit for checking and approval.

## References

1. Alcoa Aluminum and Its Alloys, Bulletin of the Aluminum Company of America.
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12. S.A.E. "Aircraft Engine Drafting Room Practice."

## CHAPTER 7

## CRANKSHAFT VIBRATION AND BALANCE

7-1. Fundamental Nature of Vibration.-When an elastic body is subjected to a force, it deflects, and if the foree is suddenly removed, the restoring forces in the body return it to its original or neutral position. But the momentum acquired during the restoring action is such that the body passes beyond its neutral position and is deflected in the opposite direction. This in turn sets up restoring forces in the original direction of deflection, etc., so that the body oscillates or vibrates. If the original deflecting force is applied but once, the vibration gradually diminishes and finally ceases because of internal and external friction. However, if the deflecting force is applied repeatedly, the body will continue to vibrate, but the magnitude of the vibration will vary widely, depending upon the frequency of application of the deflecting force and the natural vibrating frequency of the body.

To illustrate, in Fig. 7-1 (A), $R$ represents an elastic rod rigidly supported at one end. If the free end of the roded is struck a sudden blow with the hammer $I$, the rod will defleert from its neutral position $C$ to a distorted position $D$. Buat restoring forces are set up in the rod when it is deffected so that as soon as the foree of the hammer blow is spent the rod will spring back toward its neutral position. Its inertia of motion carries it beyond $C$ to $E$, and then opposito restoring forces start it back toward $D$. This cycle or series of events will continue with gradually diminishing amplitude until the continuously opposing forces of internal and external frietion bring the rod to rest at its neutral position.
If cam $S$, Fig. 7-1 (A), is rotated, the hammer hlows will he repeated at a frequency depending upon the rate of rotation and the number of lobes on the cam. If the hammer hows occur when the vibrating rod is at $C$ and moving in direetion $M$, the vibration will obviously be damped, but if the hows are
timed to occur at $N$, the force of the blows will aid in continuing and amplifying the vibration. Such a case is sometimes called synchronous vibration, or resonance. Figure 7-1 ( $B$ ) illustrates the case for torsional vibration.

If the hammer blows occur at intermediate points between $M$ and $N$, the resulting vibration of the rod will be intermediate. If the blows occur at one-half the frequency of the rod, vibration will be damped or aided as before, but the effect will be less


Fig. 7-1.-Fundamental idea of vibration in elastic machine parts. (A) Lateral vibration and ( $B$ ) torsional vibration.
pronounced, and for one-fourth the frequency, the blows will have still less effect. Hence, as the speed of rotation of $S$ is increased from a very low to a very high value, there will be several speeds at which vibration will be aided to a greater or less degree.

If the intensity of the hammer blows is varied, the vibration of the rod will be affected accordingly. Every elastic body has a natural period of vibration, i.e., time per cycle of movement which depends upon its mass, moment of inertia (i.e., dimensions), and stiffness. If these characteristics are changed, in the case of the rods in Fig. 7-1, the speeds of $S$ at which synchronous vibration will occur will also be changed. However, blows
occurring at frequencies other than those producing synchronous vibration will produce "forced" vibrations, but these forced vibrations are small compared with the ones produced at the "critical" speeds.

If the support for the vibrating member is not absolutely fixed and rigid, it will also vibrate. Thus the rods in Fig. 7-1 can produce vibrations in their supports.

By applying the foregoing principles to airplane engines, the hammer blows correspond to the varying gas and inertia forees and the crankshaft corresponds to the vibrating rod. The crankshaft is more complex than a simple rod, and its natural periods of vibration are harder to predict, but the basic idea is the same. In other words, at certain speeds, the varying forces occur at such a rate that vibration is greatly amplified. It is at these speeds that the engine is said to be "rough," and if they occur at the desired or usual speeds of operation, the engine is unsatisfactory. If the engine is operated for prolonged periods at a speed at which synchronous vibration occurs, some of the parts, usually the crankshaft, may fail owing to the increasing amplitude of the vibrations deflecting the parts beyond their fatigue strength. Thus a crankshaft can fail structurally even though it is many times stronger than the elementary formulas of mechanics would indicate as necessary.

7-2. Engine Balance.-In approaching the problem of deciding upon proper dimensions for the crankshaft, it is advisable first to consider the major causes of vibration. They are as follows:

1. Variation in engine torque.
2. Flexibility of the crankshaft, in torsion.
3. Unhalanced rotating parts.*
4. Unbalanced reciprocating parts.*

In considering these items, it is important, to distinguish between (a) vibration of the engine structure as a whole and (b) vibration of individual parts of the structure.

7-3. Variation in Engine Torque.-Variation in engine torque (Chap. 4) causes a corresponding variation in torfue reartion, i.e., piston side thrust (Fig. 4-10). This is an example of case $a$, Par. $7-2$, and tends to rock the engine in the plane of rotation of the crank arms, the magnitude of the effect being largely

[^6]dependent upon the ratio of maximum to mean torque in the engine (Figs. 4-15 and 4-16). This ratio varies with cylinder arrangement, but in general, it decreases with increase in the number of cylinders. There is no practical way to counterbalance this reaction-torque vibration, but rubber mountings and other devices are frequently incorporated to reduce the transmission of the rocking or vibration to the vehicle in which the engine is mounted.

7-4. Flexibility of the Crankshaft in Torsion.-At the other end of the connecting rod, the variation in torque sets up torsional oscillations in the crankshaft (item 2, Par. 7-2), which, owing to the large moment of inertia of the propeller, act in a manner similar to that of the supported rod in Fig. 7-1 (B). When these varying torque impulses occur at a frequency corresponding to the natural torsional frequency of the crankshaft, serious torsional vibration can occur if means for damping the oscillations are not provided. Torsional-vibration dampers as used on automotive engines ${ }^{3}$ consist usually of friction disks attached to the end of the crankshaft and so mounted that they rotate with the shaft, but their inertia effect is such that they slide when torsional vibration occurs. The resulting friction between the disks and their supporting collar on the shaft tends to damp the torsional vibration quickly.

In aircraft engines, where the useful speed range is much less than in automotive power plants, it is usually possible to avoid the most troublesome critical torsional speeds by designing the shaft so that it does not have a natural period of severe vibration within the desired operating range. From detailed dimensions and other data, it is possible to predict with reasonable accuracy the shaft speed at which serious torsional vibrations will occur, but the calculations are long and somewhat complicated. ${ }^{15,20}$ However, a crankshaft has many characteristics in common with the torsional pendulum, and a knowledge of the factors contributing to the natural period of such a pendulum will aid in the intelligent selection of shaft dimensions.

The expression for the time for one complete oscillation or cycle of a torsion pendulum is ${ }^{8}$

$$
\begin{equation*}
t=2 \pi \sqrt{ } / \frac{W k^{2} \theta}{T g} \tag{7-1}
\end{equation*}
$$

where $t=$ time per cycle, sec.
$W=$ weight of the mass at the end of the pendulum (corresponds approximately* to the crank arm and counterweight masses in an airplane engine), lb.
$k=$ radius of gyration (of the crank arm and counterweight masses approximately*).
$\theta=$ angular displacement of the weight $W$ from the neutral or static position at which it is held by the rod.
$T=$ torque exerted by the pendulum rod on the weight $W$ when it is displaced through the angle $\theta$.
$g=$ acceleration of gravity.
The twisting moment or torque in the pendulum rod is

$$
T=S_{s} \frac{J}{r}
$$

where $S_{s}=$ torsional stress in the rod.
$J=$ polar moment of inertia of the rod.
$r=$ radial distance to the outer fiber of the rod.
But

$$
S_{s}=\frac{E_{\hbar} r \cdot}{L}
$$

where $E_{s}=$ modulus of rigidity or modulus of elasticity in torsion ( $=$ about $12,000,000 \mathrm{lb}$. per sca. in. for steel).
$L=$ length of the pendulum rod.
$r$ and $\theta$ are as above.
Hence

$$
T=\frac{E_{\mathrm{a}} \cdot J \theta}{L}
$$

and substituting this in E(1. (7-1)

$$
\begin{equation*}
t=2 \pi \sqrt{\frac{W k^{2} L}{E_{s} J g}} \tag{7-2}
\end{equation*}
$$

The frequency of vibration is the reciprocal of the time, hence

[^7]\[

$$
\begin{equation*}
f=\frac{1}{t}=\frac{1}{2 \pi} \sqrt{\frac{E_{s} J g}{W k^{2} L}} \tag{7-3}
\end{equation*}
$$

\]

where $f=$ number of vibrations per second and all other symbols are as above.
If the frequency is expressed in vibrations per minute,

$$
\begin{equation*}
N=60 f=\frac{30}{\pi} \sqrt{\frac{E_{s} J g}{W k^{2} L}} \tag{7-4}
\end{equation*}
$$

where $N=$ number of vibrations per minute and all other symbols are as above.
For steel, if $g$ is in inches per second per second, Eq. (7-4) may be expressed as

$$
\begin{equation*}
N=647,500 \sqrt{\frac{J}{W k^{2} L}} \tag{7-5}
\end{equation*}
$$

where $N=$ number of vibrations per minute.
$J=$ polar moment of inertia of the pendulum shaft or rod, in. ${ }^{4}$
$L=$ length of the shaft or rod, in.
$W=$ weight of the mass corresponding to the crank arms and counterweights, lb.
$k=$ radius of gyration of the weight $W$, in.
The crankshaft is considerably more complex than the torsional pendulum, but it acts in much the same way. Hence its natural frequency of torsional vibration varies (a) as the square root of the polar moment of inertia of the shaft section, (b) inversely as the square root of the weight of crank arms and counterweights, (c) inversely as the radius of gyration of its crank arms and counterweights, and (d) inversely as the square root of its length.

Referring again to Fig. 7-1 (B), if cam $S$ was rotated at such a speed that a blow was struck by the hammer every time the rod arm passed point $C$ in direction $N$, severe $\dot{\text { vibration would result. }}$ If the cam were slowed down to where the hammer struck a blow every other time the arm passed $C$ in direction $N$, vibration would again occur, but it would be less severe because the natural damping forces would have more time to act between blows. Similarly, as the speed of cam $S$ was further decreased, still less severe vibrating periods would be encountered. The net
result would be that within a sufficiently large range of cam speed there would be a series of speeds at which vibration would occur, and at each succeeding lower critical speed the vibration would


Fig. 7-2.-For descripitive legend see opposite page.
be less severe. Figure 7-2 indicates the severity of stresises (proportional to ratio of actual torque to gas torque) that have been found to exist in radial engines.

In crankshafts, study of these critical speeds is termed harmonic analysis, because it can be demonstrated mathematically that they can be represented by a constant mean value and a series of harmonics or sine-curve functions, i.e., a Fourier series. Analysis by this means ${ }^{3,10}$ is beyond consideration here, but it should be noted that the most severe vibrations occur at the higher speeds, and that by suitable design the worst critical speeds can usually be made to occur above the maximum speed at which

(C)

Fig. 7-2.-Effect on crankshaft torsional stresses due to resonant or critical speeds. (A) Effect of resonance on the amplitude of torsional vibration-in a nine-cylinder radial engine. (B) (1) Torque acting on crankshaft and (2) torque in crankshaft at a resonant speed in a nine-cylinder radial engine. (From S. A. E. Jour., Vol. 38, No. 3). (C) (1), (2) Observed actual torque and (3), (4) and (5) torque due to gas pressure in a radial-engine crankshaft. (From Judge, "Automobile and Aircraft Engines.")
the engine is to be operated. Inspection of Eq. (7-5) indicates that the crankshaft may be designed against severe torsional vibration by increasing the polar moment of inertia of the shaft cross section, decreasing the weight of crank arms, eliminating or reducing the size of counterweights, reducing the radius of gyration of crank arms and counterweights, and using as short a crankshaft length as possible. Since $J / L$ is a measure of the stiffness of the crankshaft and $W k^{2}$ is the moment of inertia of crank arms and counterweights, it follows that the crankshaft should be as stiff as possible and have a low moment of inertia of its crank arms and counterweights. Stiffness may be increased
without increase in weight by using hollow crankpins and journals. Chamfering and rounding of crank arms (Fig. 5-15) and elimination of counterweights wherever possible will contribute to reducing the moment of inertia.

An alternate method of reducing torsional vibration in radial engines that has been found to be very effective is the pendulum type of vibration absorber. ${ }^{11}$ It can be demonstrated that by mounting a pendulous weight of suitable proportions opposite the crank arms, practically complete damping of torsional vibration can be had. Since radial engines require counterweights for proper balance, and since it is possible also to use these counterweights for the pendulum mass, practically complete elimination of torsional vibration may be attained without adding any dead weight to the engine. The device has so far found its greatest application in very high-powered engines where the crankshaft is already highly stressed and any additional vibration stresses become very critical.

7-5. Types of Crankshaft Balance.-Before considering the effects of unbalanced rotating and unbalanced reciprocating parts (items 3 and 4, Par. 7-2), it is advisable to fix clearly in mind the three types of crankshaft balance. They are ${ }^{2}$

1. Static balance.
2. Dynamic balance.
3. Deflection balance.

Considering these items in order, static balance is that condition in the crankshaft in which the algebraic sum of all moments of radial forces about the axis of support is zero. An example of this condition is illustrated in Fig. 7-3 ( $A$ ) in which the shaft is supported by the bearings $M$ and $N$. Obviously the shaft will remain in any position since $2 W \times R=W \times 2 /$, and the lever arms decrease in the same proportion for any angular position of the shaft to the condition shown in the figure.

The conditions for dynamic balance require that the algebraic sum of all moments of radial forces about an axis perpendicular to the axis of support must be equal to zero. Shaft (A), Fig. 7-3, will not meet this condition, for; during rotation, the centrifugal forces on the weights will produce a rotating couple that ran be balanced only by reaction forees at the bearing supports $M$ and $N$. In Fig. 7-3 (B), however, the shaft is in dynamic balance, as the taking of moments about either $M$ or $N$ will show. Thus
taking moments about $M$,

$$
5 F_{N}=2 F(2+1)-(2 F+4 F)=0
$$

To attain dynamic balance, a shaft must also be in static balance.
Deflection balance requires that there be no deflection of the shaft due to the centrifugal loads produced by the weights. Shaft ( $B$ ), Fig. 7-3, when rotating, will be deflected as shown by the dashed curve (exaggerated). Obviously, deflection balance can be attained only when all forces are balanced by equal forces in their respective planes of rotation. Extreme deflection unbalance tends to produce high localized bearing pressures even though the shaft is dynamically balanced. This is due to distortion of the journals.

Static balance in an aircraftengine crankshaft is necessary to satisfactory operation as, obviously, its absence would produce severe shaking (vibration) that could not be tolerated. Engineshaving only one crank throw, i.e., single-bank radials, must have counterbalanced crankshafts to attain static balance. Multithrow crankshafts in practically all cases have the cranks symmetrically spaced about


Fig. 7-3.-Three types of balance in engine crankshafts. (Adapted from Huebotter, "Mechanics of the Gasoline Engine.' ${ }^{\prime \prime}$ ) the crankshaft axis." Hence they are in inherent static balance if properly constructed.

Dynamic balance requires the use of counterweights on multithrow as well as single-throw crankshafts. Nearly all modern automotive and aircraft engines are dynamically balanced, but counterweights on in-line and V-aircraft engines are not altogether desirable because ( $a$ ) the added weight of counterbalancing is undesirable and (b) the added rotating mass contributes to lowering the severe torsional vibration periods into the useful speed range of the engine [Eq. (7-5)].

Complete deflection balance is impossible in conventional types of engines as the counterweights would have to be in the plane of the connecting rods and hence would not permit the necessary mechanical clearance. However; deflection balance can be closely approached by placing the counterweights as near the plane of the connecting rods as proper mechanical clearance will permit.

7-6. Unbalanced Rotating Parts.-The balance of rotating partis (item 3, Par. 7-2) is a relatively simple matter in conventional types of engines as it consists merely in providing counterweights on the opposite side of the axis of rotation to the unbalanced parts. In the case of an unbalanced crank throw, the weight or weights cannot be placed directly opposite the center of the crankpin, but a weight can be attached to each crank arm and so near the plane of rotation of the crankpin center that deflection unbalance is quite small.

The centrifugal force due to an unbalanced rotating mass [Eq. (5-1)], is a function of the weight of the unbalanced mass and the distance from the axis of rotation to its center of gravity. Obviously, a counterweight or counterweights located on the opposite side of the axis of rotation from the rotating mass to be balanced and having a weight and moment arm such that the product will equal the product of the unbalanced weight and its moment arm will balance the system. In aircraft engines, it is desirable to place the counterweights as far from the center of rotation as crankcase clearance and other limitations will permit, as this will avoid the use of unnecessary dead weight in the engine.

7-7. Unbalanced Reciprocating Parts.-In the development of the expression for reciprocating inertia force [ $\mathrm{E}(\mathrm{q} .(4-8)]$, it was shown that

$$
\begin{equation*}
F_{I n}^{\prime}=0.000028+N^{2} W R(\cos \theta+Z \cos 2 \theta) \tag{7-i}
\end{equation*}
$$

where $F_{R}=$ reciprocating inertia force, lb.
$N=$ r.p.m. of the crankshaft.
$W=$ weight of reciprocating parts, ith.
$R=$ crank radius, in.
$\theta=$ the angular displacement of the erankshalt from the dead center, deg.
$Z=R / L$.
$L=$ the center-to-center length of the commerting rol, in.

This force acts along the cylinder center line, and its reaction tends to (a) distort the crankshaft and (b) move the supports for the crankshaft, i.e., shake the engine. The amount of this shaking or vibration varies with the number and arrangement of the cylinders, and when favorable conditions exist, i.e., these shaking forces vary at a frequency at or near the natural period of vibration of the engine or its supports, serious vibration can occur. Hence, it is advisable to investigate these forces with a view to balancing them by suitable counterweights or other means.


Fic. 7-4.-Primary, secondary, and resultant reciprocating inertia forces for a $41 / 2$ - by $53 / 8-\mathrm{in}$. 2,000-r.p.m., single-cylinder engine having a weight of reciprocating parts equal to 4 lb .

For this purpose, Eq. (7-6) may be divided in to two terms, i.e.,

$$
\begin{equation*}
F_{R}=0.0000284 N^{2} W R \cos \theta+0.0000284 N^{2} W R Z \cos 2 \theta \tag{7-7}
\end{equation*}
$$

The first term in this expression is usually called the primary reciprocating inertia force, and the second is called the secondary reciprocating inertia force. They are also called the first and second harmonics since, if plotted against crank angle, they will form cosine curves* (Fig. 7-4).

Inspection of the primary force in Eq. (7-7) and comparison with Eq. (5-1) shows that the two are the same except for the value of $W$ and the factor $\cos \theta$. This suggests a logical approach to balancing the primary reciprocating inertia force by attaching a counterweight opposite the crankpin such that its centrifugal force will balance the primary reciprocating inertia force. Such a procedure makes possible, for a single-cylinder engine, complete

[^8]balance of the primary fore at the 0 - and $18(0)$-deg. positions where $\cos \theta$ equals 1 , but at the $90-$ and 270 -deg. positions the primary reciprocating inertia force is zero
$$
(\cos 90 \text { and } \cos 270=0)
$$
whereas the centrifugal force on the counterweight is the same as for the 0 - and 180-deg. positions. Obviously, completely balancing the maximum primary reciprocating inertia force by a rotating counterweight on the crankshaft merely shifts the unbalance from the plane of the cylinder axis to a plane normal to this axis. This is illustrated in Fig. $7-5$ where $F_{R L}$ represents the primary reciprocating inertia force which always acts along the center line of the cylinder, $F_{c}$ is the centrifugal force


Frg. 7-5.-Counterweight method of balancing the primary reciprocating inertia - force in a single-cylinder exgine.
on the primary counterbalancing weight, $F_{B F}$ is the component of $F_{c}$ which opposes, i.e., balances, $F_{t t^{\prime}}$, and $F_{r}$ is the unhalanced transverse force component of $F_{r}$. Use of a counterweight that will balance one-half of the primary reciprocating incertia foree is about the best compromise, as this will give forees parallel and normal to the cylinder axis of the single-crolinder engine which are each one-half of the magnitude of the initial primary reciprocating unbalance.

Several other means have been tried for balancing the primary force in a single-cylinder engine, but they require more or less modification of the simple and conventional crank chain and are not commonly used in aircraft engines. For a discussion of these methods, the student should consult references 1 and 9.

The secondary reciprocating inertia forecs, as is indicated in Eq. (7-7) and Fig. 7-4, vary at twice crankshaft speed. Hence, they cannot be balanced by a counterweight rigidly attached to the crankshaft. Fortunately, the secondary unbalance is
much less than the primary unbalance, the relative magnitude depending upon the $L / R$ ratio. As a rule, no attempt is made to balance the secondary forces in a single-cylinder engine, but the Lanchester balancer ${ }^{3}$ has been used to some extent on fourcylinder in-line automotive engines.

Equation (7-6) does not precisely represent the reciprocating inertia forces, as in its derivation (Pars. 4-2 and 4-5) the smaller


Fig. 7-6.-Various arrangements of two-cylinder engines.
terms were neglected. These smaller terms are functions of $\theta$ and $R / L$, and each succeeding term may be represented by a cosine curve of higher frequency and less magnitude. These higher harmonics produce minor shaking forces or vibrations, but due to their small magnitude, they are generally neglected.

7-8. Reciprocating Balance in Multicylinder Engines. 1. The Two-cylinder In-line Engine.-In a multicylinder engine, each cylinder when considered separately will produce shaking forces in the same way as in a single-cylinder engine, but by suitably arranging the different cylinders and the angular relations of the crank arms, part or all of the unbalance in the engine
as a whole may be eliminated. In the two-cylinder in-line engine [Fig. 7-6 (A)], the crank arms are at an angular relation of 180 deg. ; hence, when one piston is moving down the other is moving up. This displaces the primary reciprocating forecs at 180 deg . and, as will be seen in Fig. 7-7, the resultant primary unbalance


Frg. 7-7.-Construction showing that the primary reriprocating incria forces are balanced in a two-eylinder engine having a rank arrangement as in Fig. 7-l; (A). $4 \frac{1}{2}-$ by $5 \frac{3}{8}-\mathrm{in}$. cylinder, 2,000 r.p.m., 4 ll . reciprocating woight.


Fig. 7-8.- Construction showingthat the secondary reciprocating incotiat foress are not balanced in a two-eylinder engime having a crank arrangement as in Fig. 7-6 (A). 41, 2 by $5^{3}$-in. eylinder, 2,000 r.p,me, 4 if. reriprocating watht. Amount of maximum unbalance is $2 \times$ maximum unhalance for one exlinder.
for the engine is zero. This means that the engine will not, tend to move up and down in the plane of the crlinders beranse of primary unbalance. However, cach eylimder haken separately still has primary unbalance, and as these unbalanerd forers in the different eylinders do not, art along the same line, they will produce a rocking couple which tends to oseillate the engine about an axis normal to the plane of the exinders. The magnitude of this couple depends upon the magnitude of the primary untalane
in each individual cylinder and the distance between the center lines of the cylinders, i.e., distance $S$; Fig. 7-6 (A). Obviously an engine of this type should have its cylinder center lines as close together as other limitations will permit.

The secondary reciprocating inertia forces of the engine in Fig. 7-6 (A) will also be displaced 180 deg., but upon combining them graphically (Fig. 7-8) it is seen that they do not cancel.


Fig. 7-9.-Construction showing that the primary reciprocating inertia forces give a constant radial rotating force in a 90 -deg., single-crank, two-cylinder V-engine, Fig. 7-6 (B). $4 \frac{1}{2}-$ by $53 / 8$-in. cylinder, $2 ; 000$ r.p.m., 4 lb . reciprocating weight per cylinder.

Hence, the secondary forces in this type of engine are not balanced, and as will be seen from the figure, the maximum secondary unbalance is twice that for one of the cylinders.
2. The Two-cylinder Single-crank $V$-engine.-By arranging the engine as in Fig. 7-6 ( $B$ ), the unbalanced reciprocating forces due to each cylinder act at an angle $\alpha$ to one another. The resultant unbalance may be determined by adding them vectorially (Figs. 7-9 and 7-10). An example of primary unbalance determination is shown in Fig. 7-9 in which it is seen that the resultant
primary unbalance is a constant radial force that rotates with the crankshaft. For a $90-\mathrm{deg}$ : V-engine, this primary unbalance is equal to the maximum primary unbalance for one of the cylinders taken separately. Obviously, since the primary unbalance of the engine in Fig. 7-6 (B) is constant and rotates with the crankshaft, it may be balanced by a suitable counterweight attached opposite the crank arm.

An example of secondary unbalance determination for the engine in Fig. 7-6 ( $B$ ) is shown in Fig. 7-10. The resultant is a


Fig. 7-10.-Construction showing that the secondary reciprocating inertia forces in a $90-\mathrm{deg}$, single-crank, two-cylinder V-engine, Fig. 7 -fj (B) embine to form a transverse resultant force that varies at twice crankshaft speed. 412 -hy $53 / 8-\mathrm{in}$. cylinder, $2,000 \mathrm{r} . \mathrm{p} . \mathrm{m} ., 4 \mathrm{ib}$. reciprocating weight per eylinder.
transverse force which varies at twice crankshaft speed and has a value for a $90-\mathrm{deg}$. V-engine of

$$
F_{s R}=\sqrt{F_{M s_{1}}^{2}+\sqrt{F_{R s_{2}}^{2}}}
$$

where $F_{S R}=$ secondary resultant foree.
$F_{R S_{1}}=$ secondary force in cylinder 1.
$F_{R S_{2}}=$ secondary force in cylinder 2.
3. The Two-cylinder Opposed Engine. - In this type of engine, the pistons always move in opposite directions; hence the primary forces in one cylinder cancel these forces in the other cylinder. The secondary forces also cancel as will be seen from Fig. 7-11, but for the conventional crankshaft-cylinder arrangement shown in Fig. 7-6 (C), there will be a rocking couple which tends to oscillate the engine in the plane of the cylinder center lines. This
couple is proportional to the distance $S$ between the cylinder center lines; hence, as in the case of the two-cylinder in-line engine [Fig. 7-6 ( $A$ )], it is desirable to have these center lines as close together as possible. When this distance $S$ is small, the twocylinder opposed engine is a rather satisfactory type for small inexpensive light planes.
4. The Three-cylinder In-line Engine.-In this type of engine (Fig. $\cdot 7-12$ ), the crank arms are at an angle of 120 deg . The


Fig. 7-11.-Construction showing that the secondary reciprocating inertia forces are balanced in a two-cylinder engine having a crank arrangement as in Fig. 7-6 (C). $41 / 2$ - by $53 / 8$-in. cylinder, 2,000 r.p.m., 4 lb . reciprocating weight per cylinder.


Fig. 7-12.-Crank arm arrangement for the three-cylinder in-line engine.
cylinder axes are all in the same plane, however, and a graphical determination of the degree of unbalance may be made by shifting the primary and secondary reciprocating inertia force curves through an angle of 120 deg . and then combining them. This has been done (Figs. 7-13 and 7-14), and from these diagrams it is seen that both the primary and secondary reciprocating inertia force resultants are zero. Hence, the three-cylinder in-line engine is balanced, but rocking couples still exist which tend to oscillate the engine about an axis normal to the plane of the cylinders.

The magnitude of these rocking couples can be reduced by placing the center lines of the cylinders as close together as possible.
5. The Four-cylinder In-line Engine.-This arrangement usually consists of two two-cylinder engines [Fig. 7-6 (A)], with the crank arms arranged so that the two inner cranks are parallel


Frg. 7-13.-Construction showing that the primary reciprocating inertia forces in a three-cylinder in-line engine arranged as in Fig. 7-12 are balanced. 4ty-by $53 / 8-\mathrm{in}$. cylinder, $2,000 \mathrm{f} \cdot \mathrm{p} . \mathrm{m} ., 4 \mathrm{lb}$. reciprocating weight per eylinder.


Fig. 7-14. Construetion showing that the serondary recionocating incraia forces are balanced in a three-cylinder in-line engint arranged as in Fig. $7-12$.

and extend in the same direction and the two outer ranks are parallel and at an angle of 180 deg. to the inner cranks. Such an arrangement will have the same balance characteristies as the two-cylinder in-line engine, and in addition the rocking couples will cancel. It should be noted, however, that the unbalanced secondary forees in the four-cylinder in-line engine will sum up to twice the magnitude of the two-evlinder engine of the same size cylinders, reciprocating weights, etc.

This unbalanced secondary force is of sufficient magnitude in the four-cylinder in-line engine to cause appreciable vibration, especially at synchronous speeds, and considerable attention has been directed toward effectively counteracting it. For this purpose, the Lanchester balancer or antivibrator has proved effective, but for aircraft engines, the added weight is objectionable.


Fig. 7-15.-Conventional crank-arm arrangement in the six-cylinder in-line engine.
6. The Six-cylinder In-line Engine.-The usual crank arrangement for this type of engine (Fig. 7-15) is such that it consists of two three-cylinder engine crankshafts arranged so that crank arms 1 and 6, 2 and 5, and 3 and 4 are parallel and extend in


Fig. 7-16.-Conventional crank-arm arrangement in the cight-cylinder V-engine. the same directions, respectively. Hence, the primary and secondary forces are balanced and the rocking couples cancel.* The six-cylinder in-line engine is smooth and quite free from vibration due to reciprocating parts. $\dagger$

Since the twelve-cylinder V-engine is essentially two six-cylinder in-line engines attached to the same crankshaft, it is also inherently free from vibration due to reciprocating parts.
7. The Eight-cylinder V-engine.-Eight-cylinder V-engine crankshafts may be arranged either in one plane (the same as four-cylinder in-line engine shafts) or preferably in two planes (Fig. 7-16). With the one-plane arrangement, forging and other construction problems are simplified, but the secondary forces are not balanced. The magnitude of the unbalance depends upon the angle of the $V,{ }^{3}$ the minimum severity being at an angle of 60 deg., but this gives unequal firing intervals.

It was noted in Par. 7-8, item 2, that the primary forces in a two-cylinder V-engine could be balanced by means of a rotating

* See footnote $\ddagger$ of Table 7-1.
$\dagger$ The sixth harmonics are not balanced, but the magnitude of the unbalance is so small that it is negligible, see reference 9 .
weight attached opposite the crank arm, and since the eightcylinder V-engine may be considered as four two-cylinder V -engines, it is apparent that primary reciprocating inertia forces may be balanced by means of suitable counterweights.

From Fig. 7-10, it was observed that the secondary forces in a 90-deg. two-cylinder V-engine combine to form a transverse


Fig. 7-17.-Construction showing that the primary reciprocating inertia forces in a three-cylinder single-crank radial engine have a constant resultant, that acts outward along the crank-arm center line. $41 / 2-$ by $53 / 8-i n$. cylinders, 2,000 r.p.m., 4 lb . reciprocating weight per cylinder.
force having a period twice crankshaft speed. With the crank arrangement shown in Fig. 7-16, this force at crank 1 is opposite in direction to the secondary force at crank 4. Therefore the secondary forces at these two cranks will cancel. Similarly, the secondary forces at cranks 2 and 3 will cancel, and the engine will have inherent secondary reciprocating balance. Also the rocking couples will cancel; hence the eight-cylinder V-engine having a crank arrangement as in Fig. 7-16 may be made relatively free from vibration due to reciprocating inertia forees.
8. Radial Engines.-To permit even firing intervals, singlebank radial engines are built with an odd number of cylinders equally spaced around the crankshaft. The number of cylinders may be $3,5,7$, or 9 , with the latter three numbers much the more common.

Balance conditions in radial engines may be studied graphically by a procedure similar to that for the two-cylinder V-engine, but for engines of more than three cylinders, the construction becomes somewhat tedious, and analytical methods are preferable.

Figure $7-17$ shows the construction procedure for a threecylinder single-crank radial. In this figure, it is seen that the primary reciprocating inertia forces combine to form a constant rotating force that acts outwardly along the crank arm. Hence, the unbalanced primary force may be balanced by a suitable counterweight placed opposite the crank arm. Data for constructing Fig. 7-17 were taken from Fig. 7-4, and from the values shown, it is seen that the magnitude of the rotating primary unbalance is 1.5 times the maximum primary unbalance for one cylinder or one-half the maximum for all three cylinders.

This conclusion may also be reached by analytical methods, ${ }^{1}$ and the unbalance expressed as

$$
\begin{equation*}
F_{P R}=3 / 2\left(0.0000284 N^{2} W R\right) \tag{7-8}
\end{equation*}
$$

where $F_{P R}=$ resultant primary unbalanced reciprocating inertia force, lb.

$$
N=\text { r.p.m. of the crankshaft. }
$$

$W=$ reciprocating weight per cylinder, lb .
$R=$ crank radius, in.
It may also be shown by analytical methods ${ }^{1}$ that for any singlecrank radial engine having an odd number of cylinders

$$
\begin{equation*}
F_{P R}=\frac{n}{2}\left(0.0000284 N^{2} W R\right) \tag{7-9}
\end{equation*}
$$

where $n$ is the number of cylinders and all the other terms are the same as in Eq. (7-8).

By procedure similar to that used in Fig. 7-17 or by analytical methods, it may be shown that the secondary reciprocating inertia forces in a three-cylinder radial engine are one-half balanced and that the resultant secondary force rotates in the opposite direction to the crankshaft and at twice crankshaft speed. Obviously, it
is impractical to balance the secondary reciprocating incrtia forces in a three-cylinder single-crank radial engine. The secondary forces in single-crank radials of more than three cylinders are balanced, however, and this already has been demonstrated for a five-cylinder radial (see Fig. 5-8).

- 9. Summary of Reciprocating Balance.-For convenient reference, and to check the reciprocating unbalance quickly, Table 7-1 may be used. It should be borne in mind, however, that even though a multicylinder engine is inherently balanced as a whole, its reciprocating parts may be individually unbalanced and produce stresses within the engine. For instance, a six-cylinder in-line engine is inherently balanced,* but individual cylinders are not, and the reciprocating parts in these cylinders cause stresses in the crankshaft and other parts even though there is no appreciable tendency for the engine as a whole to vibrate. Hence, counterweights greater than necessary for rotating unbalance help to reduce deflection unbalance even in an engine having inherent reciprocating balance. However, for aireraft, engines, the added weight is oljectionable.

7-9. Counterbalancing.-Counterweights are attached to engine crankshafts to

1. Attain static balance of rotating parts. In in-line and V-engines, the several crank arms are usually placed symmetrically about the shaft axis so that counterweights are umeressary for static balance. However, in single-rank enginess such as radials, counterweights are necessary to attain statio balance.
2. Obtain dynamic balance. This condition is desirable as it aids in reducing bearing pressures, but, for aircraft congines, the added weight is undesirable.
3. Improve deflection balance. Placing counterwerghts as nearly opposite the crank-arm center of gravity as pessible reduces the distortion of the shaft due to centrifugal forees on the crank arm, and this in turn redures main bearing preseures.
4. Balance one-half of the primary reciprovating incria foree.

In aircraft engines, where weight is at a premium, it is dasirable to have the counterweights as small as possible, and since centrifugal force is proportional to the produrt of weight and the distance from the center of gravity of the weight to the axis of rotation, it is desirable to place the weight as far as possible from

[^9]the center of the crankshaft [see Eq. (5-1)]. The limits on this radial distance are, of course, the clearances in the crankcase, and, as an increase in crankcase dimensions will increase the weight of that part, the proper length of counterweight arms

Table 7-1.-Rectprocating Balance in Conventional Engines

| Cylinders |  | Angle between cranks | Primary forces | Secondary forces | Rocking couples | Feasible to balance |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Arrangement |  |  |  |  |  |
| 1 |  | 1 crank | Unbalanced | Unbalanced | None | One-half of primary force |
| 2 | In-line | 180 deg . | Balanced | Unbalanced | Unbalanced |  |
| 2 | Opposed | 180 deg . | Balanced | Balanced | Unbalanced |  |
| 3 | In-line | 120 deg . | Balanced | Balanced | Unbalanced |  |
| 3 | Radial* | 1 crank | One-half balanced $\dagger$ | $\begin{gathered} \text { One-half } \\ \text { balanced } \dagger \end{gathered}$ | None | Other half of primary force |
| 4 | In-line | 180 deg . | Balanced | Unbalanced | Balanced |  |
| 4 | Opposed | 180 deg . | Balanced | Balanced | Balanced |  |
| 5 | Radial* | 1 crank | $\begin{gathered} \text { One-half } \\ \text { balanced } \dagger \end{gathered}$ | Balanced | None | Other half of primary force |
| 6 | In-line | 120 deg . | Balanced | Balanced | Balanced $\ddagger$ |  |
| 7 | Radial* | 1 crank | $\begin{aligned} & \text { One-half } \\ & \text { balanced } \dagger \end{aligned}$ | Balanced | None | Other half of primary force |
| 8 | V | 180 deg . <br> 4 cranks | Balanced | Unbalanced | Balanced |  |
| 8 | V | 90 deg . | Balanced | Balanced | Balanced |  |
| 9 | Radial* | 1 crank | One-half balanced $\dagger$ | Balanced | None | Other half of primary force . |

[^10]distance from the crankshaft axis to the outermost part of the big end of the connecting rod. The shape of the weight is then made such that its center-of-gravity distance is as large as possible.

Figures 7-18 and 7-19 show some geometric shapes that give a high $W R_{G}$ product for a minimum value of weight ( $W$ ) and distance to outer fiber ( $R$ ).

Circular Sector ( $A$ )
Area $=0.01745 R^{2} \alpha$, sq. in.
Weight $=0.01745 T R^{2} \alpha d, \mathrm{lb}$.

$$
R_{G}=38.197 \frac{R \sin \alpha}{\alpha}, \mathrm{in} .
$$

$$
d=\text { density of material, lb. per cu. in. }
$$

Circular Ring Sector ( $B$ )
Area $=0.01745\left(R^{2}-r^{2}\right) \alpha$, s(in. in.
Weight $=0.01745\left(R^{2}-r^{2}\right) T d \alpha$, lh.
$R_{G}=38.197 \begin{aligned} & R^{3}-r^{3} \sin \alpha \\ & R^{2}-r^{2} \quad \alpha\end{aligned} .$.
$d=$ density of material, lb . per cu. in.
Circular Segment (C)
Area $=R^{2}(0.01745 \alpha-0.5 \sin 2(\alpha)$, sq. in. Weight $=R^{2}(() .(01745 \alpha-0.5 \sin 2 \alpha), T(d, \mathrm{Ib}$. $R_{G}=\frac{R \sin ^{3} \alpha}{0.02617 \alpha-0.75 \sin 2 \alpha,}$, in.
(C)
$d=$ density of material, lth. per cu. in.

Fig. 7-18.-Counterweight shapes having a high value of woight $\times$ distance to center of gravity ( $W R_{G}$ ) for given values of weight ( $W$ ) and distance to outer fiber ( $R$ ). (From Hueboter, "Mechanics of the (iasoline Engine.")

7-10. Example.-For an engine having the following characteristies, determine the size of counterweights neressary :

Five-cylinder single-bank radial, 4 , 2 - by 5 -in. cevlinders, 2,000 r.p.m., 4-lb. reciprocating weight per cylinder, 12-lh. rotating weight per crankpin, crank-arm details as shown in Fig. 7-20, ratio of connecting-rod length to erank radius $=4: 1$, allowable distance to outermost part of counterweight $=5.5 \mathrm{in}$.

Procedure.-From Par. 7-8, items 8 and 9, it is scen that onehalf of the primary reriprocating inertia foree is unbalanced and that it is feasible to balance this foree by means of a rotating counterweight. From Ea. (7-9), the force arting along the crank
arm due to reciprocating unbalance is

$$
F_{P R}=5 / 2\left(0.0000284 \times \overline{2,000}^{2} \times 4 \times 2.5\right)=2,840 \mathrm{lb}
$$

From Eq. (5-1), the centrifugal force due to the big end of the connecting rods (rotating weight per crankpin) is

$$
F_{C R}=0.0000284 \times 12 \times \overline{2,000}^{2} \times 2.5=3,408 \mathrm{lb}
$$



Circular Segment and Triangle (A)

Area $=A_{P}+A_{S}=L H+R^{2}(0.01745 \alpha-0.5 \sin 2 \alpha)$, sq. in. $L=\sqrt{F(2 R-F)} \quad F=R(1-\cos \alpha)$
Weight $=\left(A_{P}+A_{S}\right) T d, \mathrm{lb} . \quad d=$ density of material, lb. per cu. in. $R_{G P}=N+2 / 3 H$
$R_{G S} \quad \begin{gathered}R \sin ^{3} \alpha \\ 0.02617 \alpha-0.75 \sin 2 \alpha\end{gathered} \quad R_{G}=\frac{A_{P} R_{G P}+A_{S} R_{G S}}{A_{P}+A_{S}}$


Circular
Segment and Trapezoid (B)

$$
k-T \rightarrow 1
$$

Area $=A_{Q}+A_{S}=(M+L) H+R^{2}(0.01745 \alpha-0.5 \sin 2 \alpha)$
Weight $=\left(A_{Q}+A_{S}\right) T d \quad d=$ density of material, lb. per eu: in.
$R_{G Q}=N+\frac{H(M+2 L)}{3(M+L)} \quad R_{G}=\frac{A_{Q} R_{G Q}+A_{S} R_{G S}}{A_{Q}+A_{S}}$
$R_{G S}=\frac{R \sin ^{3} \alpha}{0.02617 \alpha-0.75 \sin 2 \alpha} \quad L=\sqrt{F(2 R-F)} \quad F=R(1-\cos \alpha)$
Fig. 7-19.-Composite counterweight shapes.
The probable easiest way of finding the centrifugal force due to the unbalanced portion of the crank arms is to separate the arms into several simple geometric shapes, determine the values for each, and add the results.

Thus, for the crankpin the volume is

$$
V_{C P}=0.785\left(\overline{2.25}^{2}-\overline{1.125}^{2}\right) 3=8.93 \mathrm{cu} . \mathrm{in} .
$$

The density of steel may be taken as 0.28 lb . per cu. in.; hence the weight of the crankpin is

$$
W_{C P}=8.93 \times 0.28=2.5 \mathrm{lb}
$$

Since the crankpin is symmetrical about the crankpin center line, the distance from the axis of rotation to the center of gravity is 2.5 in .

From Eq. (5-1) the centrifugal force on the crankpin is

$$
F_{C P}=0.0000284 \times 2.5 \times \overline{2,000}^{2} \times 2.5=710 \mathrm{lb}
$$

Calculation for weight and center of gravity of chamfered and rounded crank arms may be made by determining the weight and center of gravity of each geometric part.

A suggested procedure is to determine the weight or volume of the outer end of the crank arms beyond the crankpin center line and then take enough of the crank arms below the crankpin center line to place the center of gravity of the combined weights or volumes on the crankpin center line. The lower ends of the crank arms may be handled similarly with reference to the center line of main bearings, and then the mid-portion of the crank arms, which are usually more uniform in section, may be handled in the usual way.

Figure 7-21 is an enlarged detail sketch of the end of one of the crank arms of Fig. 7-20. In this detailed sketch, the various geometric shapes are designated by letters. For the parts above the crankpin center line, the following table ran be used:

| Name of part | Volume of part | Distance from \& to (i. (i. of part |
| :---: | :---: | :---: |
| Half cylinder. | $V_{B}=\frac{\pi S^{2} U}{2}$ | $\bar{X}_{B}=\frac{4 S}{3 \pi}$ |
| Ungula of a right circular cylinder. | $V_{e}=\frac{2}{3} R^{2} Y$ | $\bar{X}_{C}=\frac{3 \pi}{16}$ |
| Ungula of a right circular cylinder. | $V_{G^{\prime}}=\frac{2}{3} S^{\prime 2} K=\frac{2}{3} S^{3} \frac{Y}{R}$ | $\bar{X}_{r^{\prime}}=\frac{3 \pi,}{16}$ |

Hence for part $A$

$$
V_{A}=\frac{\pi R^{2} U}{n}-\frac{\pi S^{2} U}{n}-\left(\frac{2}{3} R^{2} Y-\frac{2}{3} S^{3} \frac{Y}{R}\right)
$$

and since

$$
\begin{aligned}
& V \bar{X}=\Sigma(v \bar{X}) \\
& \frac{\frac{\bar{X}_{A}}{}=}{\frac{\pi R^{2} U}{2} \times \frac{4 R}{3 \pi}-\frac{\pi S^{2} U}{2} \times \frac{4 S}{3 \pi}-\left(\frac{2}{3} R^{2} Y \times \frac{3 \pi R}{16}-\frac{2}{3} S^{3} \frac{Y}{R} \times \frac{3 \pi S}{16}\right)} \\
& \frac{\pi R^{2} U}{\pi S^{2}} \bar{U}-\left(\frac{2}{3} R^{2} Y-\frac{2}{3} S^{3} \frac{Y}{R}\right.
\end{aligned}
$$

or

$$
\bar{X}_{A}=\frac{\frac{2 R^{3} U}{3}-\frac{2 S^{3} U}{3}-\left(\frac{\pi R^{3} Y}{8}-\frac{\pi S^{4} Y}{8 R}\right)}{\pi R^{2} U-\frac{\pi S^{2} U}{2}-\frac{2}{3} Y\left(R^{2}-\frac{S^{3}}{R}\right)}
$$

Below the center line, the volume $V_{D}$ is

$$
V_{D}=V U S-\frac{\pi S^{2} U}{2}
$$

and the distance from the $\pm$ to the center of gravity is

$$
\bar{X}_{D}=\frac{\frac{V U S^{2}}{2}-\frac{2 S^{3} U}{3}}{V U S-\frac{\pi S^{2} U}{2}}
$$

If we allow the remaining volume $V_{F}$ to be such that

$$
V_{F} \bar{X}_{F}=V_{A} \bar{X}_{A}-V_{D} \bar{X}_{D}
$$

the center of gravity of $V_{A}+V_{D}+V_{F}$ will fall on the center line of the crankpin.

Using values from Fig. 7-20, the volume above the center of gravity of the crankpin is

$$
\begin{aligned}
& \begin{array}{l}
V_{A}=\frac{\pi \times \overline{1.75}}{}{ }^{2} \times 1.25 \\
2
\end{array} \frac{\pi \times \overline{0.5625}^{2} \times 1.25}{2} \\
& \\
& V_{A}=3.93 \mathrm{cu} . \mathrm{in} .
\end{aligned}
$$

The distance to the center of gravity is

$$
\frac{2 \times \overline{1.75} \times 1.25}{3}-\frac{2 \times \overline{0.5625^{3} \times 1.25}}{3}
$$

$\bar{X}_{A}=$

$$
\pi\left(1.25-\underline{0.5)}\left(\overline{1.75^{3}}-\frac{\overline{0.5625^{4}}}{1.75}\right)\right.
$$

$\bar{X}_{A}=0.7 \mathrm{in}$.


Fig. 7-20.-Crank-arm details for the example of Par. 7-10.
Below the crankpin center line,

$$
\begin{aligned}
& V_{D}=3.5 \times 1.25 \times 0.5625-\frac{\pi \times 0.5625^{2} \times 1.25}{2} \\
& V_{D}=1.839 \mathrm{cu} . \mathrm{in} .
\end{aligned}
$$

The distance to the center of gravity is

$$
\begin{align*}
\bar{X}_{D} & =\frac{3.5 \times 1.25 \times 0.5(625}{}{ }^{2} \\
2 & \frac{2 \times 0.56 \overline{525}^{3}}{3} \times 1.25 \\
\bar{X}_{D}= & 0.296 \mathrm{in} .
\end{align*}
$$

To place the center of gravity of the combined volumes on the center line of the crankpin,

$$
V_{F} \bar{X}_{W}=3.93 \times 0.7-(1.839 \times 0.299(\mathrm{j})=2.207
$$

From the detailed figure,

$$
V_{F}=V U Z=3.5 \times 1.25 \times Z=4.375 Z \mathrm{cu} . \mathrm{in} .
$$

and

$$
\bar{X}_{F}=S+\frac{Z}{2}=0.5625+\frac{Z}{2}
$$

hence

$$
4.375 Z\left(0.5625+\frac{Z}{2}\right)=2.207
$$

or

$$
Z=0.6 \mathrm{in}
$$

Therefore,

$$
V_{F}=4.375 \times 0.6=2.63 \mathrm{cu} . \mathrm{in} .
$$

and

$$
\bar{X}_{F}=0.83 \mathrm{in} .
$$

This still leaves $2.5-(S+Z)=2.5-(0.5625+0.6)=1.33$ in. of the crank arm and the part on the opposite side of the axis of rotation to be considered, but before calculating the effect of these parts, the centrifugal force on the upper part of the crank arms will be determined.

The weight of the several volumes found above is (for both crank arms)

$$
\begin{aligned}
& W_{C A}=2\left(V_{A}+V_{D}+V_{F}\right) d \\
& =2(3.93+1.839+2.63) 0.28 \\
& =4.7 \mathrm{lb}
\end{aligned}
$$



Fig. 7-21.-Enlarged detailed arrangement of the outer end of the crank arms in Fig. 7-20.
and the distance to the center of gravity from the axis of rotation is equal to crank radius, i.e., 2.5 in . Hence, the centrifugal force on the upper end of the crank arms is

$$
F_{C A}=0.0000284 \times 4.7 \times 2,000^{2} \times 2.5=1,335 \mathrm{lb}
$$

The remainder of the crank arms, i.e., the parts extending from the center of rotation out a distance of 1.33 in . may be handled in much the same way as for other parts, but inasmuch as it will be necessary to extend the arms on the other side of the axis of rotation far enough to reach the counterweights, it is probable that most of the remaining part of the crank arms will be balanced. In fact, it is a convenient preliminary assumption (for the example being considered here) to let the point of attach-
ment for the counterweights be $1.33+J$ in. from the axis of rotation. This eliminates the inner 1.33 in . of the arms from the unbalance calculations, and the total force to be balanced is

$$
\begin{array}{r}
F_{P R}+F_{C R}+F_{C P}+F_{C A}=2,840+3,408+710+1,335 \\
=8,293 \mathrm{lb}
\end{array}
$$

The detailed shapes of counterweights to balance this foree are largely a matter of individual preference; it should be kept in mind, of course, that minimum weight and adequate clearance are important items. Hence, for the purpose of the example, assume that counterweight shapes like Fig. 7-19 ( $B$ ) are to be used. Further, assume that they are to be attached a distance $(J)$ beyond the balanced portion of the crank arms of 2 in . The balancing effect of these 2 in . of extended crank arms is found as follows:

The volume for both arms is

$$
V_{w X}=3.5 \times 1.25 \times 2 \times 2=17.5 \mathrm{cu} . \mathrm{in}
$$

The weight of the extended crank arms is

$$
W_{E X}=17.5 \times 0.28=4.9 \mathrm{lb}
$$

The distance from the axis of rotation to the center of gravity is

$$
\bar{X}_{E x}=1.33+1=2.33 \mathrm{in}
$$

and the centrifugal force is

$$
F_{E X}=0.0000284 \times 4.9 \times \overline{2,000}^{2} \times 2.33=1,295 \mathrm{lb}
$$

Hence the net force to be balanced by counterweights is

$$
F_{N}=8,293-1,295=6,998 \mathrm{lb}
$$

Referring to Fig. 7-19 (B), let $\alpha=40$ deg., $M=3.5 / 2=1.75 \mathrm{in}$, and $R=5.5 \mathrm{in}$. Then

$$
\begin{aligned}
& F=R(1-\cos \alpha)=5.5(1-0.7(6()=1.29 \mathrm{in} . \\
& L=\sqrt{F\left(2 R-F^{\prime}\right)}=\sqrt{1.29(2 \times 5.5-1.29)=3.51 \mathrm{in} .} \\
& N=1.33+2=3.33 \mathrm{in} . \\
& H=R-(F+N)=5.5-(1.29+3.33)=0.88 \mathrm{in} .
\end{aligned}
$$

The area of the trapezoidal part of the counterweight is [from the data of Fig. 7-19 (B)]

$$
A_{Q}=(M+L) H=(1.75+3.54) 0.88=4.65 \text { sq. in. }
$$

The area of the circular segment is

$$
\begin{aligned}
& A_{S}=R^{2}(0.01745 \alpha-0.5 \sin 2 \alpha) \\
&=\overline{5.5}^{2}(0.01745 \times 40-0.5 \sin 80)=6.24 \mathrm{sq} . \mathrm{in}
\end{aligned}
$$

The total area is

$$
A_{Q}+A_{s}=4.65+6.24=10.89 \text { sq. in. }
$$

The radial distance to the center of gravity of the trapezoid is

$$
R_{G Q}=N+\frac{H(M+2 L)}{3(M+L)}=3.33+\frac{0.88(1.75+2 \times 3.54)}{3(1.75+3.54)}=3.82 \mathrm{in} .
$$

The radial distance to the center of gravity of the circular segment is

$$
\begin{aligned}
& R_{G S}=\frac{R \sin ^{3} \alpha}{0.02617 \alpha-0.75 \sin 2 \alpha} \\
& 5.5 \times 0.6428^{3} \\
& 0.02617 \times 40-0.75 \times 0.9848=4.72 \mathrm{in} .
\end{aligned}
$$

The radial distance to the center of gravity of the combined area is

$$
R_{G}=\frac{A_{Q} R_{G Q}+A_{S} R_{G S}}{A_{Q}+A_{s}}=\frac{4.65 \times 3.82+6.24 \times 4.72}{4.65+6.24}=4.345 \mathrm{in} .
$$

The thickness of the counterweights may now be found as follows:

Let

$$
F_{c w}=6,998 \mathrm{lb} .\left(=F_{N}\right)
$$

Then, the necessary weight of the counterweights is

$$
W_{c w}=\frac{F_{c i v}}{0.000028+N^{2} R_{G}}-\frac{6,998}{0.0000284 \times 2,000^{2} \times 4.345}=14.17 \mathrm{lb}
$$

Since this weight is divided equally between the two crank arms, for a density of the steel of 0.28 lb . per cu. in., the thickness of cach counterweight is

$$
T=\frac{W_{\text {cw }}}{2\left(A_{Q}+A_{s}\right) d}-\frac{14.17}{2 \times 10.89 \times 0.28}=2.32 \mathrm{in} .
$$

For this thickness of counterweights, from Fig. 7-20, it is seen that the space between the weights for passage of the connecting rods is

$$
(2 \times 1.25+3)-(2 \times 2.32)=0.86 \mathrm{in} .
$$

This space probably would be inadequate for the size of connecting rods needed. The space could be increased (a) by shifting the counterweights to overhang the outside edges of the crank arms, (b) by increasing the radial distance to the center of gravity of the counterweights $R_{G}$, or (c) by using a counterweight metal of greater density. Shifting of the counterweights is objectionable because the main bearing supports will have to be moved out of line of the main bearings, and this will complicate the crankcase, although a slight shift sufficient for a small increase in space between the counterweights might be made without difficulty. Increase in $R_{G}$ will require a larger diameter and hence an increased weight of crankease. Increase in the density may be attained by using bronze ( $d=0.32 \mathrm{lb}$. per cu. in.). Thus for bronze counterweights,

$$
T=\frac{14.17}{2 \times 10.89 \times 0.32}=2.03 \mathrm{in}
$$

and the space for passage of the connecting rods is

$$
(2 \times 1.25+3)-(2 \times 2.03)=1.44 \mathrm{in}
$$

As the width of the connecting rods for this size of engine would probably not exceed 1 or at most $1 / \frac{1}{4}$ in., this space should be: adequate and the dimensions of the counterweights as determined above and shown in Fig. 7-20 should be satisfactory.

## Suggested Design Procedure

Important. Include sample calculations of all items (as applires). Make: layouts to a large enough seale to permit aceuracy of meatiorements.

1. For the engine being designed, cheok arrangemont of rank arms and rearrange if necessary to attain most suitable conditions for balance.
2. Determine necessary data and, for one cylinder through 360 ) deg . of crank travel, plot curves of
a. Primary reciprocating inertia force.
b. Secondary reciprocating inertia fores.
3. Determine the centrifugal foree that would have to be applied at the crankshaft to balance one-half of the maximum primary reciprocating inertia force in one cylinder.
4. Determine the centrifugal force on the crankpin due to unbalanced rotating weight.
5. By using the crankpin and main bearing dimensions determined in Suggested Design Procedure, page 86, data from Tables A1-8 and A1-9 (as apply), and data from available blueprints, etc., lay out the crankshaft (except the end portions) and determine the detail dimensions of the crank arms.

Make this crankshaft layout to scale, and leave sufficient room on the drawing for both an end view and a longitudinal view. Also leave room for later addition to the drawing of the shaft-end details, i.e., propeller hub and auxiliary-drive connections.

Note: If the engine being designed is an in-line or V type, use the layout, of Suggested Design Procedure, page 86 item 4 as a basis for the detail dimensioning.
6. Determine the centrifugal force on the crankshaft due to the unbalanced weight of the crank.
7. If more than one connecting rod is attached to each crankpin, determine the total centrifugal force that would have to be applied to the crankshaft to balance the part of the unbalanced portion of the reciprocating weight that it is feasible to balance.
8. Determine the total centrifugal force due to item 3 or 7 (as applies), item 4, and item 6 .
9. Determine the dimensions of counterweights necessary to provide for item 8.
10. Lay out the counterweights (item 9 on the drawing of item 5).

Do not blueprint the crankshaft layout at this stage.
11. When items 1 to 10 have been completed and put in proper form; submit for checking and approval.

## References

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## CHAPTER 8

## CRANKSHAFT DETAILS AND REDUCTION GEARING

8-1. Crankshaft Details.-The principal dimensions of the crankshaft having been determined; it is now possible to complete the details of parts. In doing this, it is important to give proper attention to the following points.

1. Provide adequate fillets for all reentrant corners. Such corners are points of high stress concentration and are apt to be critical if sharp. Large radius fillets ${ }^{8}$ aid greatly in reducing this stress concentration.
2. Check the arrangement of parts for possible manufacturing difficulties. See if forging of the shaft can be simplified by some improvement in detail. Aircraft-engine crankshafts are usually machined all over. Check your details of design for any unnecessarily difficult or complicated machining operations. Skilled labor is expensive.
3. All main and connecting-rod bearings should be provided with pressure-feed lubrication. When plain bearings are used, as in in-line and V-engines, oil is usually supplied to the main bearings through passageways in the main-bearing supports. Drilled passageways in the shaft then lead some of this oil to the crankpins. In arranging these passageways, care should be exercised to avoid an excessive number of sharp turns as those turns increase the resistance to circulation of the oil. Avoid too small a size of passageway as the chances of solid particles obstructing the flow will be increased. Excessively large passageways may impair the strength or rigidity of the crank arms, especially if they pass close to highly stressed reentrant corners. Arrangement of oil passageways are shown in Figs. 5-11, 5-12, $5-13$, and 6-6. Other arrangements may be studied from available blueprints and drawings.

Accessory drives such as magnetos, oil pumps, gun synchronizers, and superchargers are usually driven from the rear end of the crankshaft. The main accessory drive shaft for these parts
is usually splined to the crankshaft, and the individual accessories are driven from this shaft through suitable gearing. Considerable leeway is available to the designer in arranging such drives, but for inexperienced designers, it is advisable to adhere rather closely to proven arrangements. Sectional cuts of current successful engines are of assistance in this respect, and examples of proven construction as shown on available blueprints and drawings should be studied.

Aircraft propeller shaft ends have been standardized by the S.A.E. Both taper and spline-type shaft ends are used, the latter being more common in large sizes of engines. Figure A1-6 and Tables A1-19 and A1-20 may bo used for selecting the proper sizes and laying out the propeller end of the crankshaft. In general, the S.A.E. shaft number to solect is that which has a maximum diameter nearest under the diameter of the crankshaft.

8-2. Reduction Gearing.-The brake horsepower that an engine can develop is a function of the speed, but in the case of aircraft engines, the rate of rotation is limited by the propeller efficiency so that it is usually inadvisable to operate direct-drive engines above 2,200 to 2,500 r.p.m. In many instances, the inherent tendency for the propeller efficiency to drop at high speeds can be offsct by suitable reduction gearing.

Wood has shown ${ }^{1}$ that for best performance the diameter of a two-bladed propeller necessary to absorb the sea-level rated power of an engine is

$$
\begin{equation*}
D=\frac{303}{\sqrt{\text { r.p.m. }}} \times \sqrt[4]{\frac{\mathrm{h} \cdot \mathrm{hp}}{\mathrm{~m} \cdot \mathrm{p} \cdot \mathrm{~h}} .} \tag{8-1}
\end{equation*}
$$

where $D=$ diameter of the propeller, ft.
r.p.m. $=$ rated speed of the engine.
b.hp. $=$ rated power of the engine.
m.p.h. $=$ maximum speed of the plane in level flight.

With these data known, the corresponding propeller officiency can be readily determined from Fig. 8-1. The effert of using redurtion gearing in the engine may be demonstrated as follows:

Let $R=$ the reduction gear ratio and $c_{m}=$ the merhanical efficiency of the reduction gear. Then

$$
K=\frac{\text { r.p.m. }}{\text { r.p.m.2 }}, \quad c_{m}=\frac{h_{1} \cdot h_{p \cdot 2}}{\text { h.hp. }}
$$

where subscript 1 refers to the crankshaft and subscript 2 refers to the propeller shaft, and for the same air speed

$$
\begin{equation*}
D_{2}=\frac{303}{\sqrt{\text { r.p.m. } / R}} \times \sqrt[4]{\frac{\text { b.hp. } 1 \times e_{m}}{\text { m.p.h. }}} \tag{8-2}
\end{equation*}
$$

or

$$
\begin{equation*}
D_{2}=D_{1} \sqrt{R} \sqrt[4]{e_{n}} \tag{8-3}
\end{equation*}
$$

The corresponding change in effective propeller pitch will be (for $V_{1}=V_{2}$ )

$$
\frac{V_{2} / n_{2} D_{2}}{V_{1} / n_{1} D_{1}}=\frac{V_{2} / n_{2} D_{2}}{V_{2} / R n_{2}\left(D_{2} / \sqrt{R} \sqrt[4]{e_{m}}\right)} \quad \sqrt{\bar{R}}
$$

or

$$
\begin{equation*}
\frac{V_{2}}{n_{2} D_{2}}-\frac{V_{1}}{n_{1} D} \times \frac{\sqrt{R}}{4} \tag{8-4}
\end{equation*}
$$

With the new value of effective pitch known, the gain in propeller efficiency may be readily found from Fig. 8-1.


Fig. 8-1.-Maximum efficiency of wood and metal propellers as a function of design $V / n D$. (From Wood, "Technical Aerodynamics.")

Example.-An airplane attains $140 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. with an engine of $300 \mathrm{~b} . \mathrm{hp}$. operating at 2,700 r.p.m. (a) find the propeller diameter and maximum propeller efficiency. (b) What gain in propeller efficiency could be had if the engine was equipped with a 3:2 reduction gear having a mechanical efficiency of 90 per cent?

Solution.-From Eq. (8-1),

$$
D_{1}=303 \times \sqrt[4]{\frac{300}{140}}=7.05 \mathrm{ft.}(\text { Ans. } a)
$$

and

$$
\begin{array}{cc:c}
\frac{V_{1}}{n_{1} D_{1}} & 88 \times 140 & 0.649 \\
2,700 \times 7.05 & 0.649
\end{array}
$$

From Fig. 8-1 (for metal propellers),

$$
\eta_{1}=80 \%
$$

From Eq. (8-4),

$$
n_{2} D_{2}=0.649 \underset{\sqrt[4]{0.9}}{1.5} \quad 0.815
$$

From Fig. 8-1,

$$
\eta_{2}=84 \%, \quad \text { and } \quad \eta_{2}-\eta_{1}=84-80=4 \% \text { (Ans. b) }
$$

Since for the same velocity, the thrust horsepower required will be the same, the b.hp. actually needed with the geared engine will be

$$
\text { b.hp. } 2=80 / 84 \times 300=286
$$

If the engine were slowed down enough to attain this gain in efficiency by direct drive, i.e., maintain $V / n D=0.815$, the


Frg. 8-2.-Variation of fullthrottle brake horsepower with speed. power that it could develop would be approximately represented by the expression

$$
\begin{align*}
\text { b.hp. }=\text { b.hp } \cdot \pi
\end{aligned} \quad \begin{aligned}
& \text { r.p.m. } \\
& \text { r.p.m. } \cdot x \\
& d I^{\prime}  \tag{8-5}\\
& d N
\end{align*}
$$

where the subseript $R$ represents rated conditions and
$\frac{d I}{d N}=$ the slope of the full throtite curve (Fig. 8-2). factors, but the ratio of rated to maximum possible $b$.hy. is a major factor. The tendency for volumetrice effiriency to drop at higher speeds is also a contributing factor to lower values of $d P / d N$.

For the example, $d P / d N$ will probably not exceed 0.9 ; hence

$$
\text { b.hp. }=300 \times \frac{1,800}{2,700} \div 0.9=222
$$

But maintenance of the original air speed requires $286 \mathrm{~b} . \mathrm{hp}$. This may be attained either by increasing the amount of supercharging, which will require a higher octane fuel, or by increasing the displacement of the engine.

If the increase in power from 222 to $286 \mathrm{~b} . \mathrm{hp}$. is attained by supercharging, the b.m.e.p. will have to be increased in direct proportion to the brake horsepower. If we assume that the 222 hp . is developed on a 73 octane number fuel, the b.m.e.p. for average conditions (Fig. 1-10) will be about 114 lb . per sq. in. To attain $286 \mathrm{~b} . \mathrm{hp}$., the b.m.e.p. will have to be about

$$
114 \times 286 / 222 \doteq 147 \mathrm{lb} . \text { per sq. in. }
$$

To attain this m.e.p., the engine would have to be supercharged. From Fig. 1-10, it is seen that the fuel would have to have an octane number of upwards of 100 . Such fuels are commercially available but rather expensive.

If the increase in power is attained by increasing the displacement, the weight will also be increased (Fig. 1-3) by upwards of $\frac{(1.85 \times 286)-(1.95 \times 222)}{1.95 \times 222} \times 100=22$ per cent, and this is more
than the increase due to adding reduction gearing.
To keep the bulk and weight of the engine as low as possible, it is essential that the reduction gearing be compact and of a material that will withstand extremely high allowable stresses. This calls for high grades of alloy steel, careful design, and precision workmanship in manufacture. Hence the advantages of a geared drive are partly offset by greater cost and complexity. The power output for which the engine is being designed is an important factor in the decision of whether or not reduction gearing shall be used. Very high power requirements usually dictate the use of reduction gearing, whereas small and mediumpowered engines are usually direct drive. However, the continually increasing demand for small and medium-powered engines of lower specific weight (Fig. 1-3) may ultimately result in a greater use of geared drives in these sizes of power plants.

There are a large number of possible arrangements for reduction gearing, but experience has narrowed the field to three main types (Figs. 8-3 to 8-7).

The single reduction gear has the advantage of simplicity and somewhat lower cost, but it places the thrust line to one side of the axis of symmetry of the engine, and this may produce


Fig. 8-3.-Single reduction gear used on geared models of ranger inverted V-12 engine. Gears are of the herringhone type.
complex stresses in the crankcase. However, when the propeller axis is placed above the crankshaft axis (as is usually the case with single-reduction gearing), the visibility forward in a singleengine tractor-type plane can be improved.

The planetary reduction type of gearing permits keeping the propeller and crankshaft axes concentric, and thereby reduces the complex and more or less indeterminate stresses in the nose of the crankcase. This gain is at the expense of some increase in romplexity of the gearing. A particular advantage of planetary reduction gearing in high-powered engines is the ability to use
more than one planetary gear. This permits dividing the load into several parts and reducing the strain on the gear teeth.


Fig. 8-4.-Arrangement of the Pratt and Whitney type planetary reduction gear.
(A) Propeller shaft; (B) thrust-bearing assembly; ( $C$ ) nose of crankcase; (D) fixed gear bolted to crankcase; ( $E$ ) pinion cage splined to propeller shaft; $(F)$ internal tooth-drive gear splined to crankshaft; $(G)$ crankshaft; ( $H$ ) planetary pinion.


Fig. 8-5.-Arrangement of the Wright Cyclone type of planetary reduction gear.
8-3. Gear Materials and Dimensions.-To provide adequate strength and minimum weight, aircraft-engine reduction gears
are usually made of heat-treated and hardened alloy steels. Casehardened S.A.E. 2515 steel is used in reduction gears of Pratt and Whitney engines, and S.A.E. 4140 or Nitralloy (Table 8-1) is recommended by the Climax Molybdenum Company.

Table 8-1.-Nitralloy Steela Suitable for Rmitetion (iears**
Steel No.
Si
Mn
(r Al
Mr
$0.50-0.55|0.25-0.35| 0.40-0.50|2.00-2.20| 0.30-0.40 \mid 0.20-0.35$
$0.40-0.45|0.20-0.300 .40-0.501 .70-1.90| 0.30-0.40 \mid 0.20-0.35$
$0.25-0.30|0.20-0.30| 0.40-0.501 .70-1.90|0.30-0.40| 0.20-0.35$

* From The Moly Matrix, Vol. 3, No. 8, July, 1936.

Allowable static stresses of 20,000 to $30,000 \mathrm{lb}$. per sq. in. or more may be used depending upon the nature and heat-treatment


Fig. 8-(j.-Arrangement of the Wright ('yclone 2 to 1 ratio bevel-t.ver manotary reduction gear.
(A) Propeller shaft; ( $B$ ) thrust-bearing assembly; (c') mosir of rankease; (D) fixed gear attached to crankease; (E) pinion-gear supporting arm splinod to propeller shaft; $(F)$ drive gear splined to crankshaft; ( $(i)$ drivo-grar thrist braring; $(H)$ pinion gear; (J) pinion-gear thrust bearing; ( $K$ ) erankshaft.
of the steel, and upon the accuracy of construction of the gear teeth. Pratt and Whitney engineers have found an allowable static stress of $22,000 \mathrm{lb}$. per sci. in. satisfactory. Buckingham
recommends ${ }^{2,3}$ the use of data in Tables 8-2 and 8-3 for determining the allowable static stress to be used.

Allowable stresses decrease with increase in pitch-line velocity. This necessary decrease is partly due to the increase in the effect


Fig. 8-7.-Arrangement of bevel type 1.58 to 1 planetary reduction gear from a Wright Cyclone.
of shock loads and inertia of parts at the higher speeds. However, a purely rational expression for variation of allowable stress with pitch-line velocity would be very difficult to obtain due to
Table 8-2-Factors of Safety for Gear Teeth For steady load on a single pair of gears................... 3 For suddenly applied loads on single pairs of gears....... . 4 For steady loads on gears of a train beyond the first mesh. . 5
For suddenly applied loads on gears of a train beyond the first mesh.

the uncertainty of the numerous variables involved. Hence, empirical expressions are used, the most applicable to aircraft engines probably being the following:

For accurately cut gears, Buckingham suggests

$$
\begin{equation*}
S=S_{0}\left(\frac{1,200}{1,200+V}\right) \tag{8-6}
\end{equation*}
$$

and for pitch-line velocities above 4,000 f.p.m., the AGMA recommends the use of Eq. (8-7) for determining the allowable stresses

$$
\begin{equation*}
S=S_{0}\left(\frac{78}{78+\sqrt{V}}\right) \tag{8-7}
\end{equation*}
$$

where $S=$ allowable stress at velocity $V$, lb. per sq. in.
$S_{0}=$ allowable static stress, lb. per sq. in.
$V=$ pitch-line velocity, f.p.m.

$$
\begin{equation*}
V=\frac{\pi D n}{12} \tag{8-8}
\end{equation*}
$$

where $V$ is as in Eqs. (8-6) and (8-7).
$D=$ pitch diameter, in.
$n=$ speed of the gear, r.p.m.
The maximum safe tangential load that can be transmitted by the gear tooth (or the actual transmitted load at the pitch diameter) may be expressed as

$$
\begin{equation*}
W=\frac{S b Y^{\prime}}{P_{d}}=\frac{\pi S b Y}{P_{d}} \tag{8-9}
\end{equation*}
$$

where $W=$ allowable or transmitted load at the pitch line, lb.
$S=$ allowable or transmitted unit stress at velocity $V$, lb. per sq. in.
$b=$ face width of the gear tooth, in.
$Y^{\prime}=$ Lewis outline factor (Table 8-4).
$Y=$ Buckingham strength form factor (Table 8-4) ( $Y^{\prime}=\pi Y$ ).
$P_{d}=$ diametral pitch.
Table 8-4.-Gear-tooth Factors ${ }^{2,3}$ ( $Y^{\prime}=\pi Y$ )

| $\begin{aligned} & \text { Number } \\ & \text { of } \\ & \text { teeth } \end{aligned}$ | $\dot{\text { Lewis outline factor }=Y^{\prime}}$ |  | Buckingham strength form factor $=Y$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $141 / 2$ deg. involute and cycloidal | 20 deg. full-depth involute | $141 / 2 \mathrm{deg}$. involute composite | 20 deg. full-depth involute | $\begin{aligned} & 20 \mathrm{deg} . \\ & \text { stub } \\ & \text { involute } \end{aligned}$ |
| 12 | 0.210 | $0.245^{\circ}$ | 0.067 | 0.078 | 0.099 |
| 13 | 0.220 | 0.261 | 0.071 | 0.083 | 0.103 |
| 14 | 0.226 | 0.276 | 0.075 | 0.088 | 0.108 |
| 15 | 0.236 | 0.289 | 0.078 | 0.092 | 0.111 |
| 16 | 0.242 | 0.295 | 0.081 | 0.094 | 0.115 |
| 17 | 0.251 | 0.302 | 0.084 | 0.096 | 0.117 |
| 18 | 0.261 | 0.308 | 0.086 | 0.098 | 0.120 |
| 19 | 0.273 | 0.314 | 0.088 | 0.100 | 0.123 |
| 20 | 0.283 | 0.320 | 0.090 | 0.102 | 0.125 |
| 21 | 0.289 | 0.327 | 0.092 | 0.104 | 0.127 |
| 23 | 0.295 | 0.333 | 0.094 | 0.106 | 0.130 |
| 25 | 0.305 | 0.339 | 0.097 | 0.108 | 0.133 |
| 27 | 0.314 | 0.349 | 0.099 | 0.111 | 0.136 |
| 30 | 0.320 | 0.358 | 0.101 | 0.114 | 0.139 |
| 34 | 0.327 | 0.371 | 0.104 | 0.118 | 0.142 |
| 38 | 0.336 | 0.383 | 0.106 | 0.122 | 0.145 |
| 43 | 0.346 | 0.396 | 0.108 | 0.126 | 0.147 |
| 50 | 0.352 | 0.408 | 0.110 | 0.130 | 0.151 |
| 60 | 0.358 | 0.421 | 0.113 | 0.134 | 0.154 |
| 75 | 0.364 | 0.434 | 0.115 | 0.138 | 0.158 |
| 100 | 0.371 | 0.446 | 0.117 | 0.142 | 0.161 |
| 150 | 0.377 | 0.459 | 0.119 | 0.146 | 0.165 |
| 300 | 0.383 | 0.471 | 0.122 | 0.150 | 0.170 |
| Rack | 0.390 | 0.484 | 0.124 | 0.154 | 0.175 |

However, the actual dynamic load on the gear tooth will be greater than $W$ by the amount of an increment or impact load that results from acceleration and deceleration of the gear due to inaccuracy in the tooth profiles and tooth spacing. The AGMA

Table 8-5.-Values of the Bugkingham Dynamie Tooth Load Constant, $C$

Material
Tooth form
$0.0005|0.001| 0.002 \mid 0.003$

| Gray iron and gray iron | $14^{12}$-deg. involute | 400 |  | $1,600 \mid 2,400$ |
| :---: | :---: | :---: | :---: | :---: |
| Gray iron and gray iron. | 20-deg. full-depth involute | 415 | 830 | 1,660)\|2,490 |
| Gray iron and gray iron | 20-deg. stub involute | 430) | 860 | 1,720\|2,580 |
| Gray iron and steel | $1+1{ }^{\text {d }}$-deg. involute | 550 | 1,100 | $2,200) 3,300$ |
| Gray iron and steel. | 20-der. full-depth involute | 570 | 1,140 | 2,280)3,420 |
| Gray iron and steel | $20-\mathrm{deg}$. stub involute | 590 | 1,180 | 2,360\|3,540 |
| Steel ${ }^{\text {and }}$ anteel | $14^{12}$-(leg. involute | 800) | 1,600) | $3,200 \cdot 4,800$ |
| Steel and steel. | 20-deg. full-depth involute | 830 | 1,660) | 3,320\|4,980 |
| Steel and steel. | 20-deg. stub involute. | 860 | 1,720 | :3,440 5,160 |

recommends the use of Ed. ( $(\$-10)$ for determining the dymanic tooth load.

$$
\begin{equation*}
W_{d}=\frac{0.05 V(b C+W)}{0.05 V+\sqrt{b C}+W}+W \tag{8-10}
\end{equation*}
$$

where $W_{d}=$ dynamic tooth load, lb .
$V=$ pitch-line velocity,* f.p.m.
$b=$ face width of the gear, in.
$C=$ constant which depends on the material, tooth form, and accuracy of construction of the gear.
$W$ is obtained from Eff. (8-9).
Valucs of $C$ as determined by Buckingham are given in Table 8-5.

* For planetary (epicyclic) gear trains, the velocity of actual footh engagement (Table A3-6) must be used to determine the dynamic lowdings. ${ }^{4}$

To ensure against tooth breakage, the dynamic load should not produce a stress in the material greater than the flexural endurance limit $S_{t}$ of the material. The stress produced may be checked by substituting $W_{d}$ in Eq. (8-9) and solving for the dynamic tooth load stress $S_{d}$. The value thus found should not exceed the value of $S_{t}$ (Fig. 8-8) corresponding to the Brinell hardness number of the gear material.* As an added precaution, Buckingham suggests*

For steady loads, $S_{t} \geqq 1.25 S_{d}$.
For pulsating loads, $S_{t} \geq 1.35 S_{d}$. For shock loads, $S_{t} \geq 1.50 S_{d}$.
Reduction gear teeth may be strong enough to transmit the desired horsepower and withstand the dynamic loading and yet be unable to resist rapid wear. This wear which is usually evidenced by a pitting of the tooth surfaces is generally conceded to be due to compressive fatigue stresses. An


Fig. 8-8.-Relation between Brinell hardness number and flexural endurance-limit stress for steel. (Data from Buckingham, "Manual of Gear Design.") expression for equivalent static tooth load beyond which failure from pitting is likely to occur has been developed by Buckingham and adopted by the AGMA as follows:

$$
\begin{equation*}
W_{w}=D b K Z \tag{8-11}
\end{equation*}
$$

where $W_{w}=$ equivalent static tooth load beyond which pitting (wear) is likely to occur, lb.
$D=$ pitch diameter of the pinion or smaller gear, in.
$b=$ face width of the gears, in.
$Z=$ ratio factor $=2 N_{G} /\left(N_{P}+N_{G}\right)$ for spur gears and $2 N_{G} /\left(N_{G}-N_{P}\right)$ for internal gears.
$N_{P}=$ number of teeth in the pinion.
$N_{G}=$ number of teeth in the gear.
$K=$ stress factor involving the maximum fatigue-limit compressive stress, the pressure angle of the gear teeth, and the moduli of elasticity of the material of the gears. ${ }^{4}$

[^11]Values of $K$ have been determined by Buckingham and are given in Fig. 8-9 and Table 8-6. Since the allowable static load $W_{w}$ varies directly with $K$, it is readily apparent (Fig. 8-9) why casehardened or Nitralloy steels are highly desirable in reduction gearing. To avoid pitting, $W_{d}$ should not exceed $W_{w}$, and for safety, $W_{d} \leq 0.75 \dot{W}_{w}$.


Fig. 8-9.-Values of the Buckingham gear-tooth fatigue constant or loadstress factor. Repetitions of stress in millions: $A-10, B-20, C-50$, D 100. (Data from Buckingham, "Manual of Gear Design.")

The torque on the gear when subjected to a tooth load $W$ is

$$
\begin{equation*}
Q=\frac{W D}{2}=\frac{W N}{2 P_{d}} \tag{8-12}
\end{equation*}
$$

where $Q=$ torque, lb.-in.
$D=$ pitch diameter, in.
$N=$ number of teeth in the gear.
$W=$ allowable load at the pitch line, lb.
$P_{d}=$ diametral pitch.
The face width $b$ is usually made a function of the diametral pitch; the AGMA recommends as good practice

$$
\begin{equation*}
b=\frac{10}{\bar{P}_{d}} \tag{8-13}
\end{equation*}
$$

where $b=$ face width, in.
$P_{d}=$ diametral pitch.

Table 8-6.-Values of the Buckingham Gear-tooth Fatigue Constant ${ }^{2}$ or Stress-load Factor

| Material | Assumed maximum specific compressive stress, lb. per sq. in. | $K$ for 141/2deg. tooth | $K$ for 20-deg. tooth |
| :---: | :---: | :---: | :---: |
| Cast steel and cast steel. | 60,000 | 43 | 59 |
| Forged steel and cast steel. | 65,000 | 50 | 68 |
| Forged steel and forged steel. | 80,000 | 76 | 104 |
| Hardened steel and cast steel. | 90,000 | 96 | 131 |
| Forged steel and semisteel. | 80,000 | 114 | 156 |
| Hardened steel and phosphor bronze. . | 85,000 | 135 | 185 |
| Hardened steel and semisteel. | 90,000 | 145 | 198 |
| Heat-treated steel and heat-treated steel. | 120,000 | 171 | 234 |
| Phenolic laminated and metal | 32,000 | 189 | 259 |
| Semisteel and semisteel. | 90,000 | 193 | 264 |
| Hardened steel and heat-treated steel. | 130,000 | 201 | 275 |
| Hardened steel and hardened steel. | 220,000 | 576 | 790 |

Note: Additional values of $K$ in terms of Brinell hardness will be found in reference 4.
Hence the allowable torque may be expressed as

$$
\begin{equation*}
Q=\frac{5 \pi S Y N}{P_{d}^{\mathbf{3}}} \tag{8-14}
\end{equation*}
$$

where $S=$ allowable unit stress at velocity $V$, lb. per sq. in.
$Y=$ Buckingham strength-form factor (Table 8-4).
$N=$ number of teeth in the gear.
$P_{d}=$ diametral pitch.
The maximum safe horsepower corresponding to Eq. (8-14) is

$$
\begin{equation*}
\text { b.hp. }=\frac{2 \pi n Q}{12 \times 33,000} \tag{8-15}
\end{equation*}
$$

where $n$ is the speed of the gear, r.p.m.
$Q$ is the torque, lb.-in.
Combining Eqs. (8-14) and (8-15)

$$
\begin{equation*}
\text { b.hp. }=\frac{n S Y N}{4,010 P_{d}^{3}} \tag{8-16}
\end{equation*}
$$

or

$$
\begin{equation*}
=\sqrt[3]{\frac{n S Y N}{4,010 \mathrm{~b} \cdot \mathrm{hp}}} \tag{8-17}
\end{equation*}
$$

8-4. Example of Single Reduction Gearing Calculation.-Determine suitable dimensions for a $3 / 2$ single reduction gear to be used on a $150-\mathrm{h}$.hp. 2,700-r.p.m. aircraft engine.

Procedure.-Experience has shown (Par. 8-3) that casehardened S.A.E. 2515 is suitable for reduction gears. Using this material, the allowable static stress may be taken as $S_{0}=22,000 \mathrm{lb}$. per sq. in. For strength (Table A3-4) a $20-\mathrm{deg}$. stub involute tooth should be used. The arrangement of the gearing will be as in Fig. 8-10.


Frg. 8-10.-Arrangement for a single reduction gear.
To start, assume the drive gear No. 1 has 18 teeth, and to keep down weight and frontal area, let the distance between gear eenters $\approx 6$ in. Then $\left(D_{1}+D_{2}\right) / 2=6, \quad D_{2} / D_{1}=32$. From which $I_{1}=4.8$ in., and

Table 8-7.-Standard Diametrai Pitcheis

| 1.00 | 2.50 | 6.00 | 12 | 24 |
| :---: | :---: | :---: | :---: | :---: |
| 1.25 | 3.00 | 7.00 | 14 | 28 |
| 1.50 | 3.50 | 8.00 | 16 | 32 |
| 1.75 | 4.00 | 9.00 | 18 | 36 |
| 2.00 | 5.00 | 10.00 | 29 | 40 |

$P_{d}=18 / 4.8=3.75$. The nearest, standard diametral pitch (Tahle $火-7$ ) is either 3.5 or 4 . Assume $P_{d}=4$, then

$$
D_{1}=18 / 4=4.5 \mathrm{in} .
$$

and the distance between gear centers is

$$
\frac{I_{1}+I I_{2}}{2}=\frac{4.5+1.5 \times 4.5}{2}=5.625 \mathrm{in}
$$

The velocity of the pitch line [ $\mathrm{H}(\mathrm{x} .(8-8)$ ] is

$$
V=\frac{\pi}{12} \times 4.5 \times 2,700=3,180 \text { f.p.m }
$$

and the allowable stress [Ef. (8-6)] is

$$
S^{\prime}=22,000\left(\frac{1,200}{1,200+3,180}\right)=6,020 \mathrm{H} . \text { per } \mathrm{sq} . \text { in. }
$$

From Table 8-4, $Y=0.12$, and from Eq. (8-16),

$$
S=\frac{150 \times 4,010 \times 4^{3}}{2,700 \times 0.12 \times 18}=6,600 \mathrm{lb} . \text { per sq. in. }
$$

This is almost 10 per cent greater than the allowable stress, and although it would likely be taken care of in the factor of safety of the material, it is inadvisable to take unnecessary chances in so important an item.

A reduction in the stress may be made either by increasing the number of teeth or by reducing the diametral pitch, but for small changes, probably the easiest way is to widen the face of the gear. Thus the face width based on Eq. $(8-13)$ is

$$
b=\frac{10}{P_{d}}=\frac{10}{4}=2.5 \mathrm{in}
$$

This width corresponds to a stress at full rated load of $6,600 \mathrm{lb}$. per sq. in. and the face width necessary to reduce this stress to $6,020 \mathrm{lb}$. per sq. in. is

$$
b=2.5 \times \frac{6,600}{6,020} \approx 2.75 \mathrm{in}
$$

Other dimensions of the gears now follow directly (Table A3-4) from the known dimensions, but before assuming that the preceding values of $P_{d}$ and $b$ will be satisfactory, it is necessary to investigate for dynamic loading and excessive wear.

For aircraft-engine reduction gears, the error in tooth action (Table 8-5) will probably not exceed 0.001 in ., and for this error the dynamic tooth load constant for $20-\mathrm{deg}$. stub involute steel gears will be $C=1,720$. From Eq. (8-9),

$$
W=\frac{\pi \times 6,020 \times 2.75 \times 0.12}{4}=1,560 \mathrm{lb}
$$

Hence, from Eq. (8-10) .

$$
W_{d}=\frac{0.05 \times 3,180(2.75 \times 1,720+1,560)}{0.05 \times 3,180+\sqrt{2.75 \times 1,720+1,560}}+1,560=5,750 \mathrm{lb}
$$

Substituting this value of $W_{d}$ in Eq. (8-9) and solving for the stress,

$$
S \quad \frac{W_{d} P_{d}}{\pi b Y}=\frac{5,750 \times 4}{\pi \times 2.75 \times 0.12} \quad 22,200 \mathrm{lb} . \text { per sq. in. }
$$

From Table 8-2, the factor of safety for a single reduction gear should be about 4. Hence the tensile strength will be

$$
22,000 \times 4=88,000 \mathrm{lb} . \text { per sq. in. }
$$

and from Fig. A2-1, the corresponding Brinell hardness will be about 175.* From Fig. 8-8, the flexural endurance limit stress is

$$
S_{t}=42,000 \mathrm{lb} . \text { per sq. in. }>1.5 \times 22,200=33,300 \mathrm{lb} . \text { per sq. in. }
$$

Therefore, the gears are adequate to withstand the dynamic tooth loads.

* This represents the average hardness, not the surface conditions after casehardening.

For the check on probable wear resistance [Eq. (8-11)], $D=4.5 \mathrm{in}$., $b=2.75$ in., and $Z=(2 \times 1.5 \times 18) /(18+1.5 \times 18)=1.2$. By assuming that the steel gears will be casehardened to 500 Brinell hardness, a value of $K$ (Fig. 8-9) of 350 to 750 may be used depending upon the desired life of the gears. For the operating life of an aircraft engine, a value of $K=600$ would appear to be reasonable. Hence,

$$
W_{w}=4.5 \times 2.75 \times 600 \times 1.2=8,900 \mathrm{lb} .
$$

and since $8,900 \times 0.75=6,700 \mathrm{lb} .>5,750 \mathrm{lb}$., the gears are adequate for resistance to wear.

8-5. Example of Planetary-reduction Gearing Calculation.-Determine suitable dimensions for a $3 / 2$ planetary reduction gear to be used on a 150 -b.hp. 2,700-r.p.m. aircraft engine.

Procedure.-Since it will be of interest to compare this type of reduction gearing with the single reduction gearing (Par. 8-4), assume the same material, i.e., S.A.E. 2515 caschardened, $S_{0}=22,000 \mathrm{lb}$. per sc. in. Simple epicyclic spur gearing has been found to be suitable for reducing propeller shaft speed (Fig. 8-4); hence this system of gearing will be selected.


Frg. 8-11.-General arrangement for a three-planet ininion planetary reduction gear.

The arrangement of parts will be as in the figure of Table A3-6 except that in order to reduce and distribute the stress in the most eritical parts more than one planet pinion will be used. For an engine of the size being considered, three* planet pinions will probably be adequate, and these may be supported by a Y-shaped arm (A, Table A3-6). Experience indicates that case 6 of Table A3-6 is a suitable arrangement; hence sun gear $S$ will be fastened to the crankcase so that it cannot rotate, $A$ will be splined to $M_{1}$ (the propeller shaft), and $G$ will be splined to $M_{2}$ (the crankshaft).

* In simple planetary (epicyclic) drives, ${ }^{4}$ the sum of the numbers of teeth in the internal gear and the sun gear must be divisible by the number of planet pinions used, i.e., for three planet pinions, $\left(N_{G}+N_{S}\right) \div 3$ must equal a whole number, etc.

A preliminary sketch of the proposed arrangement of the gearing is shown in Fig. 8-11. Such layouts are useful in fixing more clearly in mind the necessary or desired arrangement o various parts even though later detailed study of means for lubrication, arrangement of bushings, methods of attaching the fixed gear to the crankcase, etc., may necessitate detailed changes.

This layout is sufficient to fix in mind the general plan of the reduction gear and to form a basis for the calculating of over-all dimensions that will be necessary. These sizes having then been determined, the layout may be altered in detail to fac litate manufacture, use of standard parts, arrangement of means for lubrication, etc. In this detail work, much assistance can be had from a study of the details of current successful designs (Figs. 8-4, and 8-5).

To keep the reduction unit as compact as possible, assume that the pitch diameter of the gear is 10 in ., and since there will be three times as many contact points between gears as in the single reduction gearing (Par. 8-4), a larger value of diametral pitch may be used. Let $P_{d G}=6$. Then

$$
N_{G}=6 \times 10=60 \text { teeth }
$$

and from Table A3-6, case 6, for $a_{*} 3 / 2$ reduction*

$$
\text { or } \quad N_{S}=30 \text { teeth }
$$

and the pitch diameter of sun pinion $S$ is

$$
D_{S}=\quad 5 \mathrm{in}
$$

To fit the gears together, the pitch radius of $S$ plus the pitch diameter of $P$ will have to be equal to the pitch radius of $G$ or

$$
D_{P}^{*}=\frac{D_{G}}{2}-\frac{D_{S}}{2} \quad: 5-2.5=2.5 \mathrm{in}
$$

The number of teeth on the pinion gear is

$$
N_{P}=2.5 \times 6=15 \text { teeth }
$$

From Table A3-6, case 6, the speed of the pinions around their own centers will be

$$
n_{P}=2,700 \times \frac{30}{15} \times \frac{60}{60+30}=3,600 \text { r.p.m. }
$$

and the pitch-line velocity [Eq. (8-8)] is

$$
V_{P}=\frac{\pi \times 2.5 \times 3,600}{12}=2,355 \text { f.p.m. }\left(=V_{S}=V_{G},\right. \text { Table A.3-6, case 6) }
$$

From Eq. (8-6), the allowable stress is

$$
S=22,000\left(\frac{1,200}{1,200+2,355}\right)=7,420 \mathrm{lb} . \text { per sq. in. }
$$

The center distance of gears $S$ and $P$ is

$$
E=\frac{D_{S}}{2}+\frac{D_{P}}{2}=2.5+1.25=3.75 \mathrm{in} .
$$

and the pitch-line velocity of the transmitted load (Table A3-6, case 6) is

$$
V=0.5236 \times 2,700 \times 3.75\left(\frac{60}{60-15}\right)=7,060 \text { f.p.m. }
$$

The transmitted load per planet pinion (Table A3-6, case 6) for a threc-planet pinion reduction gear is

$$
W=\frac{33,000 \times 150}{7,060 \times 3}=234 \mathrm{lb} .\left(=W_{S}=W_{G}\right)
$$

From Eq. (8-9), the face width of the pinion to produce a transmitted stress equal to the allowable stress is

$$
z-\frac{234 \times 6}{\pi \times 7,420 \times 0.111}=0.542 \approx \frac{9}{16} \mathrm{in} .
$$

To increase the margin of safety, let $b=5 / 8=0.625 \mathrm{in}$.
To facilitate comparisons, assume the same aceuracy of construction as in the single reduction gearing example of Par. 8-4, i.c., an error in tooth action of 0.001 in . Then; from Table 8-5, the dynamic tooth load constant is $C=1,720$ and the dynamic tooth load [Eq. (8-10)] is

$$
W_{d}=\frac{0.05 \times 2,355(0.625 \times 1,720+234)}{0.05 \times 2,355+\sqrt{0.625 \times 1,720+234}}+234=1,234 \mathrm{lb} .
$$

Substituting this value of $W_{d}$ in Fid. (8-9) and solving for the stress

$$
S_{d}=\frac{1,234 \times 6}{\pi \times 0.625 \times 0.111}=34,000 \mathrm{lb} . \text { per sq. in. }
$$

By using the same flexural enduranee limit load as in the example of Par. 8 - 4 , i.e., $S_{t}=42,000 \mathrm{lb}$. per scl. in., it is apparent that the gear teeth would not break because of the shock loading. However, the factor of safety is $42,000 / 34,000=1.23<1.5$, the value recommended by Buekingham for shock loading.

To increase the factor of safety for shoek or dynamic loading, let $b=1.0 \mathrm{in}$. Then

$$
W_{d}=\frac{0.05 \times 2,355(1.0 \times 1,720+234)}{0.05 \times 2.355 \sqrt{1.0 \times 1,720+234}}+234=1,6554 \mathrm{lb} .
$$

and

$$
S_{d}=\frac{1,654 \times 6}{\pi \times 1.0 \times 0.111}=28,500 \mathrm{lb}, \text { per sq. in. }
$$

The factor of safety for shock loading is now $42,000 / 28,500=1.475 \approx 1.5$; hence the gears should be adequate to withstand the dynamic loading.

For the check on wear resistance, two conditions exist, i.e., (a) wear between the pinion and sun gear and (b) wear between the pinion and internal gear. Considering case (a) first and referring to Eq. $(8-11), D_{P}=2.5 \mathrm{in}$., $b=1$ in., and $Z=(2 \times 30) /(15+30)=1.333$. Assuming the same degree of casehardening, i.e., Brinell hardness $=500$, as in the example of Par. $8-4, K=600$, and

$$
W_{w}=2.5 \times 1 \times 600 \times 1.333=2,000 \mathrm{lb}
$$

Since $W_{d}=1,654<2,000=W_{w}$, wear or pitting should not occur, but $W_{d}=1,654>0.75 \times 2,000=1,500 \mathrm{lb}$., hence the margin of safety is not large.

For case (b), $Z=(2 \times 60) /(60-15)=2.67$ and

$$
W_{w}=2.5 \times 1 \times 600 \times 2.67=4,000 \mathrm{lb}
$$

Since $W_{d}=1,654<0.75 \times 4,000=3,000 \mathrm{lb}$., there is little likelihood of pitting or wear between the pinion and the internal gear.

8-6. Special Gears.-Since interchangeability is not important in reduction gears, it is possible to improve materially on conventional standard gears by resorting to special gearing. Of the possible variations, variable-center-distance gears are in considerable favor. With such gears, the pitch, center distance, addendum, and pressure angle may be varied to suit the tooth number of mating gears best. Reduction in wear, specific sliding, and greater ease of attainment of acceptable accuracy of tooth form are advantages claimed for variable-center-distance gears. Detailed data on these gears are to be found in references 3 and 12.

8-7. Reduction Gear Bearing Loads.-To ensure the selection of proper sizes of bearings for reduction gear shafts, bearing loads due to the gearing should be determined. In general, these loads are dependent upon the horsepower transmitted, the type of gearing, i.e., whether single or double reduction, the tooth pressure angle, and the axial distance of the bearings from the center line of the gears. For helical or bevel gearing, additional thrust loads are also important. Methods of determining bearing loads due to gearing are given in Tables A3-9 to A3-12.

Example.-Determine bearing loads and select suitable sizes of antifriction bearings for the single-reduction gearing of Par. 8-4.

Procedure.-Referring to Fig. 8-10, the location of the bearings relative to the gears will be determined in part by the desired arrangement of the nose of the crankcase and by the location and arrangement of other adjacent parts. Assume for this example that these factors dictate a value of
$A=2$ in., $B=2$ in., $E=2.5$ in., and $F=2.5$ in. Referring to Table A3-9, the torque input is

$$
Q=\frac{63,025 \times 150}{2,700}=3,500 \mathrm{lb} .-\mathrm{in} .
$$

The tangential force is

$$
I^{\prime}=\frac{3,500}{2.25}=1,550 \mathrm{lb}
$$

The separating force for $20-\mathrm{deg}$. stub teeth is

$$
S^{\prime}=1,550 \tan 20^{\circ}=565 \mathrm{lb}
$$

The bearing loads calculated by the methods given in Table A3-9 are tabulated as follows:

| Load duc to | 1 | S |
| :---: | :---: | :---: |
| Bearing 1... | $P_{1}=1,550 \frac{2}{2+2}=775 \mathrm{l}$ | $S_{1}=\pi 65 \frac{2}{2+2}=282.5 \mathrm{H}$ |
| Bearing 2... | $P_{2}=1,550 \frac{2}{2+2}=775 \mathrm{H}$ | $s_{2}=5(5) \frac{2}{2+2}=282.5 \mathrm{lb}$ |
| Bearing 3... | $P_{3}=1,550 \frac{2.5}{2.5+2.5}=77.5 \mathrm{ll}$ | $S_{3}=5\left(i 5 \frac{2.5}{2 . i)+2 . i)}=282.5 \mathrm{lb} .\right.$ |
| Bearing 4... | $P_{4}=1,550 \frac{2.5}{2.5+2.5}=775 \mathrm{lh}$ | $S_{1}=5(5) \frac{2 . i}{2 . i)}+2.5=282.5 \mathrm{lb} .$ |

## Total load

$$
\text { On bearing } 1=L_{1}=\sqrt{775^{2}+242.5^{2}}=825 \mathrm{lh}
$$

By inspection, it is seen that $L_{1}=L_{2}=L_{3}=L_{4}$; hence all bearings will be equally loaded.

Assume that ball bearings are to be used. Then, referring to Table A1-22, for bearings 1 and 2 ,
$L=825 \mathrm{lh}$.
$n=2,700$ r.p.m.
$F=1.0$ (assuming that the thrust will not exceeel 10 per cent of $L$ for straight spur gears).
$Z=0.88$ ( 10 hr . per day $\times 300$ days por year $=3,000$ hr. : easily the life of the usual aireraft engine).
$K=2.0$ (reduction gears are subjeeted to eonsiderable shoek due to torque variation and viluration).
$C=825 \times 1 \times 0.88 \times 2.0=1,450 \mathrm{lb}$.
By assuming that filling-noteh type hearings are tobe userd (Tahbl A1-22W), S.A. E. bearing 407 (heavy series), 308 (medium series), or possihly 210 (light series) could be used. The choice now largely rests with the bore most suitable to fit the crankshaft (see Table A1-22I), but ot hor major dimensions may dictate in some cases.

To simplify the construction, the bearing adjacent to the crank arm might also be used as the end main bearing. In this case, the bearing load should be combined with the gear load to find the resultant load on the bearing.

For bearings 3 and $4, \dot{L}=825 \mathrm{lb}$., $n=1,800$ r.p.m. (for a $3 / 2$ reduction gear), $F=1.0, Z=0.88, K=2.0$, and $C=1,450 \mathrm{lb}$. as before. For filling-notch type bearings (Table A1-22E), S.A.E. bearings 406, 407, 308, or 209 should be strong enough. From Fig. A1-6, it appears that S.A.E. taper-type propeller shafts 1 or 2 should be adequate. The largest diameter of shaft end 1 is 2.05 in . and of shaft end 2 is 2.362 in . (Table Al-20). As the bearing on the propeller shaft end side of the reduction gear could not have a bore less than the maximum diameter of the S.A.E. shaft end, it would have to be at least an S.A.E. 211 bearing for the No. 1 shaft end and probably an S.A.E. 213 bearing if the No. 2 shaft end is used.

Again for the purpose of simplifying construction, it would be advisable to give some attention to the possibility of using the reduction gear bearing. adjacent to the propeller for the dual purpose of taking the gear load and also the propeller thrust. Assume that the propeller efficiency at full throttle climb is 80 per cent, reduction-gear efficiency is 90 per cent, and the airplane speed under climb conditions is $60 \mathrm{~m} . \mathrm{p} . \mathrm{h}$.
The thrust is

$$
T=\frac{375 \times 150 \times 0.9 \times 0.8}{60}=675 \mathrm{lb}
$$

The ratio of thrust to radial load is

$$
\frac{T}{L}=\frac{675}{825}=0.82
$$

and from Table A1-22A, it is apparent that this value of $T / L$ is beyond the recommended range for filling-notch-type bearings. For the nonfillingnotch type, $F=1.3$ and

$$
C=825 \times 1.3 \times 0.88 \times 2.0=1,885 \mathrm{lb}
$$

From Table A1-22K, S.A.E. bearings 312, 313, or 314 should be adequate to handle the combined propeller thrust and reduction-gear load. As S.A.E. bearing 313 has a bore ( $=2.5591$ in.) nearest over the maximum diameter of the propeller shaft end, it is the more logical selection.

8-8. Reaction-torque Measurements.-In connection with the study of reduction gearing, a development by the Pratt and Whitney Company ${ }^{6}$ for measuring brake horsepower in flight is of interest.

In this device (Fig. 8-12), the fixed gear ( $D$, Fig. 8-4) is not bolted to the nose of the crankcase but instead is connected through suitable linkages to two pistons in small hydraulic cylinders. These hydraulic cylinders are connected to a high*
pressure oil line, and one piston head is so shaped that it acts as a control valve. Hence the pistons are always kept floating near mid-travel position. A line from the hydraulic cylinders to a suitable pressure gage on the instrument board of the air-


- Fig. 8-12.-Schematic diagram of Pratt and Whitney torque indieator.
craft permits direct reading of the engine torque. The brake horsepower may readily be found from

$$
\begin{equation*}
\text { b.hp. }=K \times P_{q} \times n \tag{8-18}
\end{equation*}
$$

where $K=$ a constant depending upon the reduction gear ratio and the dimensions of the torque indicator.
$P_{Q}=$ torque-indicator gage reading, lb. por sc. in.
$n=$ r.p.m. of the engine.
For an engine equipped with a constant-speed propeller, the gage could be calibrated to read in units of brake horsepower directly.

8-9. Thrust-bearing Details.-Thrust bearings are usually subjected to a combination of thrust and radial loads. The thrust load will usually be a maximum under full throttle relimb conditions. The thrust in pounds may be determined from

$$
\begin{equation*}
T=\frac{37.5 \times \mathrm{b} . \mathrm{hp} . \times \eta \times \mathrm{c}_{n g}}{V} \tag{8-19}
\end{equation*}
$$

where $T=$ thrust, lb .
b.hp. = brake horsepower.
$\eta=$ propeller efficiency.
$e_{R G}=$ mechanical efficiency of the reduction gearing $(=1.0$ for direct drive).
$V=$ climbing speed of the airplane, m.p.h.

The radial load on the thrust bearing depends upon the arrangement of shaft parts, the type of reduction gearing, and the arrangement of the engine, i.e., in-line, radial, etc. An instance of procedure in combining reduction gear loads with the thrust load has been given in Par. 8-6. For direct-drive radial engines, Table A1-10 should be of assistance in determining the radial load on the thrust bearing.

With the thrust and radial loads known, the procedure in selecting a suitable thrust bearing is essentially the same as the


Fig. 8-13.-Front main and thrust bearing arrangement of Leblond, model 5-F.
(A) Crankshaft; (B) front main bearing; (C) crankcase nose section; ( $D$ ) thrust bearing; ( $E$ ) oil slinger; $(F)$ thrust bearing lock nut; $(G)$ engine nose plate.
example of Par. 8-7. For most conventional arrangements, Table A1-22 gives adequate data for the preliminary selection. Before a design is given final approval for construction, it is advisable to have the manufacturer of the bearing to be used check the selection.

Detail arrangement of thrust-bearing installations vary considerably and probably can best be studied by reference to available cuts and drawings of typical engines. Figure 8-13 shows the detail arrangement of the thrust bearing used on the Leblond radial engine, model 5-F, and Fig. 8-14 shows the thrust
bearing arrangement used on the Menasco six-cylinder in-line engine. Other arrangements are shown in Figs. 8-4 and 8-6.


Fig. 8-14.-Thrust-bearing arrangement. Menasco six cylinder in-line engine.
(A) Crankshaft; (B) front main bearing; (C) thrust bearing; ( $D$ ) oil slinger; $(E)$ excess oil slinger; $(F)$ thrust bearing lock nut; $(G)$ engine nose plate.

## Suggested Design Procedure

Important. Give references for all formulas and empirical factors used. All drawings should bé on standard-size paper and complete in all details, including dimensions, clearances, material specifications, number required, etc. Drawings (except as noted) should be blueprinted and properly folded (Fig. 2-4) for insertion in the design notebook. Keep a record of the manhours required on each item.

1. Complete the remaining crank-arm and crankshaft details (see Suggested Design Procedure, page 142), and check for items suggested in Par. 8-1. Complete the layout and dimersioning of the crank arm and bearing portions of the crankshaft.
2. Select a suitable size of S.A.F. propeller shaft end.
3. Make a preliminary pencil sketch approximately to scale of the desired arrangement of the nose of the crankcase and the connecting parts between the crankshaft and the propeller shaft end. Locate the various parts of the crankshaft, reduction gearing (if used), supporting bearings, and supports for the bearings. Check the arrangement to be certain the parts can be fitted together. Arrange to use standard S.A.E. bearing sizes,
bearing lock nuts, splines, etc., wherever possible. (See tables in the appendix and/or the S.A.E. "Handbook.")
4. If reduction gears are to be used, select the desired arrangement and determine all necessary dimensions. Alter the sketch of item 3 above as necessary.
5. Determine bearing loads for reduction-gear supporting bearings, and select suitable bearings. Alter the sketch of item 3 above as necessary.
6. Determine thrust bearing loads, and select a suitable size of thrust bearing. Alter the sketch of item 3 above as necessary.
7. Complete the detail arrangement of crankshaft and propeller-shaft parts in the nose section. Use S.A.E. standard parts as applies. Complete the desired arrangement of detail parts in the nose section.
8. Make detail drawings of all parts that cannot be definitely identified by S.A.E. number. Include all dimensions, specify materials to be used (by S.A.E. number as applies), indicate heat-treatment and type of casehardening as applies, check arrangement for lubricating of parts, and identify each part by number or-letter in accordance with the part-numbering system being used.
9. Make an assembly drawing of the nose section parts on the layout drawing of Suggested Design Procedure, page 24, item 4. Show parts in section whenever such sectioning increases the clarity or legibility of the drawing. Include only principal over-all dimensions. Identify each part of the assembly drawing by a reference number corresponding to the detail drawing or reference number of that part. When the detailed drawing contains more than one part, identify each part by the detailed drawing number and a letter. Do not blueprint the assembly drawing at this stage.
10. When items 1 to 9 have been completed and put in proper form, submit for checking and approval.

## Problems

1. An airplane attains $150 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. with an engine of $200 \mathrm{~b} . \mathrm{hp}$. operating at 3,200 r.p.m. direct drive.
a. Find the propeller diameter and maximum propeller efficiency.
b. What gain in propeller efficiency could be had if the engine was equipped with an $8 / 5$ reduction gear having a mechanical efficiency of 95 per cent?
c. What brake horsepower could the 3,200-r.p.m. direct-drive engine develop if it were slowed down to the geared-engine propeller speed of 2,000 r.p.m.?
d. By assuming 73 octane number fuel for the slowed-down engine in part $c$, what increase in octane number would be necessary to attain the power required by supercharging?
e. By assuming that the reduction gear increases the weight of the 3,200r.p.m. engine by 12 per cent, what saving in weight will this represent over increasing the size of the engine at 2,000 r.p.m. to where it will develop 190 b.hp.?
2. An engine builder plans to use spur-type single reduction gearing for his in-line 150 -b.hp. $3,000-$ r.p.m. engine. If the pitch diameter of the
pinion is 4 in . and the material is forged S.A.E. 1045 steel, what would be a safe allowable stress at pitch-line velocity?
3. If the pinion in Problem 2 has 16 teeth, a $20-\mathrm{deg}$. stub involute form, and a face width corresponding to AGMA recommendations, what maximum safe tangential load can be transmitted? Will this be adequate for rated brake horsepower?
4. The reduction-gear pinion in Problems 2 and 3 has a Brinell hardness number of 200 and an error in tooth action of 0.001 in . What is the dynamic tooth load stress? Will this dynamic or shock load stress the material beyond its flexural endurance limit?
5. The pinion in the preceding three problems is casehardened to 500 Brinell, and the reduction gear ratio is $3 / 2$. What stress factor $K$ is necessary to prevent pitting and wear of the gear teeth? Explain briefly why a higher surface hardness would help reduce pitting and wear.
6. Select materials and determine suitable dimensions for a $4 / 3$ single reduction gear to be used on a 200 -b.hp. 2,800-r.p.m. aircraft engine. Minimum desirable number of teeth on the pinion 15, minimum desirable diametral pitch 4. Center distance and frontal area to be as small as possible to keep down drag and shielding of cooling fins. Give reasons for each selection or assumption.
7. Select materials and determine suitable dimensions for a $4 / 3$ planetary reduction gear to be used on a 200-b.hp. 2,800-r.p.m. aircraft engine. Minimum desirable number of teeth on any "gear 15, minimum desirable diametral pitch 6 , minimum desirable number of pinion gears 3 , maximum 6 , internal gear to be splined to engine shaft, supporting arms for planet pinion gears to be splined to propeller shaft, sun pinion gear to be bolted to nose of crankcase. Make. a sketch approximately to scale showing the arrangement of gearing, and tabulate calculated stresses, pitch diameters, numbers of teeth, diametral pitch, face width, and approximate over-all dimensions of assembled gearing. Give reasons for each selection or assumption.

## References

1. Wood: "Technical Aerodynamics.'
2. Norman, Ault, and Zarobsky: "Fundamentals of Machine Design."
3. Buckingham: "Spur Gears."
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5. "New Departure Handbook."
6. S.A.E. Jour., Vol. 42, No. 2, February, 1938.
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9. Heldt: Gear Steels, Automotive Ind., Dec. 17, 1938.
10. Rasmussen: Gear Calculations Based on Dynamic Loading and Wear Resistance, Product Eng., Part I, February, 1939; Part 2, March, 1939.
11. Larsen: Internal Gears, Formulas for Calculating Wear Resistance, Product Eng., July, 1939.
12. Albert and Rogers: "Kinematics of Machinery."

## CHAPTER 9

## CYLINDERS AND VALVES

9-1. Functions of the Cylinder.-Aircraft-engine cylinders serve to

1. Provide space for confining accurately metered portions of the charge while it is passing through the cycle or process of having its chemical energy converted into heat and mechanical energy.
2. Guide the piston in its reciprocating motion.
3. Provide the thermal path for removal of a large portion of the heat energy liberated during combustion.
4. Support and guide the valves, and usually support part of the valve gear.
5. Support the spark plugs or, in the case of Diesels, the injector nozzles.
6. Support part of the inlet and exhaust passages for the charge.

These principal funotions very largely dictate the details of design of the cylinder. For instance, requirement 1 necessitates a relatively gastight construction, an accurate combustion chamber space, sufficient structural rigidity to prevent distortion during combustion, fatigue resistance to rapidly varying forces, sufficient strength at operating temperatures, and resistance to corrosion by the products of combustion. Requirement 2 calls for a rigid cylinder to prevent binding of the piston, a smooth wall surface to keep friction to a minimum, a hard wall surface to keep wear low, and in conventional construction sufficient strength to transmit the axial force to the crankcase. Requirement 3 dictates the use of materials of high thermal conductivity. For air-cooled cylinders within the range of sizes used in aircraft engines, this calls for more or less elaborate cooling fins. For liquid-cooled cylinders, a means of confining the liquid closely around the cylinder must be provided. Requirement 4 requires the use of wear-resistant valve seats and guides and sufficient rigidity to prevent binding of parts or leakage of charge. Requirement (5) is evident, and requirement 6 necessitates a more or less complex construction.

In addition to these requirements, the cylinder must (7) be ass light in weight as possible.

9-2. Types of Cylinder Construction.-As in the case of other aircraft-engine parts, compliance with the diverse requirements for cylinders results in numerous compromises in the selection and arrangement of parts. In the automotive. marine, and


Fig. 9-1.-Types of air-cooled cylinders.
(A) Leblond, 4.25 - by 3.75 -in. five-cylinder radial, $18 \mathrm{~b} . \mathrm{hp} . / \mathrm{cyl}$. (B) Lycoming $4.624-\mathrm{by} 4.5-\mathrm{in}$. nine-cylinder radial, 27 b .hp./cyl. (C) Sky Motor $3.875-$ by $4.25-\mathrm{in}$. four-cylinder in-line, $15 \mathrm{~b} . \mathrm{hp} . / \mathrm{cyl}$. ( $D$ ) Menasco 4.5 - by $5.125-\mathrm{in}$. six-cylinder in-line, $27 \mathrm{~b} . \mathrm{hp}$./cyl.

(E)


Fig. 9-1 (Cont.).-Types of air-cooled cylinders. (E) Wright 6.125-loy $6.875-\mathrm{in}$. nine-cylinder radial, 90 b.hp./cyl. ( $F$ ) Kinner $4: 25-\mathrm{by} 5.25-\mathrm{in}$. fivecylinder radial, 20 b.hp./cyl. (G) Lenape 4.125- by 4-in. thiree-cylinder radial, 17 b.hp./eyl.
industrial fields where weight is at less of a premium, cast iron is by far the most commonly used material for cylinders, but for aircraft-engine cylinders its strength-weight ratio is too low, and for air-cooled cylinder heads, its coefficient of thermal conductivity is inadequate for all but the smallest sizes of engines. In a few cases, cast iron is used because of its relatively low cost.

The majority of modern aircraft-engine cylinders are of composite construction, the barrel being machined from a steel forging bolted to or screwed and shrunk into a cast aluminum-alloy head. Aluminum has an excellent thermal conductivity, and the head sections may be made sufficiently thick, without excessive weight, to withstand the gas-force stresses, but it is not sufficiently wear resistant to serve as material for valve guides and valve seats, and usual practice is to use a more suitable alloy for these parts.

To resist wear, steel cylinder barrels are treated to a high surface hardness. In some types of engines, replaceable cylinder liners are used, but in aircraft engines this method is seldom used. Cylinder barrels are usually provided with a hold-down flange which permits their being bolted to the crankcase, but in some cases through bolts from the head have been used. In liquidcooled. engines, jackets of cast aluminum or of sheet steel have been used to confine the cooling medium. In air-cooled engines, fins are machined on the barrel and cast integral with the head. Tigure 9-1 shows typical current arrangements of composite cylinder construction, and additional details may be studied from blueprints and drawings.

9-3. Cylinder Materials.-For cylinder barrels, Johnson ${ }^{1}$ recommends S.A.E. 1050; S.A.E. 4140, or Nitralloy (Tables A2-9 and A2-11). Choice among the three will rest largely with the severity of the service, i.e., the specific performance desired, and with the cost, the plain carbon steel being, of course, the least expensive.

For cylinder heads, aluminum alloys 142, 355, A355, or 195, (Tables A2-1, A2-2, A2-3, A2-4, and A2-5) are recommended. These alloys retain their mechanical properties well at elevated temperatures, a feature particularly desirable in cylinder-head materials.

Valve guides may be made of cast aluminum bronze, ${ }^{1,2}$ S.A.F. Specification 68 (Table A2-12), wrought aluminum bronze, ${ }^{1,2}$
S.A.E. Specification 701 (Table A2-12), or hard cast bronze, ${ }^{1,2}$ S.A.E. Specification 62 (Table A2-12). Valve seats may be made of cast aluminum bronze, ${ }^{1,2}$ S.A.E. Specification 68 (Table A2-12), wrought aluminum bronze, ${ }^{1,2}$ S.A.E. Specification 701 (Table A2-12), or NF-9, an alloy of copper, aluminum, iron, nickel, and manganese (Table A2-10). For severe service, valve seats may be faced with Stellite No. 6 (Table A2-10). Cylinder studs and nuts ${ }^{1}$ may be made of S.A.E. 3140 or 6150 (Tables A2-9 and A2-11). Stellite No. 1 is recommended for valve stem tips.

9-4. The Cylinder Barrel.-To prevent rupture, the cylinder barrel must be strong enough to withstand the maximum gas force to which it is subjected. The greatest gas force occurs normally when the piston is near the top of the cylinder and hence shields the cylinder from direct action of the force, but . under adverse conditions, such as preignition, the upper end of the cylinder barrel may be subjected to near maximum explosion pressure. The usual relation for the stress in thin-walled cylinders is obtained from

$$
\begin{equation*}
P R=S t \tag{9-1}
\end{equation*}
$$

where $P=$ maximum pressure in the cylinder, lb. per sq. in.
$R=$ radius of the cylinder ( $=$ bore $/ 2$ ), in.
$S=$ stress, lb. per sq. in.
$t=$ thickness of the cylinder wall, in.
For thin-walled cylinders with closed ends, the longitudinal stress in the walls is obtained from

$$
\begin{equation*}
P R=2 S^{\prime} t \tag{9-2}
\end{equation*}
$$

where $S^{\prime}=$ longitudinal stress, lb. per sq. in. Obviously the conditions of Eq. (9-1) are the more critical.

In applying Eq. (9-1) to engine cylinders, consideration must be given to manufacturing limitations. Thus, for cast gray iron automotive cylinders with integral jackets, the outer surface of the cylinder wall cannot be machined or closely checked for shift of the core during pouring. Hence, it is usual practice to add about $1 / 8 \mathrm{in}$. to the value of $t$ as determined from Eq. (9-1). For an allowable stress of $6,000 \mathrm{lb}$. per scq. in. and an assumed maximum cylinder pressure of 500 lb . per sq. in., the cylinder wall
thickness for cast iron can be

$$
\begin{equation*}
t=0.0416 \times D+0.125 \tag{9-3}
\end{equation*}
$$

where $D=$ cylinder diameter, in.
This agrees fairly well with the recommendations of Huebotter ${ }^{3}$ and Heldt ${ }^{4}$ for automotive engines.

For air-cooled cast-iron cylinders, both inside and outside surfaces can be machined, and an allowance for eccentricity need not be made. In addition, the cooling fins act as stiffener ribs, and $t$ may be reduced somewhat to save weight. However, caution should be exercised as the longitudinal stress is not affected by the ribs, and due to the relatively small radii of fillets between the cooling fins, high local stresses may be set up.

For steel cylinder barrels, allowable stresses of 12,000 to $20,000 \mathrm{lb}$. per sq. in. may be used, depending upon the quality of the steel.

Cylinders are usually attached to the crankcase by means of hold-down studs which should be sufficient in number to distribute the stress in the cylinder flange and in the metal of the crankcase. S.A.E. coarse series threads ${ }^{2}$ should be used for studs that are to be fitted into aluminum-alloy crankcases. The effective length of the threads in the soft metal should be two to three times the diameter of the stud. Some manufacturers use a reduced diameter of the stud (equal to or slightly less than the root diameter of the threaded portions) so that any misalignment or lack of parallelism will not cause a concentration of stress at the surface of the aluminum adjacent to the edge of the stud hole. Also this shifts the bolt "stretch" away from the threads. Ground threads are also used to increase accuracy and thereby reduce the possibility of part of the threads carrying all the load. The threads are ground after hardening.

Safe loads on studs and bolts are given in Table 9-1. The critical force tending to pull the cylinder off the crankcase is equal to the maximum gas pressure times the piston area. This force is also equal to the force tending to pull the cylinder head away from the barrel. For very high maximum cylinder pressures, as in Diesels, the force tending to pull the cylinders away from the crankcase may be sufficient to require an excessive number and size of studs and a rather massive supporting boss in the crankcase or the use of a stronger crankcase metal. To
permit the use of a very light crankcase, the Packard Diesel used steel hoops around the crankcase on either side of the cylinders. In place, these hoops fitted over flanges at the base of the cylinders, and they were tightened until the crankcase was under considerable initial compression. This method of holding cylinders to the crankcase would not ordinarily be necessary in gasoline engines.

When the head is bolted to the barrel, bolt selection is much the same as for the hold-down studs. For screwed and shrunk heads, a sufficient number of threads should be used to ensure adequate resistance to shear of the weaker metal.

Cooling fins on steel cylinder barrels are usually machined into the steel forging. These fins serve primarily to conduct away excess heat, but they also serve to strengthen and increase the rigidity of the barrel. .

Table 9-1.-Safe Loads for S.A.E. Coarse (N.C.) Thread Series Boliss*

| Nominal bolt diameter, in. | Number of threads per inch | Ultimate strength, lb. per sq. in. |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 65,000 (carbon or nickel steel) | 80,000 (nickel steel) | 95,000 (nickel steel heattreated) |
| 1/4 | 20 | 186 | 229 | 272 |
| 516 | 18 | 322 | 396 | 470 |
| 3/8 | 16 ! | 488 | 601 | 714 |
| $7 / 16$ | 14 | 675 | 830 | 986 |
| $1 / 2$ | 13 | 915 | 1,125 | 1,340 |
| 916 | 12 | 1,186 | 1,460 | 1,730 |
| 5/8 | 11 | 1,480 | 1,820 | 2,170 |
| $3 / 4$ | 10 | 2,240 | 2,760 | 3,280 |
| 7/8 | 9 | 3,140 | 3,860 | 4,580 |
| 1 | 8 | 4,120 | 5,060 | 6,010 |

From Marks: " Mechanical Engineers' Handbook."

* For aircraft-quality steels under steady loads where fatique is not critical or where the uncertainty of uniform load distribution is not a factor, these allowable loads may.be safely doubled or possibly even tripled.

To prevent rapid wear, cylinder walls are usually hardened, and frequently the rubbing surfaces of pistons are made more wear resistant by anodic treatment, i.e., chemically changing the surface to a harder compound. These processes reduce the
rate of wear, but the principal cause of initial wear remains. To get at this cause of wear, it is necessary to consider briefly the usual methods of finishing metal surfaces. In cutting with a tool (Fig. 9-2A) the metal at the point of separation $P$ is torn loose because the point of the tool is too blunt to reach the bottom of the separating space. This process generates much heat, and as the cutting oil does not effectively penetrate this space, most of the heat is absorbed by the metal. When the rate of cutting


Frg. 9-2.-Types of bearing finishes: $(A)$ tearing action of a cutting tool; $(B)$ rough surface from conventional cutting or grinding; $\left(C^{\prime}\right)$ effect of tearing action; (D) principle of the "superfinish" process; ( $E$ ) conventional bearing; ( $F$ ) "superfinished" bearing. [Sections $(C)(D)(E)$ and $(F)$ greatly enlarged.]
i.s sufficient, the thin sections between the grooves made by the tool point (Fig. $9-2 B$ and $C$ ) will be annealed and softened. Subsequent casehardening will restore the temper, but the final finish grinding usually produces a recurrence of the anncaling, for the cutting grains of the stone tear and heat the metal in much the same way as does the tool. Thus, by the conventional methods of finishing, bearing surfaces are far from smooth and if highly magnified would appear in section much the same as Fig. 9-2C and $E$.

In operation, a bearing such as Fig. $9-2 E$ would be satisfactory as long as the viscosity of the lubricant was sufficient to prevent
contact of the high points on the surfaces, but under the high load and temperature conditions encountered in aircraft engines, this ideal condition is unlikely to long exist. Once metallic contact occurs, the greatly increased friction and resulting heat thins the lubricant so that further metallic contact follows rapidly. The result is either fusion of the metal and failure, or if the process is deliberate and less severe, i.e., the so-called "running in" of a new engine, the high points will be gradually removed. Unfortunately, in this latter case, the clearance will be increased, with resulting greater troubles from oil pumping, tendency to blow by, etc.

By removing the high points of the bearing surface (Fig. 9-2D), the possibility of metal-to-metal contact will be very much reduced, the running in time will be lessened or eliminated, and proper clearance will be maintained much longer. With conventional finishing, this smoothing is difficult because as the hone removes the high points it also digs deeper into the base metal to form new scratches. To get around this tendency to form new scratches, a new process of finishing (called superfinish as developed by the Chrysler Corporation) uses a very light pressure on the hone and a liquid of suitable viscosity, which allows the cutting edges of the hone to reach the high points and remove them but prevents the cutting edges from digging into the base metal and forming new scratches. Thus, the annealed high points are removed to form an exceedingly .smooth surface having a hardness practically equal to the original case value. Such finishing greatly reduces the possibility of metal-to-metal contact, and even if it does occur, wear will be less rapid because the area of contact will be much greater.

9-5. Cooling Fins and Baffles.-To prevent an excessive temperature rise in the cylinder with resulting troubles from detonation, structural failure of working parts, etc., it is necessary to provide a good thermal path for heat flow from the combustion chamber to the cooling medium. For direct air-cooled engines,* this necessitates the use of fins on the head and around the upper part of the barrel. The transfer of heat from the cylinder to the cooling air consists of conduction of the heat through the fins to the fin surfaces and of the convection of the heat from the fin surfaces to the cooling air. For constant temperature

[^12]conditions, the heat removed from the head and barrel must be equal to the heat absorbed.

The rate at which heat is given up to the air may be expressed ${ }^{5}$ for the cylinder head as

$$
\begin{equation*}
H=a_{h} U_{h}\left(t_{h}-t_{a}\right) \tag{9-4}
\end{equation*}
$$

and for the cylinder barrel as

$$
\begin{equation*}
H=a_{b} U_{b}\left(t_{b}-t_{a}\right) \tag{9-5}
\end{equation*}
$$

where $H$ is in B.t.u. per hr.
$a_{h}$ and $a_{b}=$ respective base areas of the head and barrel covered by cooling fins, sq. in.
$U_{h}$ and $U_{b}=$ respective over-all heat transfer coefficients for the head and barrel in B.t.u. per hr. per sq. in. of (head or barrel) base area per deg. F. difference between the average (head or barrel) temperature and the cooling air.
$t_{h}$ and $t_{b}=$ respective average temperatures of the head and barrel, deg. F.
$t_{a}=$ temperature of the cooling air, deg. F.
The desirability of having a high over-all heat transfer coefficient is apparent.

Biermann and Pinkel ${ }^{6}$ have shown that the over-all heat transfer coefficient may be expressed as

$$
\begin{equation*}
U=\frac{q}{S+T}\left[\frac{2}{a}\left(1+\frac{W}{2 R_{b}}\right) \tanh a W^{\prime}+S_{b}\right] \tag{9-6}
\end{equation*}
$$

where $U$ is as in Eqs. (9-4) and (9-5).
$q=$ surface heat transfer coefficient, B.t.u. per sq. in. total surface area per hr. per deg. F. temperature difference between the surface and the entering cooling air.
$T=$ average fin thickness, in.
$S=$ average space between fins, in.
$W=$ fin width, in.
$W^{\prime}=W+\frac{T_{t}}{2}$, the effective fin width.
$T_{t}=$ fin-tip thickness, in.
$R_{b}=$ radius from the center of the cylinder to the fin root, in.

$$
a=
$$

$K=$ thermal conductivity of the metal, B.t.u. per sq. in. per deg. F. through 1 in. per hr. ( $K=2.17$ for steel and 7.66 for aluminum Y alloy).
$S_{b}=$ distance between adjacent fin surfaces at the fin root, in. The relation of the various fin dimensions is shown in Fig. 9-3.

The surface heat-transfer coefficient ${ }^{5} q$ of a body is a function of the gas velocity,


Fig. 9-3.-Fin nomenclature:
$T=$ thickness
$S=$ space
$P=$ pitch
$W=$ width
$R_{b}=$ fin root radius density, conductivity, viscosity, specific heat, and dimensions of the body. These factors may be expressed by the relation

$$
\begin{equation*}
q=C_{P} \rho V \times f\left(\frac{\rho V S}{\mu}, \frac{\mu C_{P}}{K}, r_{1}, r_{2}, r_{3}, \ldots\right) \tag{9-7}
\end{equation*}
$$

where $C_{P}=$ specific heat at constant pressure.
$\rho=$ gas density.
$V=$ gas velocity.
$\mu=$ gas viscosity.
$S=$ characteristic dimension.
$\frac{\rho V S}{\mu}=$ Reynolds number.
$\frac{\mu C_{P}}{\bar{K}}=$ Prandtl number.
$r_{1}, r_{2}$, etc., $=$ dimensionless ratios of other important dimensions of the body to $S$.
and $f$ is read "function of."
Experimental studies ${ }^{6}$ by the NACA to determine the effect of these various factors on $q$ for finned cylinders indicate that the surface heat-transfer coefficient is principally affected by the fin spacing and air velocity.* Figure $9-4$ shows results of these tests. Cross plotting against velocity at constant fin spacing showed $q$ to vary about as the 0.796 power of the velocity.

* ( iibson ${ }^{16}$ found that a steel surface gave 5 to 10 per cent greater heat dissipation than aluminum and a coating of stove enamel increased the heat dissipation from cast aluminum fins about 10 per cent.

The values of $q$ in Fig. 9-4 apply only to a cylinder of 4.66-in. diameter and atmospheric conditions of $29.92 \mathrm{in} . \mathrm{Hg}$. and $80^{\circ} \mathrm{F}$. However, by use of the theory of similitude it can be shown ${ }^{6}$ that the data may be applied to other sizes of cylinders and other atmospheric conditions. Thus, if we let

$$
\begin{equation*}
J=\frac{D_{x}}{D_{T}} \tag{9-8}
\end{equation*}
$$

where $D_{x}=$ outer cylinder wall diameter in inches for the cylinder under investigation.
$D_{T}=$ outer cylinder wall diameter in inches for the cylinder upon which Fig. 9-4 is based ( $=4.66$ in.), and relate the other dimensions and the velocities by

$$
D_{T}=\frac{D_{x}}{J} \quad T_{T}=\frac{T_{x}}{J} ; \quad W_{T}=\frac{W_{x}}{J} ; \quad S_{T}=\frac{S_{x}}{J} ; \quad \begin{align*}
& V_{T}=J V_{x}
\end{align*}
$$



Frg. 9-4.-Variation of average $q$ with fin spacing. (From NACA Tech. Rept. 488.)
where $T=$ fin thickness, in.

$$
\begin{aligned}
W & =\text { fin width, in } \\
S & =\text { fin spacing, in } \\
V & =\text { velocity }
\end{aligned}
$$

and the subscripts correspond to the subscripts for the diamcters, the two cylinders may be regarded as dimensionally similar. ${ }^{6}$ The cylinder of diameter $D_{x}$ may now be converted to an equivalent cylinder of diameter $D_{T}$, and by making the conversion for the other factors [Eq. (9-9)], Fig. 9-4 may be entered to find $q_{T}$. The surface heat-transfer coefficient $q_{x}$ may now be found from the relation ${ }^{6}$

$$
\begin{equation*}
q_{x}=\frac{q_{T}}{J} \tag{9-10}
\end{equation*}
$$

The effect of altitude may be corrected by ${ }^{6}$

$$
V_{S}=\begin{gather*}
\rho V_{a}  \tag{9-11}\\
0.0734
\end{gather*}
$$

where $V_{a}=$ velocity at altitude, m.p.h.
$\rho=$ weight density at altitude, lb. per cu. ft.
$V_{S}=$ equivalent velocity at sea level (i.e., corresponding to Fig. 9-4), m.p.h.

Example 1.-Determine the surface heat-transfer coefficient for a cylinder barrel of 4 in . bore, a fin width of 0.7 in ., a fin pitch of 0.25 in ., and a fin thickness of 0.0625 in . The velocity past the cylinder (which corresponds to velocity of best climb) is $60 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. , and atmospheric conditions are standard.

Solution.-Assuming a cylinder wall thickness of in., and using the symbols of Eqs. (9-8) and (9-9),

$$
\begin{aligned}
J & =\frac{4+2 \times 0.125}{4.66}=\frac{4.25}{4.66} \\
S_{T} & =\frac{0.25-0.0625}{0.91}=0.206 \mathrm{in} . \\
V_{J} & =60 \times 0.91=54.5 \mathrm{~m} . \mathrm{p} . \mathrm{h} .
\end{aligned}
$$

From Fig. 9-4, $q_{T}=0.07$, and from Eq. (9-10), $q_{x}=\frac{0.07}{0.91}$

$$
=0.077 \text { B.t.u./(sq. in.)(deg. F.)(hr.) }
$$

Example 2.-Determine the over-all heat transfer coefficient $U$, if the cylinder barrel in Example 1 is of steel, and the fins are rectangular in cross section.


Fig. 9-5.-Values of tanh Z. (From NACA Tech. Rept. 488.)
Solution.-From Example 1, $q=0.077, T=0.0625 \mathrm{in}$. ( $=T_{t}$ for rectangular fins), $S=0.1875 \mathrm{in}$. ( $=S_{b}$ for rectangular fins), $W=0.7 \mathrm{in}$. ( $=W^{\prime}$ for rectangular fins). For steel, $K=2.17$,

$$
\sqrt{\frac{2 q}{K T}}=\sqrt{\frac{2 \times 0.077}{2.17 \times 0.0625}}-1.067, \quad 2 R_{b}=4.25 \mathrm{in} .
$$

Substituting these values in Eq. (9-6),

$$
\begin{aligned}
& U=\begin{array}{c}
0.077 \\
0.1875+0.0625
\end{array}\left[\frac{2}{1.067}\left(1+\frac{0.7}{4.25}\right) \tanh 1.067 \times 0.7+0.1875\right] \\
& U=0.308(2.185 \tanh 0.745+0.1875)
\end{aligned}
$$

From Fig. $9-5, \tanh 0.745=0.64$

$$
\begin{aligned}
& U=0.308(2.185 \times 0.64+0.1875) \\
& U=0.495 \text { B.t.u. } / \text { (hr.) (sq. in.) (deg. F.) difference }
\end{aligned}
$$

Example 3.-Determine the over-all heat-transfer coefficient for the aluminum $Y$ alloy head fins of the cylinder in Example 1 for an average fin width of $1 \mathrm{in} .$, a pitch of 0.38 in ., and an average fin thickness of 0.1 in . Assume that the fin-tip thickness is 0.08 in . and the fin-root thickness is 0.12 in . Assume an average head thickness of 0.375 in .

Solution.-The data of Fig. 9-4 are based on cylinder barrels, but it may be assumed that the air-flow characteristics around the head approximate the conditions of the barrel; hence .

$$
\begin{aligned}
J & =\frac{4+2 \times 0.375}{4.66}=1.02 \\
S_{T} & =\frac{0.38-0.1}{1.02}=0.274 \mathrm{in} . \\
V_{J} & =60 \times 1.02=61 \mathrm{~m} . \text { p.h. }
\end{aligned}
$$

From Fig. 9-4, $q_{T}=0.09$, and from Eq. (9-10),

$$
q_{x}=\frac{0.09}{1.02}=0.0882 \text { B.t.u./(sq. in.) (deg. F.) (hr.) }
$$

For the over-all heat-transfer coefficient, $q=0.0882, T=0.1 \mathrm{in} ., T_{t}=0.08$ in., $S=0.28$ in., $S_{b}=0.26$ in., $W=1$ in., $W^{\prime}=1+\frac{0.08}{2}=1.04 \mathrm{in}$,, $2 R_{b}=4.75$ in., for aluminum Y alloy $K=7.66, a=\sqrt{\frac{2 \times 0.0882}{7.66 \times 0.1}}=0.48$

Substituting these values in Eq. (9-6),

$$
\begin{aligned}
& U=\frac{0.0882}{0.28+0.1}\left[\frac{2}{0.48}\left(1+\frac{1}{4.75}\right)(\tanh 0.48 \times 1.04)+0.26\right] \\
& U=0.232[(5.04 \times \tanh 0.5)+0.26]
\end{aligned}
$$

From Fig. 9-5, $\tanh 0.5=0.475$

$$
U=0.615 \text { B.t.u./(hr.) (sq. in.) (deg. F.) difference }
$$

Pinkel ${ }^{5}$ has shown that for a Pratt and Whitney $1340-\mathrm{H}$ cylinder, the relation among the average cylinder barrel and head temperatures, the indicated horsepower, and the over-all heattransfer coefficient may be expressed as in Fig. 9-6. These curves are based on data from one size and design of cylinder, but they serve to show the approximate temperatures of other sizes of reasonably similar cylinders.

Example 4.-Determine the approximate cylinder wall and head temperatures for the cylinder in Examples 1, 2, and 3, if the engine is a five-cylinder radial rated at $70 \mathrm{~b} . \mathrm{hp}$.

Solution.-From Fig. A1-2, the mechanical efficiency will be about 85 per cent, hence the indicated horsepower per cylinder will be

$$
\text { i.hp. }=\frac{70}{0.85 \times 5} \quad 16.5
$$

For the cylinder wall,

$$
\frac{U}{\text { i.hp. }} \text {. } \quad \frac{0.495}{16.5^{0.64}}=0.0825
$$

From Figure $9-6$, the approximate average cylinder-barrel temperatiore is $325^{\circ} \mathrm{F}$.
For the cylinder head,

$$
\frac{U}{\text { i.hp. }{ }^{0.64}}=\frac{0.615}{16.5^{0.64}}=0.1027
$$

From Fig. 9-6, the approximate average cylinder-head temperature is $355^{\circ} \mathrm{F}$.
Example 5.-Determine for the engine of the preceding four examples the portion of the heat supplied which is removed by the cooling fins. Air temperature $80^{\circ} \mathrm{F}$., number of cooling fins on the cylinder barrel $=20$.

Solution.-The area of the barrel covered by cooling fins is

$$
a_{b}=20 \times 0.25 \times \pi \times 4.25
$$

66.7 sq. in. $\stackrel{\text { t }}{\circ}$

The heat removed per hour through the barrel fins is [from Eq. (9-5)]

$$
\begin{aligned}
& H_{b}=66.7 \times 0.495(325-80) \\
&=8,100 \text { B.t.u. per hr. }
\end{aligned}
$$

The area of the head covered by cooling fins is somewhat irregular and the effective area is uncertain due to the complicated heat flow around the valves. However, the area may be approximated by assuming that

$$
\begin{equation*}
\frac{a_{h 1}}{a_{b 1}}=\frac{a_{h 2}}{a_{b 2}} \tag{9-12}
\end{equation*}
$$



Fig. 9-6.-Approximate relation between cylinder-barrel and-head temperatures, indicated horsepower, and the over-all heat-transfer coefficient. (From NACA Tech. Rept. 488.)
where $\dot{a_{h 1}}$ and $a_{b 1}$ are the respective base areas of the head and barrel of the cylinder under consideration. $a_{h 2}$ and $a_{b 2}$ are the respective base areas of the head and barrel of a similar cylinder that has been measured.

According to Pinkel, ${ }^{5}$ the Pratt and Whitney $1340-\mathrm{H}$ cylinder has a base area of barrel covered by fins of $a_{b 2}=68.7 \mathrm{sq}$. in., and a base area of head of $a_{h 2}=142 \mathrm{sq}$. in. Hence, if we assume that the cylinder under considera-
tion is similar to the Pratt and Whitney 1340-Hy cylinder, the base area of the head may be taken as

$$
a_{h 1}=\frac{66.7 \times 142}{68.7}=138 \text { sq. in. }
$$

When possible, of course, it is much more advisable actually to measure the areas for the cylinder under consideration.

The heat removed per hour through the head fins is [From (Eq. 9-4)]

$$
H_{h}=138 \times 0.615(355-80)=23,400 \text { B.t.u. per } \mathrm{hr} .
$$

At rated load, an engine of this power should have a brake thermal efficiency of at least 25 per cent. Hence, the heat supplied per cylinder per hour is

$$
H_{s}=\frac{2545 \times 70}{0.25 \times 5}=142,300 \text { B.t.u. per } \mathrm{hr} .
$$

The percentage of the heat supplied that passes out through the cooling fins is

$$
\frac{8,100+23,400}{142,300} \quad 0.221, \text { or } 22.1 \%
$$

According to Swan, ${ }^{15}$ for adequate cooling, the heat dissipated from the cooling fins should be about equal to 50 to 60 per cent of the heat equivalent of the brake horsepower. On this basis, for adequate cooling of the engine in Example 5, it would be necessary for the fins to dissipate not more than

$$
\frac{2,545 \times 70 \times 0.6}{5}=21,378 \text { B.t.u. per cyl. per hr. }
$$

Since the fins are capable of dissipating

$$
8,100+23,400=31,500 \text { B.t.u. per cyl. per hr. }
$$

under the assumed conditions, it is evident that the assumed fin dimensions are easily adequate.

As the specific power output of an engine is increased by supercharging, a limit is quickly reached at which ordinary methods of air cooling are inadequate. To extend this limit, controlled cooling by means of deflectors or baffles is used. These baffles are designed to deflect the air into the fin spaces where it would not flow normally, such as the downstream or rear side of the cylinders. The effect of a well-designed close-fitting baffle in reducing cylinder temperature, particularly at the rear side of the cylinder, is shown in Fig. 9-7.

The NACA has investigated the effect of several types of baffles and deflectors on temperature reduction and heat transfer, ${ }^{7}$ and the findings indicate that the surface coefficient $q$ is increased about 30 per cent by the use of a good shell baffle. The shape of the baffle is also of importance, the conclusions being that ( $a$ ) the shell should fit tightly around the ends of the fins, (b) the entrance angle ( $\alpha$ in Fig. 9-7) should be about 145 deg., (c) the rearward extension of the baffle behind the cylinder should


Fig. 9-7.-Temperature distribution around a finned cylinder: (A) with shell baffle; (B) without baffles. (From S.A.E. Jour., Vol. 35, No. 4.)
be about 3 in., and (d) the ratio of exit area to free-flow area between the fins should be between 1.6 and 2.3. It was also observed that both with and without baffles the surface heattransfer coefficient $q$ varied as the 0.85 power of the air speed. This is slightly greater than the 0.796 reported in reference 6 .

To force the cooling air between the fins and through the baffles, it is necessary to provide a pressure drop or difference in pressure between the inlet and exit sides. This available pressure drop can be provided by suitable engine cowling such as the NACA or equivalent cowling. The quantity of air that must be forced between the fins is dependent upon the specific
weight, specific heat, and temperature rise of the air, or

$$
\begin{equation*}
Q=\frac{H}{3,600 w c_{P}\left(t_{o}-t_{i}\right)} \tag{9-13}
\end{equation*}
$$

where $Q=$ flow, cu. ft. per sec.
$H=$ heat to cooling, B.t.u. per hr. [corresponding to the $H$ in Eqs. (9-4) and (9-5)].
$w=$ specific weight of the air, lb. per cu. ft.
$c_{P}=$ specific heat of the air $=0.24$ B.t.u. per lb .
$t_{o}=$ outlet air temperature at the baffle exit, deg. F.
$t_{i}=$ inlet air temperature $=$ atmospheric temperature, deg. F.
Since the temperature rise ( $t_{o}-t_{i}$ ) is relatively small, $Q$ will have to be quite large, but since

$$
\begin{equation*}
Q=A V=C A \sqrt{2 g h} \tag{9-14}
\end{equation*}
$$

where $A=$ cross-sectional area of the space between the fins, sq. ft.
$V=$ mean velocity of the air between the fins, ft. per sec.
$C=$ a coefficient relating theoretical and actual velocity.
$g=$ acceleration of gravity, ft. per sec. ${ }^{2}$
$h=$ head or pressure drop causing flow, feet of air, and since air drag is proportional to $h$, it is apparent that increase in heat transfer by increasing the velocity will be at the expense of a rapid increase in drag of the engine. The air-drag horsepower necessary to provide the necessary $Q$ may be expressed as

$$
\begin{equation*}
H P_{A D}=\frac{Q \times P_{d}}{550} \tag{9-15}
\end{equation*}
$$

where $Q=$ air flow between the fins, cu. ft. per sec.
$P_{d}=$ pressure drop, lb. per sq. ft.
But $\quad P_{d}=h w$ where $w$ is the specific weight of the air, lb. per cu. ft.
Thërefore,

$$
\begin{equation*}
H P_{A D}=\frac{C^{\prime} w A h^{3 / 2}}{550} \tag{9-16}
\end{equation*}
$$

where $C^{\prime}=C \times \sqrt{2 g}$ and the other symbols are the same as in the preceding equations.
From this, it is evident that it is more economical from a powerloss standpoint to increase the heat transfer by increasing the area
$A$, and this may be best attained by increasing the width of the fins. Unfortunately, manufacturing limitations have prevented the use of cast fins having a width much greater than about 1.5 to 2.0 in., a thickness less than about $1 / 16$ in., and a space

Rear spark $\qquad$
$\&$ plug gasket
B

Fig. 9-8.-Effect of turbulence and pressure drop on cylinder-head temperature for $A$ Wright Cyclone cylinder. Curves $B$ approximate the turbulence of flight conditions. (From Campbell, Cylinder Cooling and Drag of Radial Engine Installations, S.A.E. Jour., Vol. 43, No. 6, December, 1938.) :


Fig. 9-9.-Baffle pressure drops for different types of cowling and air speeds. (From S.A.E. Jour., Vol. 43, No. 6.)
between fins of much less than 5,32 in., and even these dimensions are attained at considerable expense and foundry troubles. To attain greater heat transfer than these dimensions will permit at present necessitates either increasing the pressure drop $h$, by improved cowling ${ }^{10}$ or for extreme cases by blower cooling, ${ }^{8}$ or
increasing the effectiveness of heat transfer, i.e., controlling the turbulence of the air. ${ }^{10}$ An example of the effect of turbulence and pressure drop on cylinder temperature is shown in Fig. $9-8$. For recent data on cowl and baffle design for very high-


Frg. 9-10.-Effect of baffle pressure drop and fin spacing on surface heat transfer coefficient. (From S.A.E. Jour., Vol. 41, No. 3.)
performance engines, the student should consult references 8,9 , and 10 .

Attainable pressure drops across baffled cylinders vary so widely with the design details of the cowling that it is necessary


Fra. 9-11.-Type of baffle used to determine the data of Fig. 9-10. (From S.A.E. Jour., Vol. 41, No. 3.) to know in detail the arrangement of the parts of the cowling in order to decide just what pressure drop can be obtained. Very few data of this sort are available, but reference to Fig. 9-9 indicates that baffle pressure drops of 4 to 6 in . of water at maximum speed and 2 to 4 in. of water at climbing speed would be reasonable assumptions for engine-design purposes. The effect of pressure drop on the surface heat transfer coefficient is shown in Fig. 9-10. These data are based on a cylinder of 4.66 in . diameter enclosed in a special type of baffle designed for blower sooling (Fig. 9-11). However, in the absence of more complete
data, they may be approximately applied to the general case by use of Eqs. (9-8), (9-9), (9-10), and (9-11).

Example 6. What increase in the proportion of heat to cooling could be attained for the engine in Example 5 if the cylinders were baffled and a baffle pressure drop of 2 in . of water was available?

Solution.-From Example 1, $J=0.91, S_{T}=0.206$ in., and

$$
\nabla J=54.5 \mathrm{~m} . \mathrm{p} . \mathrm{h} .
$$

From Fig. $9-10, q_{T}=0.1 \dot{5} 1$, and from Eq. (9-10),

$$
q_{x}=\frac{0.151}{0.91} \quad 0.166 \text { B.t.u./(sq. ïn.)(deg. F.)(hr.) }
$$

For the over-all heat transfer coefficient of the cylinder barrel,

$$
a=\sqrt{\frac{2 q}{K T}}=\sqrt{\frac{2 \times 0.166}{2.17 \times 0.0625}}
$$

and

$$
\begin{aligned}
& U_{\mathrm{b}}=\frac{0.166}{0.1875+0.0625}\left[\frac{2}{1.565}\left(\mathrm{I}^{\cdot}+\frac{0.7}{4.25}\right)(\tanh 1.565 \times 0.7)+0.1875\right]^{-} \\
& U_{b}=0.91 \text { B.t.u./(hr.)(sq. in.)(deg. F. difference) }
\end{aligned}
$$

From Example 3; $J=1.02, S_{T}=0.274$, and $V J=61 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. From Fig. $9-10, q_{T}=0.164$, and from Eq. (9-10),

$$
\frac{0.164}{1.02}=0.161 \text { B.t.u./(sq. in.)(deg. F.)(hr.) }
$$

For the over-all heat transfer coefficient for the cylinder head,

$$
a=\sqrt{\frac{2 q}{K T}}=\sqrt{\frac{2 \times 0.161}{7.66 \times 0.1}}=0.649
$$

and

$$
\begin{aligned}
U_{h} & =\frac{0.161}{0.28+0.1}\left[\frac{2}{0.649}\left(1+\frac{1}{4.75}\right)(\tanh 0.649 \times 1.04)+0.26\right] \\
U_{h} & =1.042 \text { B.t.u. } / \text { hr. }) \text { (sq. in.)(deg. F. difference) }
\end{aligned}
$$

For the cylinder barrel,

$$
\underset{\text { i.hp. }{ }^{0}}{U} \quad \frac{0.91}{16.5^{0.6}}=0.1515
$$

From Fig. 9-6, the approximate average cylinder-barrel temperature is $240^{\circ} \mathrm{F}$.

For the cylinder head,

$$
\frac{U}{\text { i.hp. } .^{0.64}}=\frac{1.042}{16.5^{0.64}}=0.1735
$$

From Fig. 9-6, the approximate average cylinder-head temperature is $250^{\circ}$.

The heat removed per hour through the barrel fins is [from Eq. (9-5)]

$$
H_{b}=66.7 \times 0.91(240-80)=9,200 \text { B.t.u. per hr. }
$$

The heat removed per hour through the head fins is [from Eq. (9-4)]

$$
H_{h}=138 \times 1.042(250-80)=24,450 \text { B.t.u. per hr. }
$$

The percentage of the heat supplied that passes out through the cooling fins is

$$
H_{C F}=\frac{9,200+24,450}{142,300}=0.2365, \text { or } 23.65 \%
$$

The increase in heat to cooling is

$$
23.65-22.1=1.55 \%
$$

The percentage increase is

$$
\frac{1.55}{22.1} \times 100=7 \%
$$

Example 7.-Assuming an octane number such that the cylinder temperatures without baffles, i.e., $t_{b}=325^{\circ} \mathrm{F}$. and $t_{h}=355^{\circ} \mathrm{F}$. as found in Example 4, are satisfactory, what increase in indicated horsepower per cylinder would be possible with baffles and a baffle pressure drop of 2 in . of water.

Solution.-For the cylinder barrel, for $t_{b}=325^{\circ}$ F. (from Fig. 9-6),

$$
\frac{U_{b}}{\text { i.hp.0.64 }} \quad 0.0825
$$

and for $U_{b}=0.91$ (Example 6)

$$
\text { i.hp. }=\left(\frac{0.91}{0.0825}\right)^{1 / 0.64}=43
$$

For the cylinder head for $t_{b}=355^{\circ}$ F. (from Fig. 9-6),

$$
\frac{U_{h}}{\text { i.hp. }{ }^{0.64}}=0.1027
$$

and for $U_{h}=1.042$ (Example 6)

$$
\text { i.hp. }=\left(\frac{1.042}{0.0127}\right)^{1 / 0.64}=37.2
$$

The limiting part is the cylinder head, and for $t_{h}=355^{\circ} \mathrm{F}$., the percentage increase in horsepower by using baffles and a 2 -in. pressure drop is

$$
\frac{37.2-16.5}{16.5} \times 100=125 \%
$$

The value of baffles and cowling is readily apparent.

9-6. Valve Requirements and Materials.-During operation, aircraft-engine valves are subjected to or must withstand

1. Combustion temperatures ranging up to $3,000^{\circ} \mathrm{F}$. or more.
2. Exhaust temperatures of the order of 1,200 to $1,500^{\circ} \mathrm{F}$.
3. Pressures of 500 or more pounds per square inch without leaking.
4. Rapid hammering of the valve face against its seat and of the tappet against the end of the stem.
5. Wear due to friction in the valve guides.
6. Corrosion or oxidation by various constituents in the charge and in the products of combustion.

To meet these conditions a valve must have

1. A high strength at unusually high working temperatures.
2. Maximum resistance to distortion or warping.
3. Sufficient hardness and resistance to impact to prevent rapid wear.
4. Resistance to corrosion and oxidation.
5. No tendency to air-harden when cooled rapidly.

These requirements are difficult to meet and some of them are conflicting. Hence, few materials are entirely satisfactory, and valves, especially exhaust valves, have long been regarded as limitations to further increases in performance. However, gradual progress in design details, particularly in regard to more effective cooling, and now developments in special steels are continually pushing back. the limitations. Suitable valve materials ${ }^{4,11,12}$ are S.A.E. 3140, chrome nickel steel, silcrome steel, and colbalt-chromium steel (see also Tables A1-3 and A2-11). The advantage in physical properties of austenitic steels over hardenable steels for exhaust valves at high-performance operating temperatures is indicated by Fig. 9-12.


Fig. 9-12.-Strength of hardenable vs. austenitic steel. Note superiority of austenitic steel at high temperatures. (From Wil-Rich Forum, Vol. 11, No. 3.) Austenitic steels also have high corrosion resistance. For severe service, Stellite-faced seats, special hardening, and internal cooling by salts or sodium may be used. Salts usually
used are lithium and potassium nitrate. These salts or sodium, when sealed in the hollowed-out stem of the exhaust valve, melt at operating temperatures and are thrown back and forth in the space due to the reciprocating motion of the valve. In this way, heat is mechanically carried from the hot head of the valve to the relatively cooler stem adjacent to the valve guide. The hollow stem is usually filled a little more than half. full of the coolant.

9-7. Breathing Capacity and Valve Size.-The area of a valve head exposed to the combustion gases increases as the square of the diameter, but the area through which heat can escape to the valve seat increases only as the first power of the diameter (for a given seat width). Hence, large valves are more difficult to cool. ' Large valves are also heavier, and this means greater load on the valve gear during the rapid acceleration of opening


Fig. 9-13.-(A) Conventional conical-seated valve. (B) Flat-seated valve.
and on the valve springs during closing. However, too small a valve tends to restrict the flow of charge and thereby reduce the volumetric efficiency and power of the engine (Fig. 9-15). Valve size is also limited by the available area of combustionchamber wall. Multiple valves, i.e., two intake and two exhaust valves per cylinder, permit a greater area of opening for the charge and increase the ratio of area of valve seats to head but at the expense of increased complexity of valve gear and cylinder head. At present, multiple valves are used principally on large liquid-cooled engines. Adequate area of opening is obtained in radial engines with one intake and one exhaust valve by inclining the valves at an angle to the cylinder axis (Fig. 9-1).

Valve seats (Fig. 9-13) may be flat, i.e., normal to the valvestem axis, or inclined (conical), the latter being the practice in aircraft engines. Flat-seated valves give a somewhat greater area of opening for a given valve lift, but gas in passing through
the opening has to make two approximately $90-\mathrm{deg}$. turns which tend to increase the turbulence and the resistance to passage. Gas in passing a conical-seated valve can assume a more nearly streamlined flow with resulting less friction. Hence, although the conical-seated valve has the disadvantage of a less area of opening for a given valve lift, it is generally conceded to give higher volumetric efficiency than the flat-seated valve. In addition, the conical seat helps to keep the valve head aligned with the stem. Both 30-deg. and 45-deg. seats are used, but the latter is by far the most common.

Theoretically, the area of opening through the valve seat should be about the same as the minimum net area of the port. For the flat-seated valve (Fig. 9-13), the area through the seat is

$$
\begin{equation*}
A_{F S}=\pi d_{1} h \tag{9-17}
\end{equation*}
$$

where $d_{1}=$ minimum port diameter, in.
$h=$ lift of the valve, in.
The area of the port is

$$
A_{v}=0.785\left(d_{1}^{2}-d_{2}^{2}\right)
$$

where $d_{2}=$ diameter of the valve stem.
Combining Eqs. (9-17) and (9-18), the lift necessary to avoid pinching the flow is

$$
\begin{equation*}
h=\frac{\left(d_{1}^{2}-d_{2}^{2}\right)}{4 d_{1}} \tag{9-19}
\end{equation*}
$$

Inlet valve stem diameters are usually about 25 per cent of the valve port diameters.
On this basis, Eq. (9-19) becomes

$$
\begin{equation*}
h=\frac{d_{1}^{2}-\left(0.25 d_{1}\right)^{2}}{4 d_{1}}=0.234 d_{1} \tag{9-20}
\end{equation*}
$$

The area of opening through a conical-seated valve (wide valve face) is the lateral area of the frustum of a right circular cone. Referring to Fig. 9-13 $A$, the diameters of the frustum of the cone are $d_{1}$ and $d_{3}$ and the slant height is

$$
M N=S=h \cos \alpha
$$

where $h=$ lift, in.,

$$
\alpha=\text { angle of the valve seat }
$$

also

$$
d_{3}=d_{1}+2 M F=d_{1}+2 S \sin \alpha=d_{1}+2 h \cos \alpha \sin \alpha
$$

Since the lateral area of the frustum of a right circular cone is

$$
A=\frac{\pi}{2} S\left(d_{1}+d_{3}\right)
$$

where $S$ is the slant height and $d_{1}$ and $d_{3}$ are the diameters of the bases, the area of opening through the conical valve seat may be expressed as

$$
\begin{equation*}
A_{c S}=\pi h \cos \alpha\left(d_{1}+h \cos \alpha \sin \alpha\right) \tag{9-21}
\end{equation*}
$$

For the most commonly used conical angle of $\alpha=45 \mathrm{deg}$., Eq. (9-21) reduces to

$$
\begin{equation*}
A_{c s}=1.11 h^{2}+2.22 d_{1} h \tag{9-22}
\end{equation*}
$$

Equating this value of $A_{C S}$ to the net area of the valve port and letting $d_{2}=0.25 d_{1}$.

$$
h^{2}+2 d_{1} h=0.663 d_{1}^{2}
$$

From which

$$
\begin{equation*}
h=0.29 d_{1} \tag{9-23}
\end{equation*}
$$

For the line $M N$ (Fig. 9-13) to pass through the valve face with this amount of lift, $d_{4}$ would have to be considerably less than $d_{1}$. If $d_{4}$ is only slightly less than $d_{1}$ (the usual case), the area of opening will approximate the lateral area of a frustum of a right cone plus the lateral area of a cylinder of diameter $d_{1}$, i.e., the lift will be intermediate between that for a conical seat and that for a flat-seated valve. For very narrow valve seats,* the lift for a conical-seated valve will approach that for a flat-seated valve. Hence, for minimum restriction to flow, $h=0.25 d_{1}$.

* Swan ${ }^{15}$ suggests the following exhaust valve seat widths:

| Port diameter, in............. | 7/8-11/8 | 11/4-17/8 | 2-21/4 | 23/8-27/8 | $3-31 / 4$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Projected seat width, in.... | $5 / 64$ | $3 / 32$ | 1/8 | 532 | 7/32 |

See also Lichty, "Internal Combustion Engines," 5th ed., p. 309.

Lewis and Nutting ${ }^{13}$ have found that verocties tnrougr valve opening more nearly approach the tneoretical velociuy $V(=\sqrt{2 g H})$ when the lift is a smaller percentage ot the diameter of the valve $[=f$ (diameter valve port)]. This is exptamearas probably being due to the "jet action" at low ratios of lift to diameter. Figure 9-14 shows the results of some tests on flow through poppet valves. In these results, the coefficient of efflux is defined as the ratio of the observed mean velocity through the valve to the mean velocity that would theoretically result from a pressure drop equal to that across the valve. Thus valve lifts somewhat less than $h=0.25 d_{1}$ may be used without serious impairment of the flow $Q(=A V)$, because as the area of opening through the valve is decreased by decreasing the lift, the coefficient of efflux and hence the actual velocity is increased. In practice, it may be desirable to make the lift considerably


Fig. 9-14.-Effect of valve lift on coefficient of efflux. (From NACA Tech. Rept. No. 24.) less than $h=0.25 d_{1}$ in order to reduce noise and acceleration forces on the valve gear.

The mean velocity of the gas through the valve port may be calculated by the relation

$$
\begin{equation*}
V_{v}=V_{p} \frac{A_{p}}{A_{v}} \tag{9-24}
\end{equation*}
$$

where $V_{v}=$ mean velocity of the gas through the valve port, f.p.s.
$V_{p}=$ mean piston speed, f.p.s. $(=2 \times$ stroke in feet $\times$ r.p.s.).
$A_{v}=$ net area of the valve port, sq. in.
$A_{p}=$ area of the piston, sq. in.
Equation (9-24) is a convenient way of relating velocity and valve size, but it does not take into account the effect of numerous factors such as pressure surging, back pressure on the exhaust, effectiveness of scavenging, compression ratio, and supercharging. However, a knowledge of usual mean velocity values aids in approximating the probable valve size that should be used.

Figure 9-15 shows the effect of gas velocity and valve size on power output on a small engine. Usual mean gas velocities through inlet valves of nonsupercharged aircraft engines of conventional design and corresponding brake mean effective pressures are shown in Fig. A1-8.


Fig. 9-15.-Effect of valve size on brake horsepower. (From Pomeroy as reported in Judge, "Automobile and Aircraft Engines.")

9-8. Valve Details.-Valves are usually formed from steel rod by upsetting. Flat- and spherical-head mushroom shapes may be used, but for aircraft engines, concave or so-called tulip heads are more common (Fig. 9-1). This dishing of the head serves to lighten the valve and possibly reduce its tendency to warp. However, the metal should be sufficient in section to provide the necessary thermal path to the stem and to provide sufficient strength against any tendency for the spring to pull the valve into the port. The valve should not appreciably overhang the seat, as the thin section at this point is exposed to the hot combustion gases on three sides and can easily be overheated.

The head should be joined to the stem by a large-radius fillet to avoid the excessive stress incident to the reentrant corner as well as to provide a more direct path for heat flow to the stem. Screw-driver slots and spanner holes for valve-grinding purposes are objectionable because they provide added area for heat absorption and act as obstructions to the heat flow in the metal. A rubber suction cup on the valve-grinding tool eliminates the
need for slots and spanner holes in the head. In general, the shape of the valve head should be such that it will absorb the least heat both from the gases in the combustion chamber and from the feed back of heat from the gases in the exhaust pipe.

When tulip-shaped heads are used, the rim of the head should be thick enough to carry the heat circumferentially and dissipate it gradually in event of poor seating on one side. Exposed thin sections should be avoided as they are apt to be the source of fine failure cracks following overheating.
, Valve stems should be sufficiently large in diameter to provide an adequate thermal path for the heat that is transferred to the valve guides. A valve-stem diameter of about one-fourth the valve-port diameter fairly well represents current practice, but in high-powered engines, this may be insufficient to prevent overheating and subsequent elongation of the stem. A larger diameter of valve stem tends to obstruct the flow of gas through the port, and the usual alternative is to use a hollow stem filled with a salt or metallic sodium. At operating temperatures, the fused salt or metal is thrown back and forth in the stem and transfers the heat by convection. Saltor sodium-cooled valves are quite effective, but they are more expensive than solid-steel valves. Hence, they are generally used only in the more critical exhaust valves (Fig. 9-1).

In aircraft-engine practice, valve-spring retainers are usually held in place by split taper collars which fit in grooves in the valve stem (Fig. 9-1). These grooves should be shallow and have fillets in reentrant corners to avoid undue stress in the stem. Even with squared ends, valve springs seldom exert the same pressure at all points around the spring retainer. This unequal pressure tends to bend the valve stem and cause binding and more rapid wear of the stem


Fig. 9-16.-Effect of unequal spring pressure on retainer ( $P_{1}>P_{2}$ ). Excessive wear at $A_{1}$ and $A_{2}$. Unequal valve seating at $B_{1}$ and $B$ g tends to bend stem or impair efficiency. (Diagram exaggerated.) and guide (Fig. 9-16). Jardine and Jardine ${ }^{12}$ suggest the use of a spherical seat between the valve-spring retainer and the split collar as a means of controlling this trouble. A shallow
groove for a snap ring is sometimes machined in the valve stem between the top of the valve guide and the valve-spring retainer to keep the valve from falling into the cylinder and doing mechanical damage in event of spring breakage.

Aluminum alloys used for cylinder heads are not suitable for valve seats, and usual practice is to use inserts of cast or wrought aluminum bronze* (Par. 9-3). Inserts are sometimes cast in place, but the difficulty of holding them accurately in position during casting of the head is an objection. More often the inserts are screwed and shrunk or simply shrunk in place in the finished casting. Regardless of the method of putting them in, it is highly important that a good thermal contact be had at all times between the inserts and the surrounding head metal. To ensure this condition, the difference in temperature between the head and insert should be large during insertion so that difference in coefficient of expansion of the two metals will not cause the insert to get loose during operation. The insert may be cooled in liquid air just before insertion or the head can be heated. Swan ${ }^{15}$ recommends a head temperature of 320 to $350^{\circ} \mathrm{C}$. for insertion, a shrinkage interference of 0.0035 in . per inch diameter of the insert, and an insert thickness of about 0.4 in . Too thin a section of head metal around the insert may result in distortion and partial pulling away around part of the insert. Poor arrangement of fins for uniform heat flow from the insert can also contribute to warping and poor thermal contact. Slight peening of the metal around the insert helps remove the possibility of the insert getting loose under extremely adverse conditions and doing mechanical damage.

Aluminum-alloy head metals are also not suitable for valve guides chiefly because of poor wearing qualities. Adequate and effective lubrication between valve stems and guides is difficult to attain, and to reduce wear, hard alloys of aluminum bronze or other materials (Par. 9-3) are usually used. Good thermal contact between the guide and head metal is essential and may be attained by shrink fits, but the desirability of being able to replace worn guides makes this type of fit objectionable. Guides are usually held in place by means of a shoulder resting on the head metal and forming the support for one end of the: valve spring. Valve guides should not extend into the port

[^13]appreciably beyond the head metal as unequal heating and resulting warpage may bind the valve stem. Split-valve guides are sometimes used to permit oversize valve tips that have a greater bearing area. . Clearance between the valve guide and valve stem should be small to minimize leakage of gas due to difference in pressure at opposite ends of the guide.

9-9. The Combustion Chamber.-Since the clearance or combustion-chamber volume is related to the piston displacement and compression ratio by the expression

$$
V_{D}+V_{C}=C R
$$

the volume of the combustion chamber may be expressed as

$$
\begin{equation*}
V_{C}=\frac{V_{D}}{C R-1}=\frac{\pi d^{2} S}{4(C R-1)} \tag{9-25}
\end{equation*}
$$

where $V_{c}=$ combustion chamber volume, cu. in. $V_{D}=$ piston displacement, cu. in.
$C R=$ compression ratio.
$d_{N}=$ cylinder diameter, in.
$S=$ stroke, in.
The shape of the combustion chamber has much to do with the effectiveness of a given design, ${ }^{14}$ and in automotive engines, recent practice has been to use a more or less elongated chamber with the part farthest from the spark plug flattened to produce a narrow space between the piston and head (Fig. 9-17F). During burning, the charge ignites at the spark-plug points and the flame spreads through the mixture as an approximately spherical front of rapidly increasing radius proportional to the flame speed through the mixture. The flame front is not strictly spherical owing to the distorting effect of turbulence and the chilling of the part of the charge closest to the combustion chamber walls, but this does not alter the basic idea of combustion control.

At the beginning of combustion (Fig. 9-18A), the mixture is at compression pressure and temperature, but as the flame spreads through the charge, the burning portion expands and compresses the unburned portion ahead of the advancing flame front (Fig. $9-18 B)$. Since this compression is very rapid, the temperature of the unburned portion also rises rapidly, and if it reaches its spontaneous ignition temperature before the advancing flame
can reach it and burn it, the last portion of the charge will ignite spontaneously with a resulting very rapid liberation of heat. This extremely rapid heat liberation produces a pressure rise much more rapid than that resulting from normal combustion. This is the usual explanation of the phenomenon known as


Frg. 9-17.-Combustion-chamber and valve arrangements.


B

Fig. 9-18.-Basic idea of combustion in gasoline-engine cylinders (see text).
detonation, and its adverse effect on bearings, pistons, valves, and power output is well known.

Chilling the last portion of the charge helps to reduce detonation by reducing the rate of temperature rise, and this in turn reduces the amount of charge that will reach its spontaneous ignition temperature. Flattening the space occupied by the last portion of the charge (Fig. 9-17F) increases the surface-
volume ratio of this part of the combustion chamber and thereby increases heat flow from this part of the mixture. Close proximity of the relatively cool intake valve (Fig. 9-17C) also helps to reduce the rate of temperature rise of the last portion of the charge. Thus, an elongated combustion chamber is desirable from the standpoint of controlling detonation.

Unfortunately, an elongated combustion chamber reduces the area of flame front during normal combustion, and this reduces the rate of heat liberation and pressure rise. Thus, the net area


Fig. 9-19.-Effect of combustion-chamber shape and flame-front area on rate of pressure rise and maximum pressure.
of the indicator card is reduced (Fig. 9-19), and this lowers the specific power output and efficiency. The effect of combustionchamber shape on rate of pressure rise $d P / d T$ and on maximum pressure ( $\propto$ to maximum temperature) is shown diagrammatically in Fig. 9-20. Case $C$ of this figure is usually conceded to be better than case $A$ or $B$ because the start of pressure rise is less abrupt than case $A$ (i.e., less shock and roughness), and maximum pressure (and temperature) is not so high as in case $B$ (i.e., less tendency to detonate).

A compact combustion chamber shape (Fig. 9-19) will permit a greater flame front area and therefore is desirable for highperformance engines, but higher octane fuels must be used to offset the poorer inherent resistance to detonation. Still more
rapid heat liberation is possible with dual ignition (Fig. 9-19), and the gain in power can be demonstrated by switching from one to both magnetos in flight.

The sphere is the most compact geometric shape, but for a combustion chamber, this would require a concave piston head. A spherical segment permits a flat piston head, and aircraftengine combustion chambers approximating this shape are extensively used (Fig. 9-1) especially in engines using valves set at an angle to the cylinder axis.


A


A


B


B


C

C

Fig. 9-20.-Effect of combustion-chamber shape and flame-front area on pressure variation during combustion.

The volume of a spherical segment having only one base is

$$
\begin{equation*}
V=\frac{\pi h}{6}\left(3 r_{2}^{2}+h^{2}\right) \tag{9-26}
\end{equation*}
$$

where $h=$ altitude of the segment, in.
$r_{2}=$ radius of the base, in.
For combustion chambers, $r_{2}$ should be about equal to the radius of the cylinder barrel, and on this basis, the altitude $h$ needed to provide the necessary combustion-chamber volume may be found by combining Eqs. (9-25) and (9-26).
Thus

$$
4\left(\frac{\pi d^{2} S}{C R-1)}=\frac{\pi h}{6}\left(\frac{3 d^{2}}{4}+h^{2}\right)\right.
$$

from which

$$
h^{3}+0.75 d^{2} h-\frac{1.5 d^{2} S}{(C R-1)}=0
$$

Let

$$
a=0.75 d^{2} \quad \text { and } \quad b=\frac{1.5 d^{2} S}{C R-1}
$$

then

$$
\begin{equation*}
h=\sqrt[3]{\frac{b}{2}+\sqrt{\frac{b^{2}}{4}+\frac{a^{3}}{27}}}+\sqrt[3]{\frac{b}{2}-\sqrt{\frac{b^{2}}{4}+\frac{a^{3}}{27}}} \tag{9-27}
\end{equation*}
$$

Example.-An engine has a cylinder diameter of 4 in ., a stroke of 4.5 in ., and a compression ratio of 5:1. If the combustion chamber is in the shape of a spherical segment, what is the distance along the cylinder axis from the center of the piston head (at T.D.C.) to the inner surface of the cylinder head?

Solution

$$
\begin{aligned}
& a=0.75 \times 4^{2}=12 \\
& { }^{2}-\frac{1.5 \times 4^{2} \times 4.5}{(5-1)}: 27
\end{aligned}
$$

From Eq. (9-27),

$$
\begin{gathered}
h=\sqrt[3]{\frac{27}{2}+\sqrt{\frac{27^{2}}{4}+\frac{12^{3}}{27}}}+\sqrt[3]{\frac{27}{2}-\sqrt{\frac{27^{2}}{4}+\frac{12^{3}}{27}}} \\
h=1.78 \mathrm{in} .
\end{gathered}
$$

Owing to the need for a flat plane for the valve seats, the shape of the valve heads, and the irregular shape of the exposed end of the spark plug, the actual combustion-chamber shape deviates somewhat from a spherical segment. If not taken into account, these detail parts will change the compression ratio, and it is desirable for the preliminary design to estimate the change in volume produced by these parts and correct the clearance volume dimensions accordingly. In any event, it is particularly important to have the compression ratio the same in each of the cylinders.

When the valve stems are parallel to the cylinder axis, the combustion chamber usually approximates a short cylinder, and to permit the use of large valves, the diameter of this cylinder is frequently made greater than the diameter of the cylinder barrel, but the height should not be so small as to reduce too greatly the area of the flame front. A check should also be made to see if mechanical clearance between the valves and piston head is adequate.

Cylinder heads should be sufficiently thick in section (a) to withstand the maximum bursting force at explosion pressure,
(b) to be rigid enough to prevent distortion of valve seats and binding of the valves in the valve guides, and (c) to conduct away adequately the heat absorbed from the combustion gases. In conventional types of heads, rigidity and thermal conductivity are critical; hence, if the head thickness is sufficient for $b$ and $c$, the strength will usually be adequate. The fins on air-cooled cylinder heads act as truss members and contribute greatly to the rigidity as well as to the strength. In spherical-segment types of combustion chambers, therefore, a head thickness sufficient for heat flow will also be adequate for strength and rigidity, but in short cylindrical chambers, the flat top may tend to bow outward under explosion pressure sufficient to distort the valve seats. The case is a close parallel to that of steam boilers wherein stay bolts are needed for flat heads, but not for hemispherical heads. However, since stay bolts cannot be used in cylinder heads, the best alternative is greater external trussing and the use of large-radius fillets at the juncture of the flat and cylindrical portions of the head. The stiffening effect of the manifolds is also quite useful.

Valve location is determined by the size of the valves, arrangement of the valve gear, and cooling factors. In in-line engines, valves set parallel to the cylinder axes can be operated by an overhead camshaft without rocker arms, a factor in favor of simplicity, but usually valve size is restricted to the point where there is a reduction in b.m.e.p. In addition, it is more difficult to provide uniform air cooling all around the valve seats. Multiple valves boost the b.m.e.p. but do not greatly help the cooling of the valve seats, and in addition they add to the complexity of the valve gear. Valves set at an angle appear to be about the best solution for small and medium-size engines and in many instances for large engines as well, since uniform air cooling of seats is improved, larger valves may be used, and push rods and rocker arms do not involve any greater, if as much, complexity as overhead camshafts. There are so many possible arrangements of valves and valve gear, however, that specific rules cannot be laid down, but the designer should be able to justify his particular selection.

Spark-plug location is highly important in elongated combustion chambers designed primarily for detonation control, but in compact chambers little choice is available. In general, dual
spark plugs are located on opposite sides of the head and between the valves. Plug bosses should not be too close to the valve seats, and the seats should not be too close together as the narrow separating section of head metal may be shunted off from the cooling air, be overheated, and crack. Spark-plug points set too far back in elongated bosses may be exposed only to stratified burned charge and give poor ignition characteristics. Poor heat flow from plug bosses can cause overheating of plug points and preignition. Excessive heat flow may cause overcooling and fowling of plug points. S.A.E. standard spark-plug dimensions for use in determining plug-boss details are given in reference 2. Arrangement of cooling fins around the spark-plug boss should be such'as to permit ready access to the plug without undue danger of breaking the fins.

## Suggested Design Procedure

1. Decide upon the type of cylinder construction to be used, and make detailed sectional sketches (to scale) of the proposed arrangement of the parts. Include enough different sections to show the arrangement clearly.

A suggested way of making these sketches is to put them on tracing paper placed over $1 / 4-\mathrm{in}$. cross-sectioned paper. These sketches should be considered as a plan of procedure and as such should be given careful study as they are prepared. Hasty assembly of a "picture" without regard to fitting of parts, logical dimensions, etc., is of little value. Be able to justify details of the arrangement by reference to current practice whenever possible, but do not try to make the sketches detailed finished drawings. They should be the preliminary bird's-eye views.
2. With the desired arrangement of the entire cylinder well fixed in mind, determine the cylinder barrel details, i.e., material, wall thickness, holddown flange dimensions, method of attaching to head, etc.
3. If air-cooled, sclect fin dimensions by reference to Fig. A1-7 or current practice. If liquid cooled, use data in reference 15 or equivalent.
4. For fin dimensions selected, determine percentage of heat to cooling and alter dimensions of fins or use baffles if inadequate.

If fins are more than adequate, a saving in cost of manufacture may be possible by using less effective but more easily constructed fins.
5. Make a detailed dimensioned sectional drawing of the cylinder barrel. Leave space on the drawing for adding the cylinder head.
6. Determine the valve dimensions necessary for adequate breathing capacity.
7. Determine the remaining detailed dimensions of the valves, and make a detailed dimensioned drawing of intake and exhaust valves.

Salt- or sodium-cooled exhaust valves will probably be advisable if the b.m.e.p. is much above 115 to 120 lb . per sq. in.
8. Determine the dimensions of the combustion chamber necessary to give the desired compression ratio.
9. Make detailed dimensioned drawings of the valve guides and valve seats.
10. Make a detailed dimensioned sectional drawing of the cylinder head except the supports and housing for the valve gear.

This drawing should be on the same sheet and a part of the cylinder barrel drawing.
11. Make an assembly drawing of the cylinder (except the supports and housing for the valve gear) on the layout drawing of Suggested Design Procedure, page 24, item 4. Show parts in section whenever such sectioning increases the clarity or legibility of the drawing. Include only principal over-all dimensions. Identify each part of the assembly drawing by a reference number corresponding to the detailed drawing or reference number of that part.
12. When items 1 to 11 have been completed and put in proper form, submit for checking and approval.

## Problems

1. Determine the surface heat transfer coefficient for a cylinder barrel of 4.5 -in. bore, a fin width of 0.5 in ., a fin pitch of 0.3 in ., and a fin thickness of 0.0625 in . Velocity of air past cylinders is $65 \mathrm{~m} . \mathrm{p} . \mathrm{h}$.
2. Determine the over-all heat transfer coefficient $U$ if the cylinder barrel in Problem 1 is of steel and the fins are rectangular in cross section.
3. Determine the over-all heat transfer coefficient for the aluminum Y alloy head fins of the cylinder in Problem 1 for an average fin width of 1.1 in ., a pitch of 0.4 in ., and an average fin thickness of 0.125 in . Assume fin-tip thickness of 0.1 in . and fin-root thickness of 0.15 in . Assume an average head thickness of 0.375 in .
4. Determine the approximate cylinder wall and head temperatures for the cylinder in Problems 1, 2, and 3 if the engine is a 75-b.hp. four-cylinder opposed type.
5. Determine for the engine of the preceding four problems the proportion of the heat supplied which is removed by the cooling fins. Air temperature $80^{\circ} \mathrm{F}$., number of cooling fins on the cylinder barrel 14.
6. What increase in the proportion of heat to cooling could be attained for the engine in Problem 5 if the cylinders were baffled and a baffle pressure drop of 2.25 in . of water was available.
7. Assuming an octane number of fuel such that the cylinder temperatures without baffles as found in Problem 4 are satisfactory, what increase in indicated horsepower per cylinder would be possible with haffles and a baffle pressure drop of 2.25 in . of water? What brake horsepower could the engine develop?
8. Take necessary measurements and determine the probable increase in brake horsepower that could be attained in a Continental A-40 engine without increase in cylinder temperatures if pressure baffles giving a 2 -in. pressure drop were used. Assume the most critical conditions will be had at full-throttle climb of $45 \mathrm{~m} . \mathrm{p} . \mathrm{h}$. with 73 octane number fuel in each case.

Assume an atmospheric temperature of $80^{\circ} \mathrm{F}$. The A-40 is rated $40 \mathrm{~b} . \mathrm{hp}$. at 2,575 r.p.m.

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## CHAPTER 10

## VALVE GEAR

10-1. Usual Valve Gear Arrangements.-In the conventional four-stroke-cycle engine, movable valves are necessary to allow induction of new charge and removal of burned charge from the cylinder. These valves are usually of the poppet type, although single sleeve valves ${ }^{8}$ are being used to a considerable extent in England. ${ }^{9}$

The motions of the poppet valves are derived from cams on a shaft or shafts driven at one-half crankshaft speed in the case


Frg. 10-1.-Arrangement of the valve gear used on the Continental A-40 L-head engine.
of in-line and $V$-engines and in some radial engines. In the majority of radial engines, however, the valve motions are derived from a cam ring or disk which rotates at much less than one-half of crankshaft speed. Where a camshaft is used, an individual cam is usually provided for each valve, but when a cam disk is used, several cams are provided in each of two races (one race for intake valves and one race for exhaust valves), and each cam operates in succession all valves connected to its race.

One camshaft operating all the intake and exhaust valves is; usual practice in in-line and V-engines, but more than one
camshaft is sometimes used. The camshaft may be located (a) in the crankcase or (b) over the top of the cylinder heads. In the first case (Figs. 10-1 and 10-2), an L-head arrangement may be used and the valve tips may ride directly on the cams or more often seat on cam-follower tappets, or overhead valves may be used and the motion of the valves transmitted through cam followers, push rods, and rocker arms. In the second case


Fig. 10-2.-Arrangement of the valve gear used on the Franklin 50-hp. valve-inhead engine.
(Figs. 10-3 and 10-4), the overhead cams may act directly against the valve tips, or more often rocker arms transmit the motion. This last arrangement increases the complexity of the valve gear but permits the use of larger valves set at an angle to the center line of the cylinder. Usually, the overhead camshaft is driven from the crankshaft through bevel gearing and a torque tube, but in a few cases a positive chain drive is used. Overhead camshafts operating directly on the valve stems are particularly well adapted to high-speed operation because the weight of parts that must be returned by the valve spring is less than with rocker arms and push rods. With inclined valves and rocker arms


Frg. 10-3.-Arrangement of the valve gear used on the Hispano-Suiza, model-H engine.


Fig. 10-4.-Arrangement of the valve gear used on the Ranger inverted aircooled engines.
(Fig. 10-4), the weight is somewhat greater, but still low enough to permit high-speed operation, and the arrangement has the added advantage of permitting larger valves and higher volumetric efficiency. A disadvantage of overhead camshafts is the need for greater cylinder rigidity to keep the camshaft bearings aligned. Also, with air-cooled types, some difficulty may be encountered in designing the camshaft housing to permit adequate cooling-air flow around the cylinder head.


Fig. 10-5.-Usual valve-gear arrangement for radial engines.
In radial engines, push rods and rocker arms are about the only feasible way of transmitting the motion of the cam followers to the valves. Usually, all intake-valve followers ride on one cam race and all exhaust-valve followers ride on an adjacent race which is attached to or is a part of the same cam disk or ring (Fig. 10-5).

10-2. Valve Timing.-The opening and closing of the intake and exhaust valves at the proper point in the cycle has much to do with the effective performance of a four-stroke-cycle engine,
and the proper point is usually not the dead-center position of the piston. Reasons for this may be shown diagrammatically by means of pumping-loop diagrams (Fig. 10-6).

Considering first the effect of exhaust-valve opening time (Fig. $10-6 A, B$, and $C$ ), if the exhaust valve is opened at bottom dead


Fig. 10-6.-Pressure-volume diagrams showing the effects of valve timing.
center as at point $M$ in $A$, the maximum area under the expansion line will be obtained, but the back pressure on the exhaust will be large and the net work of the cycle will be reduced. By opening the exhaust valve early as at point $K$ in $B$, area $K M N$ will be lost but the larger area $M Q N$ representing the reduction
in the work of pushing the exhaust gases out of the cylinder will be saved, the net result being a gain in the net power output. However, if the exhaust valve is opened too early, as at $R$ in $C$, the area $R K N S$ lost under the expansion line will be greater than the saving in work during exhaust as represented by the area TNS. Therefore, the condition $B$ is most desirable.

The effect of varying the exhaust-valve closing time is shown diagrammatically in Fig. $10-6 D$ and $E$. If the exhaust valve is closed before the end of the exhaust stroke, it will start to close even earlier with the result that there will be a pinching or throttling of the flow of burned gases out of the cylinder. This will cause a build up in pressure during the last part of the exhaust stroke and result in a higher pressure in the clearance space at the beginning of the intake stroke. Before any new charge can be drawn in, the burned charge in the clearance space must expand down at least to atmospheric pressure, and the higher the initial clearance pressure, the greater the portion of the suction displacement that will be required for the expanded clearance gases. Thus too early a closing of the exhaust valve tends to reduce the volumetric efficiency $Z / L$.

By closing the exhaust valve after the top dead-center position as in $E$, less pinching of the exhaust gas during the last part of the exhaust stroke will be had and, in addition, use may be made of the "carry-out" effect produced by the kinetic energy of the high-velocity gases passing to the exhaust manifold. This last results in a lowering of the clearance pressure and an increase in the volumetric efficiency.

The effect of varying the intake-valve opening time is illustrated in Fig. 10-6F and $G$. In $F$, the intake valve starts to open after the start of the intake stroke, and since it takes several degrees of crankshaft travel to open the valve completely, during a considerable portion of the intake stroke the incoming charge will be throttled. The result will be a lower pressure in the cylinder, and unless other factors, discussed later, more than offset this effect, compression will start on the following stroke at a pressure well below atmospheric, and this, as shown in $F$, will cause a low volumetric efficiency.

By starting to open the intake valve before top dead center as in $G$, the valve will be more nearly wide open during the suction stroke, and owing to the reduced amount of throttling, a
higher volumetric efficiency will be had. Thus the exhaust valve should close after top dead center, and the intake valve should open before top dead center.
. Obviously, with this timing both valves will be partly open at the same time, and this condition is called valve overlap. At first thought, it would seem that opening the intake valve before the exhaust valve was closed would result in a flow of burned gas back through the intake valve and into the intake manifold where it would have to be returned to the cylinder before any new charge could come in, or the other extreme, i.e., new charge would flow in to the cylinder and on out into the exhaust manifold without being burned. But this will not happen at high throttle settings if the valve overlap is not too great (a) because the inertia of the high-velocity burned gases will cause these gases to continue on out through the exhaust-valve opening even if another means of escape is provided and (b) because the valves are both so nearly closed during this overlap period that very little if any new charge will get into the cylinder far enough to be carried out by the escaping exhaust gases. The inertia of the new charge tends to hold it back, and this further contributes to preventing escape of new charge to the exhaust. A large valve overlap is not conducive to good economy at part-throttle operation, however, because under this condition, the pressure in the intake manifold is quite low, and the tendency for exhaust gas to flow back through the intake valve is increased. A sudden rush of burned gas into the intake manifold is likely to push some new charge back out through the carburetor where it will be lost. Also the new charge which is later taken into the cylinder will be more highly diluted and therefore burn less efficiently.

Intake-valve closing time has a rather major effect on engine performance, and this is illustrated in Fig. 10-6H, $I$, and $J$. In case $H$, the intake valve closes very close to bottom dead center which means that it starts to close well before the end of the suction stroke. Hence the incoming charge will be throttled during the last part of the suction stroke and the pressure in the cylinder will be lowered, or at least there can be no use made of the so-called "ramming effect" which results from the kinetic energy of the high-velocity incoming charge. With the pressure at the beginning of compression well below atmos-
pheric, the compression line will cross the atmospheric line farther from the end of the card and the volumetric efficiency will be low as in case $H$.

By leaving the intake valve open until well after bottom dead center as in case $I$, the kinetic energy of the incoming charge will tend to "ram" more charge into the cylinder and build up the pressure even though the cylinder volume is starting to decrease by the return of the piston. However, if the intake valve is held open too long after bottom dead center, the volumetric efficiency will be reduced because the returning piston will overcome the inertia of flow or ramming effect of the incoming charge and then start forcing the mixture back out through



Fig. 10-7.-Pressure-volume diagrams showing the effect of exhaust pressure waves on volumetric efficiency. (A) Properly timed wave. ( $B$ ) Improperly timed wave.
the valve port opening as in case $J$. Thus cases $B, E, G$, and $I$ in Fig. 10-6 represent optimum conditions for aircraft engines but not necessarily for all types of engines.

There are several other factors such as manifold pressure waves, the effect of common manifolds to several cylinders, and engine speed, which may alter or even completely change the engine performance that would be expected from the above optimum cases. For instance (Fig. 10-7A and B), the sudden outrush of burned gas from the cylinder when the exhaust valve opens sets up pressure waves in the exhaust pipe that have a frequency and amplitude dependent upon the diameter, length, turns, and branches of the exhaust pipe and upon the speed of the engine. If these waves are traveling away from the cylinder at the time the exhaust valve is closing, they will tend to reduce the pressure in the clearance space, as in case $A$, and therefore contribute to high volumetric efficiency. But if the waves are traveling toward the cylinder, i.e., building up pressure
at the inner end of the manifold, they ram some of the escaped gases back into the cylinder and raise the pressure in the clearance space, as in case $B$. As far as volumetric efficiency is concerned, case $A$ in Fig. 10-7 will produce results similar to case $E$ in Fig. 10-6, and case $B$ in Fig. 10-7 will produce results similar to case $D$ in Fig. 10-6. Thus changing to the correct valve timing while retaining an improper manifold or engine speed can result in no improvement or even a reduction in volumetric efficiency. In a similar. way, improper intake manifolding can offset good intake-valve timing.

In branched manifolds or manifolds leading to a common header, the pressure waves due to one cylinder can be properly timed for that cylinder and yet cause adverse affects in other cylinders.

A given optimum valve timing is in general correct for only one engine speed. The most pronounced effect of speed occurs in connection with intake-valve closing time. The principal reason for this lies in the fact that ramming effect varies with speed, whereas the intake-valve closing time remains fixed in conventional engines. At low speeds, the ramming effect is small and the returning piston can quickly overcome the inertia of inrushing gas. Hence, a valve timing such as case $I$ in Fig. 10-6 may be too late a closing for the low-speed condition and the volumetric efficiency will be low as in case $J$.

A very high engine speed will in general givé a correspondingly high ramming effect which will be overcome less quickly by the returning piston. Thus at high speed, case $l$ (Fig. 10-6) will represent too early a closing time for the intake valve and the volumetric efficiency will be low as in case $H$.

Obviously it would be desirable to vary the intake-valve closing time with speed, but since this is impracticable except in experimental engines, the fixed valve timing used must be a compromise.

In automobile engines requiring good performance over a wide range of speed, a valve timing such as case I, Fig. 10-6, is the usual compromise because it gives reasonably good average volumetric efficiency throughout the speed range. In airplanes and in racing engines, however, high power at high engine speed is essential and high power at low engine speed is of secondary importance. Hence the intake-valve closing time should be
farther after bottom dead center. Figure $10-8$ shows the variation of volumetric efficiency with engine speed for a fixed valve timing. Table 10-1 gives the valve timing of 18 aircraft engines


Fig. 10-8.-Volumetric efficiency vs. engine speed for ( $A$ ) good power over a wide range of speed and ( $B$ ) maximum power at high speed.
together with a summary of average, maximum, and minimum timings.

Table 10-1.-Aircraft-engine Valve-timing Data

| Engine type | I.V.O. deg. B.T.C. | I.V.C. deg. A.B.C. | $\begin{aligned} & \text { E.V.O. deg. } \\ & \text { B.B.C. } \end{aligned}$ | E.V.C. deg. A.T.C. |
| :---: | :---: | :---: | :---: | :---: |
| 9 cyl. radial. . | 26 | 76 | 71 | 31 |
| 14 cyl 2-row radial. | 20 | 76 | 76 | 20 |
| 7 cyl. radial..... | 5 | 55 | 55 | 5 |
| 7 cyl . radial. | 8 | 45 | 55 | 8 |
| 7 cyl . radial. | 8 | 21 | 63 | 20 |
| 7 cyl. radial. | 9 | 51 | 51 | 9 |
| 5 cyl. radial. | 35 | 90 | 80 | 45 |
| 7 cyl. radial. | 41 | 94 | 91 | 54 |
| 5 cyl. radial. | 10 | 77 | 69 | 33 |
| 9 cyl radial. | 15 | 45 | 60 | 15 |
| 4 cyl . in-line. | 17 | 77 | 50 | 10 |
| 12 cyl . V. | 15 | 65 | 70 | 30 |
| 7 cyl. radial. | 10 | 60 | 60 | 10 |
| 3 cyl. radial. . | 4 | 57 | 45 | 19 |
| 2 cyl. opposed. | 5 | 55 | 55 | 5 |
| 4 cyl. opposed. | 10 | 55 | 55 | 10 |
| 4 cyl. in-line. | 14 | 68 | 42 | 22 |
| 5 cyl. radial. | 0 | 60 | 60 | 0 |
| Average. . | 14 | 59 | 62 | 19 |
| Maximum. | 41 | 94 | 91 | 54 |
| Minimum . | 0 | 21 | 42 | 0 |

[^14]10-3. Valve Cams and Followers.-The requirements for valve cams are somewhat conflicting in that for high volumetric efficiency the valves should be opened and closed quickly and held wide open for a large part of the open time, whereas to keep. down acceleration forces and spring tension, the valves should be opened and closed gradually. In addition, the cam contours should be such that they are not too difficult or expensive to manufacture.

Many types of cam contours have been tried in the attempt to attain more fully the best compromise conditions; but the majority of cams now in current use fall into one of the following classifications:

1. Tangent cams with roller or round-nose followers.
2. Convex flank or "mushroom" cams with flat followers in sliding contact.
3. Concave-flank (hollow-faced) cams with roller followers.
4. Constant-acceleration cams, generated cams, etc., having component parts formed of curves other than straight lines or arcs of circles. Only the first three types will be analyzed here. For details of types 4, see references 1 and 2. Some manufacturers use composite curves made up to meet special requirements.

All cams have in common a base circle on which the follower rides during the time the valve is closed, an opening flank so shaped as to open the valve in the desired way, a cam nose which may include a period of dwell on which the follower rides during the time when the valve is wide open, and a closing flank which allows the valve to close properly. The problem of design is largely one of properly shaping the flank and nose portions of the cam.

10-4. Tangent Cams.-Tangent cams are frequently used in in-line and V-engines, usually with roller followers, although a round-nose sliding follower may be used. They have straightline flanks tangent to the base and nose circles and are relatively easy to lay out and manufacture, but they require a stiff valve spring to ensure contact of the follower with the cam surface at all points. Figure 10-9 shows the general layout of a tangent cam with a roller follower.

For the tangent cam (Fig. 10-9), let
$R_{B}=$ the radius of the base circle.
$R_{N}=$ the radius of the nose circle.
$R_{F}=$ the radius of the roller follower.


Fig. 10-9.-Tangent cam with roller follower on straight flank portion $M X$ and on nose circle $M_{Y}$.
$\alpha=$ one-half of the angularmotion of the camshaftfrom initial opening to final closing of the valve ( $\alpha=$ one-fourth of the angular travel of the crankshaft for a ratio of camshaft to crankshaft speed of 1:2).
$\theta=$ the angular travel of the camshaft from initial opening, i.e., the point of tangency of the flank and base circle.
$\phi=$ the angle between a line through the centers of the base and follower circles and a line through the centers of the base and nose circles.
$L_{x}=$ the lift of the follower corresponding to $\theta$, in.
$L_{Y}=$ the lift of the follower corresponding to $\phi$, in.
$L_{M}=$ the maximum lift of the cam follower.
$\delta=$ the angle between a line through the centers of the base and follower circles and a line through the centers of the nose and follower circles.
$M_{x}=$ instantaneous position of follower center when follower is on the straight flank.
$M_{y}=$ instantaneous position of follower center when follower is on the nose circle.
$M_{1}=$ position of follower center when follower is tangent to base circle and straight flank (i.e., at $T_{1}$ ).
$M_{2}=$ position of follower center when follower is tangent to straight flank and nose circle (ie., at $T_{2}$ ).
$M_{3}=$ position of follower center at maximum lift or when follower is tangent to nose circle and dwell circle.
Referring to Fig. 10-9,

$$
\cos \theta \quad \frac{R_{F}+R_{B}}{R_{F}+R_{B}+L_{x}}-\frac{S}{S+L_{x}}
$$

where $S=R_{F}+R_{B}$ or the lift is

$$
\begin{equation*}
L_{x}=\frac{S}{\cos \theta}-S=S\left(\frac{1}{\cos \theta}-1\right), \text { in } \tag{10-1}
\end{equation*}
$$

The velocity is

$$
=\frac{d L_{x}}{d t}=\left(\frac{d L_{x}}{d \theta}\right)\left(\frac{d \theta}{d t}\right)
$$

but for a given engine speed

$$
\frac{d \theta}{d t}=\frac{\cdot \theta}{\bar{t}}=\frac{2 \pi N}{60}
$$

where $N=$ r.p.m. of the camshaft.

$$
\begin{align*}
& V_{x}=\frac{2 \pi N}{12 \times 60}\left(\frac{d L_{x}}{d \theta}\right)=0.00873 N \frac{d L_{x}}{d \theta}=0.00873 N S \frac{d\left(\frac{1}{\cos \theta}\right)}{d \theta} \\
& V_{x}=0.00873 N S \frac{\tan \theta}{\cos \theta}, \text { ft. per sec. } \tag{10-2}
\end{align*}
$$

The acceleration is

$$
\begin{align*}
& A_{x}=\frac{d V_{x}}{d t}=\frac{d V_{x}}{d \theta}\left(\frac{d \theta}{d t}\right)=\frac{2 \pi N}{60}\left(\frac{d V_{x}}{d \theta}\right)=0.000914 N^{2} S \frac{d}{d \theta}\left(\frac{\tan \theta}{\cos \theta}\right) \\
& A_{x}=0.000914 N^{2} S \frac{\left(1+2 \tan ^{2} \theta\right)}{\cos \theta}, \text { ft. per sec. }{ }^{2} \tag{10-3}
\end{align*}
$$

Inspection shows that the acceleration will increase as long as the follower remains on the straight flank because $\tan \theta$ increases and $\cos \theta$ decreases with increase of $\theta$. Hence the maximum acceleration on the straight flank will occur at the point of tangency $T_{2}$ of the flank and nose circles.

On the nose circle at position $M_{Y}$, Fig. 10-9, the lift will be

$$
L_{X}=O M_{Y}-S
$$

where $S=R_{F}+R_{B}$, but

$$
O M_{Y}=h \cos \phi+i \cos \delta
$$

where $h=O P$ and $i=R_{N}+R_{F}$. (Note: $O P$ need not equal $R_{B}$ as shown in Fig. 10-9.) But from the right triangle $P Q M_{Y}$

$$
\left(i^{2}-P Q^{2}\right)^{3 / 2}=Q M_{Y}=i \cos \delta
$$

and

$$
P Q=h \sin \phi
$$

therefore

$$
\begin{align*}
i \cos \delta & =\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{1 / 2} \\
L_{Y} & =h \cos \phi+\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{3 / 2}-S \tag{10-4}
\end{align*}
$$

where $L_{Y}=$ lift, in.
By the same procedure as above (since $d \phi=-d \theta$ ), the velocity is

$$
\begin{align*}
V_{Y^{\prime}} & =\frac{-2 \pi N}{12 \times 60} \times \frac{d L_{Y}}{d \phi}=-0.00873 N \frac{d}{d \phi} \\
& =-0.00873 N\left[-h \sin \phi-\frac{h^{2} \sin \phi \cos \phi}{\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{32}}\right] \\
& =0.00873 N h \sin \phi\left[1+\frac{h \cos \phi}{\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{32}}\right.
\end{align*}
$$

where $V_{Y}$ is in ft . per sec.
The acceleration on the nose circle is

$$
\begin{align*}
& A_{Y}=+\frac{d V_{Y}}{d t}=-\frac{2 \pi N}{60} \times \frac{d V_{Y}}{d \phi}=-0.000914 N^{2} h \frac{d}{d \phi} \\
& {\left[\sin \phi\left(1+\frac{h \cos \phi}{\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{\frac{3 i}{2}}}\right)\right]} \\
& \left(i^{2}-h^{2} \sin ^{2} \phi\right)^{1 / 2} h\left(-\sin ^{2} \phi+\cos ^{2} \phi\right) \\
& -h \sin \phi \cos \phi\left(-\frac{h^{2} \sin \phi \cos \phi}{\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{3 / 2}}\right) \\
& A_{Y}=-0.000914 N^{2 h}\lfloor\cos \phi+ \\
& \left(i^{2}-h^{2} \sin ^{2}{ }^{2}\right. \\
& A_{Y}=-0.000914 N^{2} h \\
& {\left[\cos \phi+\frac{h \cos 2 \phi}{\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{3 / 2}}+\frac{h^{3} \sin ^{2} 2 \phi}{4\left(i^{2}-h^{2} \sin ^{2} \phi\right)^{3 / 2}}\right] \text {, ft. per sec. }{ }^{2}} \tag{10-6}
\end{align*}
$$

When the valve is wide open, $L_{Y}=L_{3}=$ maximum lift, $\phi=0$, and Eq. (10-6) reduces to

$$
\begin{equation*}
A_{3}=-0.000914 N^{2} h\left(1+\frac{h}{i}\right) \tag{10-7}
\end{equation*}
$$

To ensure adequate clearance, the cam base circle is usually about $1 / 8$ in. larger in diameter than the camshaft. The diameter of the camshaft is determined from stiffness requirements (see Par. 10-15), and the diameter of the cam disk in radial drives is a matter of adequate clearance for driving gears (see Pars. 10-9 and $10-10$ ), but for the moment, if it is assumed that the base-.


Frg. 10-10.-Relation of various parts in a tangential cam.
circle diameter is known, the other tangential cam dimensions may be found as follows:

Referring to Fig. 10-10 and using the same nomenclature as in Fig. 10-9,

$$
O P=h, \quad \text { and } \quad h \cos \alpha=R_{B}-R_{N}
$$

also

$$
h+R_{N}=L_{M}+R_{B}
$$

and solving simultaneously for $R_{N}$

$$
\left(L_{M}+R_{B}-R_{N}\right) \cos \alpha=R_{B}-R_{N}
$$

or

$$
\begin{equation*}
R_{N}=R_{B}-\left(\frac{L_{M S} \cos \alpha}{1-\cos \alpha}\right) \tag{10-8}
\end{equation*}
$$

and with $R_{N}$ known, the position of the nose circle center may be
found from

$$
h=\begin{gather*}
R_{B}-R_{N}  \tag{10-9}\\
\cos \alpha
\end{gather*}
$$

From Fig. 10-10, it is seen that

$$
\begin{equation*}
\theta_{M}=\arctan \frac{h \sin \alpha}{R_{F}+R_{B}} \tag{10-10}
\end{equation*}
$$

When the angle of crankshaft travel from initial opening to final closing of a valve is quite large or when it is desired to hold the valve wide open for a part of the open time in order to reduce throttling of the charge through the valve port to a minimum and thereby raise the volumetric efficiency, a "period of dwell" is built into the cam (Fig. 10-11). This period of dwell is an arc of a circle concentric with the base circle and having a radius equal to the radius of the base circle plus the total lift, i.e.,

$$
\text { Radius of dwell }=R_{B}+L_{M}
$$

The period of dwell is somewhat arbitrary with the designer, but it is limited by the capacity of the valve spring and to a lesser


Fig. 10-11.-Tangential cam with a period of dwell. extent by the allowable stress at the line of contact between the cam and roller follower.

Referring to Fig. 10-11, the distance between the centers of the base and nose circles is

$$
O P=h \quad \text { and } \quad h \cos (\alpha-\sigma)=R_{B}-R_{N}
$$

also

$$
L_{M}+R_{B}=h+R_{N}
$$

and solving simultaneously for $R_{N}$

$$
\left(L_{M}+R_{B}-R_{N}\right) \cos (\alpha-\sigma)=R_{B}-R_{N}
$$

from which

$$
\begin{equation*}
R_{N}=R_{B}-\frac{L_{M}}{1}-\frac{\cos (\alpha-\sigma)}{\cos (\alpha-\sigma)} \tag{10-11}
\end{equation*}
$$

With $R_{N}$ known, the position of the nose circle center may be found from

$$
\begin{equation*}
h=\frac{R_{B}-R_{N}}{\cos (\alpha-\sigma)} \tag{10-12}
\end{equation*}
$$

From Fig. 10-11. it is seen that

$$
\begin{equation*}
\theta_{M}=\arctan \frac{h \sin (\alpha-\sigma)}{R_{F}+R_{B}} \tag{10-13}
\end{equation*}
$$

10-5. Example of Tangent-cam Calculations.-Determine dimensions and accelerations for a tangent cam to operate an inlet valve on an in-line engine, (a) for zero dwell, and (b) for a period of dwell angle of 20 deg . of camshaft travel. Available data are as follows: inlet-valve opening, 15 deg . before top center; inlet-valve closing, 65 deg. after bottom center; maximum lift, 0.5 in .; diameter of camshaft, 1.575 in .; diameter of the roller follower, 1 in .; speed of engine, 2,000 r.p.m.

Procedure a.-Using the nomenclature of the preceding article,

$$
\begin{aligned}
R_{B} & =\frac{1.575}{2}+\frac{0.125}{2}=0.85 \mathrm{in} \\
L_{M} & =0.5 \mathrm{in} . \\
\alpha & =\frac{15+180+65}{4}=65 \mathrm{deg} .
\end{aligned}
$$

From Eq. (10-8),

$$
R_{N}=0.85-\frac{0.5 \times \cos 65}{1-\cos 65}=0.85-\frac{0.5 \times 0.4226}{1-0.4226}=0.484 \mathrm{in} .
$$

From Eq. (10-9),

$$
h=\frac{0.85-0.484}{0.4226}=0.865 \mathrm{in} .
$$

From $\cdot$ Eq. (10-10),

$$
\begin{aligned}
& \theta_{M}=\arctan \frac{0.865 \sin 65}{0.5+0.85}=\arctan 0.581=30^{\circ} 9.5^{\prime} \\
& \phi_{M}=65^{\circ}-30^{\circ} 9.5^{\prime}=34^{\circ} 50.5^{\prime}
\end{aligned}
$$

From Eq. (10-3), the maximum acceleration on the straight flank is

$$
\begin{aligned}
A_{x M} & =A_{2}=0.000914 \times\left(\frac{2,000}{2}\right)^{2}(0.5+0.85) \frac{\left[1+2\left(\tan 30^{\circ} 9.5^{\prime}\right)^{2}\right]}{\cos 30^{\circ} 9.5^{\prime}} \\
A_{2} & =2,395 \mathrm{ft} . \text { per sec. }{ }^{2}
\end{aligned}
$$

For the deceleration when $\phi=0$, from Eq. (10-7),

$$
\begin{gathered}
i=R_{N}+R_{F}=0.484+0.5=0.984 \mathrm{in} . \\
A_{Y_{M}}=A_{3}{ }^{\cdot}=-0.000914 \times\left(\frac{2,000}{2}\right)^{2} \times 0.865\left(1+\frac{0.865}{0.984}\right) \\
=-1,485 \mathrm{ft} . \text { per sec. }{ }^{2}
\end{gathered}
$$

Procedure b.-For the cam with the 20-deg. period of dwell,

$$
\begin{aligned}
R_{B} & =0.85 \mathrm{in} . \\
L_{M} & =0.5 \mathrm{in} . \\
\sigma & =10 \mathrm{deg} . \\
\alpha-\sigma & =65-10=55 \mathrm{deg} .
\end{aligned}
$$

From Eq. (10-11),

$$
R_{N}=0.85-\frac{0.5 \cos 55}{1-\cos 55} \quad 0.85-\frac{0.5 \times 0.5736}{1-0.5736} \quad 0.179 \mathrm{in}
$$

From Eq. (10-12),

$$
\begin{gathered}
h \quad 0.85-0.179 \\
0.5736
\end{gathered}=1.17 \mathrm{in}
$$

From Eq. (10-13),

$$
\begin{aligned}
& \arctan \frac{1.17 \sin 55}{0.5+0.85}=\arctan 0.71=35^{\circ} 22.5^{\prime} \\
\phi_{M} & : 55^{\circ}-35^{\circ} 22.5^{\prime}=19^{\circ} 37.5^{\prime}
\end{aligned}
$$

From Eq. (10-3), the maximum acceleration on the straight flank is

$$
\begin{aligned}
A_{x M A} & =A_{2}=0.000914\left(\frac{2,000}{2}\right)^{2}(0.5+0.85) \frac{\left.\left[1+2\left(\tan 35^{\circ} 22.5^{\prime}\right)\right)^{2}\right]}{\cos 35^{\circ} 22.5^{\prime}} \\
A_{2} & =3,040 \mathrm{ft} . \text { per sec. }{ }^{2}
\end{aligned}
$$

From Eq. (10-7) for $i=R_{N}+R_{F}=0.179+0.5=0.679$

$$
\begin{aligned}
& A_{3}=-0.000914\left(\frac{2000}{2}\right)^{2} 1.17\left(1+\frac{1.17}{0.679}\right) \\
& A_{3}=-2,915 \mathrm{ft} . \text { per sec.2 }
\end{aligned}
$$

However, for rapid valve deceleration, Eq. (10-7) will not give the maximum deceleration and Eq. (10-6) should be used to find the maximum value. Thus substituting various values of $\phi$ in Eq. (10-6) and solving for $A_{Y}$, the deceleration is found to be a maximum when $\phi=\phi_{M}=19^{\circ} 37.5^{\prime}$, at which value $A_{Y}=3,920 \mathrm{ft}$. per sec. ${ }^{2}$

From this, it is evident that increase in volumetric efficiency by using a period of dwell is attained at the expense of greater stress at the line of contact between the cam and roller during acceleration and greater spring loading during deceleration. For the example, the increase in stress during acceleration will be $[(3,040-2,395) / 2,395] \times 100=27$ per cent, and at the fullopen position, the increase in spring loading will be

$$
[(2,915-1,485) / 1,485] \times 100=96.2 \text { per cent. }
$$

However, since the maximum deceleration occurs in case $b$ when the lift is 0.309 in ., a fairer comparison would be to note the
increase in loading over case $a$ at a lift of 0.309 in. For case $a$ at a lift of 0.309 in., from Eq. (10-4)

$$
0.309=0.865 \cos \phi+\left(0.984^{2}-0.865^{2} \sin ^{2} \phi\right)^{3 / 2}-1.35
$$

or

$$
\phi=28^{\circ} 30^{\prime}
$$

and from Eq. (10-6), the deceleration on the nose circle is

$$
\begin{aligned}
& A_{Y}=-0.000914\left(\frac{2,000}{2}\right)^{2} 0.865 \\
& \qquad \begin{array}{c}
{\left[\cos 28^{\circ} 30^{\prime}+\frac{0.865 \cos 57^{c}}{\left(0.984^{2}-0.865^{2} \sin ^{2} 28^{\circ} 30^{\prime}\right)^{3 / 2}}\right.} \\
\left.\quad+\frac{0.865^{3} \sin ^{2} 57^{\circ}}{4\left(0.984^{2}-0.865^{2} \sin ^{2} 28^{\circ} 30^{\prime}\right)^{3 / 2}}\right]
\end{array} \\
& \quad A_{Y}=-1,240 \text { ft. per sec. }{ }^{2}
\end{aligned}
$$

The increase in spring loading is

$$
\frac{2,915-1,240}{1,240} \times 100=135 \%
$$

Thus the use of a period of dwell is limited first by the ability of the spring to keep the follower on the cam.


Frg. 10-12.-Layout of the tangential cams in the Example of Par. 10-5.
Figure 10-12 shows the layout of the cams, and Figs. 10-13 and $10-14$ show the lifts, velocities, and accelerations for the tangent cams of the example (Par. 10-5).

10-6. Mushroom Cams.-Mushroom cams derive their name from the mushroom-shaped sliding follower which usually has a flat surface in contact with the cam. This type of cam, which is extensively used in automotive practice, differs from the


Frg. 10-13.-Lift, velocity, and acceleration curves for the tangent cam, Case (a), Par. 10-5.


Fig. 10-14.-Lift, velocity, and acceleration curves for the tangent cam, Case (b), Par. 10-5.
tangential cam in that the flanks are ares of circles tangent to the base and nose circles, respectively. Figure $10-15$ shows the general arrangement of a mushroom cam with a flat-faced sliding follower. In the following analysis, symbols (as apply) are the same as in the analysis of tangential cams. In addition,

$$
R_{F L}=\text { radius of the flank circle. }
$$



Fig. 10-15.-Mushroom cam with flat follower on convex circular-arc flank portion ( $T_{x}$ ).

Referring to Fig. 10-15, for the lift on the flank circle

$$
\begin{aligned}
e+L_{x} & =R_{F L}-R_{F L} \cos \theta \\
e & =R_{F L}(1-\cos \theta)-L_{x}
\end{aligned}
$$

also

$$
e=R_{B}-R_{B} \cos \theta=R_{B}(1-\cos \theta)
$$

eliminating $e$

$$
R_{B}(1-\cos \theta)^{\circ}=R_{F L}(1-\cos \theta)-L_{x}
$$

or

$$
\begin{equation*}
L_{x}=\left(R_{F_{L}}-R_{B}\right)(1-\cos \theta) \tag{10-14}
\end{equation*}
$$

For the velocity on the flank circle,

$$
\begin{align*}
& V_{x}=\frac{d L_{x}}{d t} \quad \frac{d L_{x}}{d \theta} \times \frac{d \theta}{d t}=\frac{2 \pi N}{12 \times 60} \times \frac{d L_{x}}{d \theta}=0.00873 N \frac{d L_{x}}{d \theta} \\
& V_{x}=0.00873 N\left(R_{F L}-R_{B}\right) \sin \theta \tag{10-15}
\end{align*}
$$

For the acceleration on the flank circle,
$A_{x}=\frac{d V_{x}}{d t}=\frac{d V_{x}}{d \theta} \times \frac{d \theta}{d t}=0.000914 N{ }^{2}\left(R_{F \cdot \dot{L}}-R_{B}\right) \cos \theta$
On the nose circle, the lift, velocity, and the acceleration would be similar to that on the nose circle of a tangential cam except for the change from a finite to an infinite radius of the cam
follower. Referring to Fig. 10-16, the lift on the nose circle is

$$
\begin{equation*}
L_{Y}=R_{N}+h \cos \phi-R_{B} \tag{10-17}
\end{equation*}
$$

where $h=O P$, and $\phi=0$ when $L_{Y}=L_{3}\left(=L_{M}\right.$, the maximum lift). The velocity on the nose circle is

$$
\begin{align*}
& V_{Y}=\frac{d L_{Y}}{d t}=\frac{d L_{Y}}{d \phi} \times \frac{d \phi}{d t}=0.00873 N \frac{d L_{Y}}{d \phi} \\
& V_{Y}=0.00873 N h \sin \phi, \text { ft. per sec. } \tag{10-18}
\end{align*}
$$

The acceleration on the nose circle is

$$
\begin{equation*}
1 \cdot-\underset{d t}{d V_{Y}} \quad \frac{d V_{Y}}{d \phi} \times \frac{d \phi}{d t} \quad-0.000914 N^{2} h \cos \phi, \text { ft. per sec. } 2^{2} \tag{10-19}
\end{equation*}
$$

at maximum lift, $\phi=0$ and

$$
\begin{equation*}
A_{Y}=A_{3}=-0.000914 N^{2} h \tag{10-20}
\end{equation*}
$$

As with tangential cams, there are definite relations between the various dimensions and angles of the mushroom cam.


Fig. 10-16.-Mushroom cam with flat-faced follower on the nose-circle portion ( $T_{Y}$ ).


Fig. 10-17.-Mushroom cam with flat-faced follower in contact at the point of tangency of the flank and nose circles.

The radius of the base circle $R_{B}$ is determined from shaft stiffness requirements (see Par. 10-15), the lift $L_{M}$ is determined from valve and volumetric efficiency requirements, and the radius of the nose circle is assumed. Then, the distance between the base circle and nose circle centers, $h(=O P$, Fig. 10-17) is

$$
\begin{equation*}
h=R_{B}+L_{M}-R_{N} \tag{10-21}
\end{equation*}
$$

For the radius of the flank circle (Fig. 10-17),

$$
\begin{align*}
\left(R_{F L}-R_{N}\right)^{2}= & (h \sin \alpha)^{2}+\left(R_{F L}-R_{B}+h \cos \alpha\right)^{2} \\
R_{F L}^{2}+R_{N}^{2}-2 R_{N} R_{F L}= & h^{2} \sin ^{2} \alpha+R_{F L}^{2}+R_{B}^{2}-2 R_{B} R_{F L} \\
& +2 R_{F L} h \cos \alpha-2 R_{B} h \cos \alpha+h^{2} \cos ^{2} \alpha \\
R_{F L}= & \frac{R_{N}^{2}-R_{B}^{2}-h^{2}+2 R_{B} h \cos \alpha}{2\left(R_{N}-R_{B}+h \cos \alpha\right)} \quad \text { (10-22) } \tag{10-22}
\end{align*}
$$

Again from Fig. 10-17, the maximum angular travel of the cam while the follower is on the flank circle is

$$
\begin{align*}
\left(R_{F L}-R_{N}\right) \sin \theta_{M} & =h \sin \alpha \\
\theta_{M} & =\arcsin \left[\frac{h \sin \alpha}{\left(R_{F x}-R_{N}\right)}\right] \tag{10-23}
\end{align*}
$$

and the maximum angular travel of the cam from the point of tangency of the flank and nose circles to the point of maximum lift is

$$
\begin{equation*}
\phi_{M}=\alpha-\theta_{M} \tag{10-24}
\end{equation*}
$$

10-7. Example of Mushroom-cam Calculations.-Determine dimensions and accelerations for a mushroom cam with flat-faced follower to operate an inlet valve on an in-line engine. Available data are as follows: inlet valve opening, 15 deg . before top center; inlet valve closing, 65 deg . after bottom center; maximum lift, 0.5 in.; diameter of camshaft, $1.575^{\circ}$ in.; speed of engine, 2,000 r.p.m.

Procedure.-Using the nomenclature of Par. 10-6 and assuming the diameter of the base circle $=$ diameter of camshaft $+1 / 8 \mathrm{in}$.,
$R_{B}=\frac{1.575}{2}+\frac{0.125}{2}=0.85 \mathrm{in} ., \quad L_{M}=0.5 \mathrm{in} .$,

$$
\alpha=\frac{15+180+65}{4}=65 \mathrm{deg} .
$$

Assume $R_{N}=0.25 \mathrm{in}$. From Eq. $(10-21), h=0.85+0.5-0.25=1.1 \mathrm{in}$. From Eq. (10-22),

$$
R_{F L}=\frac{0.25^{2}-0.85^{2}-1.1^{2}+(2 \times 0.85 \times 1.1 \times 0.4226)}{2[0.25-0.85+(1.1 \times 0.4226)]}=3.99 \mathrm{in} .
$$

From Eq. (10-23),

$$
\theta_{M}=\arcsin \frac{1.1 \times 0.9063}{(3.99-0.25)}=\arcsin 0.2665=15^{\circ} 27.5^{\prime}
$$

From Eq. (10-24),

$$
\phi_{M}=65^{\circ}-15^{\circ} 27.5^{\prime}=49^{\circ} 32.5^{\prime}
$$

The layout of the cam is shown in Fig. 10-18.

From Eq. (10-16), it is evident that the acceleration on the flank circle will be a maximum when $\theta=0$.


Frg. 10-18.-Layout of the mushroom cam in the Example of Par. 10-7.


Fig. 10-19.-Lift, velocity, and acceleration curves for the mushroom cam, Par. 10-7.
For the data of the example,

$$
A_{x M}=0.000914(2,000 / 2)^{2}(3.99-0.85) \cos 0=2,870 \mathrm{ft} . \text { per sec. }{ }^{2}
$$

Other values of $A_{x}$ together with values of $L_{x}$ [calculated from Eq. (10-14)] and $V_{x}$ [calculated from Eq. (10-15)] may be read from Fig. 10-19. From

Eq. (10-19), it is evident that the deceleration on the nose circle is a maximum when $\phi=0$.

For the data of the example [using Eq. (10-20)],

$$
A_{Y M}=A_{3}=-0.000914\left(\frac{2,000}{2}\right)^{2} \times 1.1=-1,006 \mathrm{ft} . \text { per sec. }{ }^{2}
$$

Other values of $A_{Y}$ [calculated from Eq. (10-19)] together with values of $L_{Y}$. [calculated from (Eq. 10-17)] and $V_{Y}$ [calculated from (Eq. (10-18)] may be read from Fig. 10-19.

Comparing Figs. $10-13,10-14$, and $10-19$, it is seen that the initial acceleration for the mushroom cam is higher; hence the initial shock load on the valve gear will be higher. The deceleration loads are not greatly different for the tangent cam with zero dwell and the mushroom cam but with dwell deceleration loads rise rapidly. Mushroom cams are seldom built with a dwell period.


Fig. 10-20.-Hollow-faced cam with roller follower on concave circular-arc flank.
10-8. Hollow-faced Cams.-In the case of radial engines using a cam ring (Par. 10-1), the radius of the base circle $R_{B}$ is quite large relative to the other dimensions. Also the ring rotates at less than one-half of crankshaft r.p.m., hence $\alpha$ is a relatively small angle.

Under these conditions, tangent and mushroom types of cam contours are not sutitable with any appreciable lift because of the excessively small nose-circle radius that can be used; in many instances they are not even possible.

For radial engines using cam disks, therefore, other types of cam profiles should or must be used, and of the possible types, the so-called hollow-faced cam is probably most common. This type of cam (Fig. 10-20) differs from the mushroom cam basically in that it has a concave flank and uses a roller follower.

Referring to Fig. 10-20, from the geometry of the figure,

$$
\begin{aligned}
\frac{O K}{O C} & =\cos \theta \\
O C & =R_{B}+R_{F L} \\
O K & =O M_{x}+M_{x} K \\
O M_{x} & =R_{B}+L_{x}+R_{F} \\
M_{x} K & =\sqrt{M_{x} C^{2}-C K^{2}}=\sqrt{\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta}
\end{aligned}
$$

Hence

$$
\frac{R_{B}+L_{x}+R_{F}+\sqrt{\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta}}{R_{B}+R_{F L}}=\cos
$$

From which the lift on the flank circle is

$$
\begin{array}{r}
L_{x}=\left(R_{B}+R_{F L}\right) \cos \theta-\sqrt{\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta} \\
-\left(R_{B}+R_{F}\right)(10-25)
\end{array}
$$

For the velocity on the flank circle,

$$
\begin{align*}
& \cdot V_{x}=\frac{d L_{x}}{d t}=\frac{d L_{x}}{d \theta} \times \frac{d \theta}{d t}=\frac{2 \pi N}{12 \times \overline{60}} d L_{x} d \theta=\dot{0} .00873 N \frac{d L_{x}}{d \theta} \\
& V_{x}=0.00873 N \frac{u}{d \theta}\left[\left(R_{B}+R_{F L}\right) \cos \theta\right. \\
& \left.-\sqrt{\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta}-\left(R_{B}+R_{F}\right)\right] \\
& =0.00873 N^{\circ}\left\{-\left(R_{B}+R_{F L}\right) \sin \theta\right. \\
& \left.+\begin{array}{c}
\left(R_{B}+R_{F_{L}}\right)^{2} \sin \theta \cos \theta \\
\left(R_{B}+R_{F}\right)^{2}
\end{array}\right) \\
& V_{x}=0.00873 N\left(R_{B}+R_{F_{L}}\right) \sin \theta \\
& \left.\frac{\left(R_{B}+R_{F_{L}}\right) \cos \theta}{\left[\left(R_{F_{L}}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta\right]^{3 / 2}}-1\right\} \tag{10-26}
\end{align*}
$$

For the acceleration on the flank circle

$$
\begin{align*}
A_{x}= & \frac{d V_{x}}{d t}=\frac{d V_{x}}{d \theta} \times \frac{d \theta}{d t}=\frac{2 \pi N}{60} \times \frac{d V_{x}}{d \theta} \\
= & 0.000914 N^{2}\left(R_{B}+R_{F L}\right) \frac{d}{d \theta} \\
& \quad\left(\sin \theta\left\{\overline{\left[\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta\right]^{3 / 2}}-1\right\}\right) \\
A_{x}= & 0.000914 N^{2}\left(R_{B}+R_{F L}\right) \\
& \quad\left(\frac{\left(R_{B}+R_{F L}\right) \cos 2 \theta}{}\right. \\
& \frac{\left.\left(R_{F L}+R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2} \theta\right]^{1 / 2}}{} \\
& \left.+\frac{\left(R_{B}+R_{F L}\right)^{3} \sin ^{2} \theta \cos ^{2} \theta}{\left[\left(R_{F L}-R_{F}\right)^{2}-\left(R_{B}+R_{F L}\right)^{2} \sin ^{2}\right.}-\cos \theta\right\} \quad(10-27) \tag{10-27}
\end{align*}
$$

On the nose circle, the hollow-faced cam with roller follower is the same as the tangent cam with roller follower. Hence for the hollow-faced cam,


Fig. 10-21.-Hollow-faced cam with the roller follower in contact at the point of tangency of the flank and nose circles.
For $L_{Y}$, use Eq. (10- $\dot{4}$ ).
For $V_{Y}$, use Eq. (10-5).
For $A_{Y}$, use Eq. (10-6).

As with tangent and mushroom cams, the parts of hollow-faced cams are definitely related. When applied to radial-engine cam rings, the radius of the base circle $R_{B}$ is no longer determined from shaft-stiffness requirements but instead is based upon the geardrive dimensions (see Par. 10-9). The lift $L_{M}$ is determined from valve and volumetric efficiency requirements, and the radii of the nose circle $R_{N}$ and the roller follower $R_{F}$ are assumed. The angle $\alpha$ is no longer one-fourth of the total valve open time, but is

$$
\begin{equation*}
\alpha=\frac{\text { total valve open time, deg. }}{2 R} \tag{10-28}
\end{equation*}
$$

where $R=\frac{\text { crankshaft r.p.m. }}{\text { cam-ring r.p.m. }}$ [see Par. 10-9 and Eq. (10-34)].
From Fig. 10-21, the distance between the base and nose circle centers, $h(=O P)$, is

$$
\begin{equation*}
h=R_{B}+L_{M}-R_{N} \tag{10-29}
\end{equation*}
$$

For the radius of the flank circle,

$$
E P=h \sin \alpha
$$

also

$$
\begin{align*}
E P & =\left(R_{F L}+R_{N}\right) \sin \delta \\
\sin \delta & =\frac{h \sin \alpha}{\left(R_{F L}+R_{N}\right)} \\
\sin ^{2} \delta & =\frac{h^{2} \sin ^{2} \alpha}{\left(R_{F L}+R_{N}\right)^{2}}  \tag{a}\\
R_{B}-T_{1} E & =O E=h \cos \alpha \\
T_{1} E & =R_{B}-h \cos \alpha  \tag{b}\\
R_{F L}+T_{1} E & =C E=\left(R_{F L}+R_{N}\right) \cos \delta \\
T_{1} E & =\left(R_{F L}+R_{N}\right) \cos \delta-R_{F L} \tag{c}
\end{align*}
$$

Combining (b) and (c)

$$
\begin{align*}
\cos \delta & =\frac{R_{B}+R_{F L}-h \cos \alpha}{R_{F L}+R_{N}} \\
\cos ^{2} \delta & =\frac{\left(R_{B}+R_{F L}-h \cos \alpha\right)^{2}}{\left(R_{F L}+R_{N}\right)^{2}} \tag{d}
\end{align*}
$$

adding ( $a$ ) and (d)

$$
\sin ^{2} \delta+\cos ^{2} \delta=\frac{h^{2} \sin ^{2} \alpha}{\left(R_{F L}+R_{N}\right)^{2}}+\frac{\left(R_{B}+R_{F L}-\hbar \cos \alpha\right)^{2}}{\left(R_{F L}+R_{N}\right)^{2}}
$$

From which

$$
\left(R_{F L}+R_{N}\right)^{2}=h^{2} \sin ^{2} \alpha+\left(R_{B}+R_{F L}-h \cos \alpha\right)^{2}
$$

Solving this expression for the radius of the flank circle gives

$$
\begin{equation*}
R_{F L}=\frac{h^{2}+R_{B}^{2}-R_{N}^{2}-2 R_{B} h \cos \alpha}{2\left(R_{N}-R_{B}+h \cos \alpha\right)} \tag{10-30}
\end{equation*}
$$

Again referring to Fig. 10-21,

$$
\frac{K M_{2}}{E P}=\frac{C M_{2}}{C P}
$$

but

$$
\begin{aligned}
E P & =h \sin \alpha \\
C M_{2} & =R_{F_{L}}-R_{F} \\
C P & =R_{F L}+R_{N}
\end{aligned}
$$

Hence

$$
\begin{equation*}
K M_{2}=\left(\frac{R_{F L}-R_{F}}{R_{F L}+R_{N}}\right) h \sin \alpha \tag{a}
\end{equation*}
$$

Also

$$
\begin{equation*}
\tan \theta_{M}=\frac{K M_{2}}{O K}=\frac{K M_{2}}{(O C-C K)} \tag{b}
\end{equation*}
$$

but

$$
\begin{aligned}
& O C=R_{B}+R_{F L} \\
& C K=C M_{2} \cos \delta=\left(R_{F L}-R_{F}\right) \cos \delta=\sqrt{\left(R_{F L}-R_{F}\right)^{2} \cos ^{2} \delta} \\
& C K=\sqrt{\left(R_{F L}-R_{F}\right)^{2}\left(1-\sin ^{2} \delta\right)}
\end{aligned}
$$

From step (a) in the development of Eq. (10-30),

$$
\sin ^{2} \delta=\frac{h^{2} \sin ^{2} \alpha}{\left(R_{F L}+R_{N}\right)^{2}}
$$

Hence

$$
\begin{equation*}
C K=\sqrt{\left(R_{F L}-R_{F}\right)^{2}\left(1-\frac{h^{2} \sin ^{2} \alpha}{\left(R_{F L}+R_{N}\right)^{2}}\right)} \tag{d}
\end{equation*}
$$

Combining (b), (c), and (d),

$$
\begin{align*}
& K M_{2}=\left\{\left(R_{B}+R_{F L}\right)\right. \\
&\left.\quad-\sqrt{\left(R_{F L}-R_{F}\right)^{2}\left[1-\frac{h^{2} \sin ^{2} \alpha}{\left(R_{F L}+R_{N}\right)^{2}}\right]}\right\} \tan \theta_{M} \tag{e}
\end{align*}
$$

combining ( $a$ ) and (e)

$$
\left.\begin{array}{l}
\theta_{M}=\arctan \tan \\
\left\{\left(R_{B}+R_{F L}\right)-\sqrt{\left(\frac{R_{F L}-R_{F}}{R_{F L}+R_{N}}\right) h \sin \alpha}\right. \\
\sum_{\left.R_{M L}-R_{F}\right)^{2}[1-}^{\left.\left.\overline{\left(R_{F L}+R_{N}\right)^{2}}\right]\right\}} \tag{10-32}
\end{array}\right)
$$

When a period of dwell is used with the hollow-faced cam, Eqs. (10-30), (10-31), and (10-32) may be used by replacing $\alpha$ by ( $\alpha-\sigma$ ) where $\sigma=$ dwell angle/2. As in the case of tangential cams, the period of dwell is somewhat optional, but as the radius of the nose circle $R_{N}$ is reduced, the spring load to keep the follower on the cam increases rapidly [Eq. 10-6]. If $R_{N}$ is maintained large, then the radius of the flank circle $R_{F L}$ is smaller [Eq. (10-30)] and the acceleration on the flank $A_{x}$ increases. Thus the period of dwell is limited either by the allowable spring load or by the stress at the line of contact between the roller follower and the flank circle.


Frg. 10-22.-Schematic arrangement of usual cam-ring drives for radial engines. (A) For opposite rotation of cam ring and crankshaft. (B) For same direction of rotation of cam ring and crankshaft.

10-9. Radial-engine Cam Rings.-Four-stroke-cycle radial engines have an odd number of cylinders per bank to permit even firing, and for such engines, a cam ring containing more than one cam is generally used. Usually two rows of cams are used (one row for intake and one row for exhaust valves), both rows of cams are integral with the same cam ring, and this ring is concentric with and connected by suitable gearing to the crankshaft (Fig. 10-22).

Each intake cam operates the intake valves of all cylinders in succession, and the corresponding action occurs with each exhaust cam. Hence the cam ring must rotate at such a speed that $X$ intake cams operate $Y$ intake valves in two revolutions or 720 deg. of crankshaft travel.

For opposite rotation of cam ring and crankshaft (Fig. 10-23), $\operatorname{cam} A$ is just ready to operate the follower of No. 1 cylinder. Usual cylinder numbering is in succession in the direction of rotation; hence the next cylinder to start the event is No. 3, and


Frg. 10-23.-Radial-engine cam-ring analysis.
the next will be No. 5. But for purposes of this analysis, it is preferable to number the cylinders in the order of firing or cyclic sequence, and this method of numbering is indicated in parentheses adjacent to the usual numbering.

For an engine of $Y$ cylinders (Fig. 10-23), No. (2) valve will start to open $720 / Y$ deg. after the start of No. 1 cylinder, and to be in position to accomplish this, cam $B$ will have to move through an angle of $\Delta$ deg. For $X$ equally spaced cams,

$$
\Delta=\frac{360}{\bar{X}}-\frac{720}{Y}
$$

If there are more than two cams, the third cam will have to move through an angle of $2 \Delta[=(3-1) \Delta]$ to operate valve (3),
and cam $X$ will have to move through an angle of $(X-1) \Delta$ to operate valve $\left(\frac{Y-1}{2}\right)$. When cam $X$ is ready to operate its valve, cam $A$ will also have moved through ( $X-1$ ) $\Delta$ deg.; hence cam $A$ can operate valve $\left(\frac{Y+1}{2}\right)$ by moving an additional angle $\Delta$ or a total motion of $(X-1+1) \Delta=X \Delta$ deg. But this distance that cam $A$ moves from the start of opening valve (1) to the start of opening valve $\left(\frac{Y+1}{2}\right)$ is $\frac{360}{Y}$ or

$$
\frac{360}{Y}=X \Delta=X\left(\frac{360}{X}-\frac{720}{Y}\right)
$$

from which

$$
\begin{equation*}
X=\frac{Y-1}{2} \tag{10-33}
\end{equation*}
$$

When cam $A$ has reached valve $\left(\frac{Y+1}{n}\right)$, all the other cams will be in the same respective position as when cam $A$ started to operate valve (1); hence one row of $X$ cams can operate all the intake valves for $Y$ cylinders, and a parallel row of $X$ cams attached to the same cam ring can operate all the exhaust valves.

In the preceding analysis, when the crankshaft turned through $720 / Y$ deg., the cam ring turned through an angle of $\Delta$ deg. in the opposite direction. Thus the speed ratio is

$$
R=\frac{720 / Y}{\Delta}=\frac{720 / Y}{(360 / X)-(720 / Y)}=\frac{1}{(360 Y / 720 X)-1}
$$

but from Eq. (10-33)

$$
X=\frac{Y-1}{2}
$$

hence

$$
K=\frac{1}{360 Y}-\frac{1}{720\left(\frac{Y-1}{2}\right)}-1
$$

from which

$$
\begin{equation*}
R=Y-1 \tag{10-34}
\end{equation*}
$$

or the ratio of cam ring r.p.m. to crankshaft r.p.m. is

$$
\begin{equation*}
\frac{1}{R}=\frac{1}{Y-1} \tag{10-35}
\end{equation*}
$$

By a similar line of reasoning to the above, it can be demonstrated that for the same direction of rotation of the cam ring and crankshaft the number of cams required is

$$
\begin{equation*}
X^{\prime}=\frac{Y+1}{2} \tag{10-36}
\end{equation*}
$$

and the ratio of crankshaft to cam ring r.p.m. is

$$
\begin{equation*}
R^{\prime}=Y+1 \tag{10-37}
\end{equation*}
$$

In general, opposite rotation of the cam ring to crankshaft is desirable because fewer cams have to be accurately machined on the cam ring and because the relative velocity between the cam ring and follower rollers is usually less than for the same direction of rotation.

Because the drive gear attached to the crankshaft and the driven gear to which the cam ring attaches are concentric about the crankshaft axis, some limitations are placed on the possible gear-tooth combinations that will give the correct crankshaft/cam-ring ratio $R$ or $R^{\prime}$. It is usually not desirable for any gear to have less than 12 teeth, and to keep down weight, and relative velocity between the cam ring and roller follower, the largest gear should have a small over-all diameter. Also care should be exercised to see that the gears do not interfere with adjacent parts.

Referring to Fig. 10-22, it is seen that for opposite rotation of crankshaft and cam ring (case $\boldsymbol{A}$ ) the gear train is a special case of compound epicyclic gearing in which the arm ( $A$, Table A3-7) does not revolve. From case 1 of Table A3-7, the speed ratio of the driven gear to the drive gear is

$$
\begin{equation*}
\frac{1}{R}=\frac{N_{S} N_{P G}}{N_{G} N_{P S}} \tag{a}
\end{equation*}
$$

where $R=$ ratio of crankshaft to cam ring, r.p.m.
$N_{S}=$ number of teeth on the drive gear $S$, Fig. 10-22A.
$N_{P G}=$ number of teeth on the pinion gear $P_{G}$, Fig. 10-22A.
$N_{G}=$ number of teeth on the driven gear $G$, Fig. 10-22A.
$N_{P S}=$ number of teeth on the pinion gear $P_{S}$, Fig. 10-22A.

From Fig. 10-22A it is apparent that

$$
\begin{equation*}
D_{S}+D_{P S}=D_{G}-D_{P G} \tag{10-38}
\end{equation*}
$$

where $D=$ the pitch diameter of the various gears designated by the subscripts. But

$$
D=\frac{N}{P_{d}}
$$

where $N=$ number of teeth in the gear.
$P_{d}=$ diametral pitch.
Hence, for all gears having the same diametral pitch, Eq. (10-38) becomes

$$
\begin{equation*}
N_{S}+N_{P S}=N_{G}-N_{P G} \tag{10-39}
\end{equation*}
$$

Suitable gear-tooth combinations must satisfy both Eqs. (10-37) and (10-39), and with so many unknowns, a trial solution is necessary. However, the problem may be simplified by assuming ratios of $N_{s} / N_{P S}$. Thus, for a seven-cylinder singlebank radial engine with opposite crankshaft and cam-ring rotation, from Eq. (10-34), $R=6$. Assuming $N_{P G}=12$ teeth and $N_{S} / N_{P S}=1$, from Eq. (10-37)

$$
\frac{1}{6}=1 \times \frac{12}{N_{G}} \quad \text { or } \quad N_{G}=72 \text { teeth }
$$

since from the foregoing assumption $N_{S}=N_{P S}$, Eq. (10-39) will be satisfied when

$$
2 N_{s}=72-12
$$

Hence

$$
N_{S}=N_{P S}=30 \text { teeth }
$$

Several other gear combinations are given in Table 10-2, some of which are more desirable than others. In general, the best combination is one which, for the desired minimum number of teeth on the smallest pinion, gives the lowest number of teeth on the internal gear without interference of parts anywhere. The minimum chance for interference between the crankshaft and pinion $P_{G}$ will exist when $N_{P G}$ is small numerically. Over-all dimensions will be least when $N_{G}$ and $N_{P S}$ are small numerically.

Table 10-2.-Reduction-gear Tooth Combinations Suitable* for Compound Epicyclic Gear Trains as Applied to Radial-engine. Cam-ring Drives

|  |  |  |  |  | - | $V_{S}$ | $\begin{array}{r} R \\ N_{P S} \\ R \\ N \end{array}$ | $\begin{aligned} & =\frac{N_{P}}{N_{S}} \\ & =N_{G} \\ & =\frac{\mathrm{cra}}{\mathrm{ca}} \\ & =\text { nur } \end{aligned}$ | $\begin{aligned} & \frac{N_{G}}{T P G} \\ & -N_{F} \\ & \text { kisha } \\ & \text { a-ring } \\ & \text { ber } \end{aligned}$ | G <br> ft r.p <br> r.p. <br> of tee |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  | 7-cyl. radial, $R=6$ |  |  |  | 9 -cyl. radial, $R=8$ |  |  |  |
| $N_{P S}$ | $N_{\text {PG }}$ | $N_{P S}$ | $N_{S}$ | $N_{G}$ | $N_{\text {PG }}$ | $N_{\text {PS }}$ | $N_{S}$ | $N_{G}$ | $N_{\text {PG }}$ | $N_{P S}$ | $N_{S}$ | $N_{G}$ |
| 1/1. | 12 | 18 | 18 | 48 | 12 | 30 | 30 | 72 | 12 | 42 | 42 | 96 |
|  | 14 | 21 | 21 | 56 | 14 | 35 | 35 | 84 | 14 | 49 | 49 | 112 |
|  | 16 | 24 | 24 | 64 | 16 | 40 | 40 | 96 | 16 | 56 | 56 | 128 |
|  | 18 | 27 | 27 | 72 | 18 | 45 | 45 | 108 | 18 | 63 | 63 | 144 |
| 2/1 | 12 | 28 | 56 | 96 | 12 | 44 | 88 | 144 | 12 | 60 | 120 | 192 |
|  | 15 | 35 | 70 | 120 | 15 | 55 | 110 | 180 | 16 | 80 | 160 | 256 |
| 1/2 | 36 | 24 | 12 | 72 | 18 | 24 | 12 | 54 | 12 | 24 | 12 | 48 |
|  | 39 | 26 | 13 | 78 | 21 | 28 | 14 | 63 | 24 | 48 | 24 | 96 |
|  | 42 | 28 | 14 | 84 | 24 | 32 | 16 | 72 | 36 | 72 | 36 | 144 |
| $3 / 2$ | 15 | 30 | 45 | 90 | 15 | 48 | 72 | 135 | 15 | 66 | 99 | 180 |
|  | 20 | 42 | 63 | 120 | 20 | 64 | 96 | 180 | 20 | 88 | 132 | 240 |
| 2/3 | 24 | 24 | 16 | 64 | 20 | 36 | 24 | 80 | 15 | 39 | 26 | 80 |
|  |  |  |  |  |  |  |  |  | 30 | 78 | 52 | 160 |
| $3 / 4$ | 28 | 32 | 24 | 84 | 28 | 56 | 42 | 126 | 14 | 40 | 30 | 84 |
|  |  |  |  |  |  |  |  |  | 21 | 60 | 45 | 126 |
| $5 / 4$ | 18 | 32 | 40 | 90 | 18 | 52 | 65 | 135 |  |  |  |  |
| 7/8 |  |  |  |  |  |  |  |  | 15 | 48 | 42 | 105 |

* As far as satisfying Eqs. (10-37) and (10-39) is concerned. However, before definitely selecting any particular combination, a layout to scale should be made to check on interference of parts.

10-10. Example of Radial-engine Cam Calculations.-Determine dimensions and accelerations for a hollow-faced cam to operate the inlet valves on a seven-cylinder radial engine. Available data are as follows: inlet valve opening, 15 deg . before top center; inlet valve closing, 65 deg . after bottom center; maximum lift of roller follower, 0.5 in.; diameter of roller follower,

1 in.; diameter of engine crankshaft, 3 in ; opposite rotation of crankshaft and cam ring; speed of engine, 2,000 r.p.m.

Procedure.-From Eq. (10-33), the number of inlet cams required will be

$$
X=\frac{7-1}{n}=3
$$

From Eq. (10-34), the ratio of crankshaft speed to cam-ring speed will be

$$
R=7-1=6
$$

From Table 10-2, tentatively select

$$
N_{P G}=18, \quad N_{P S}=45, \quad N_{S}=45, \quad N_{G}=108
$$

Since the loads to be transmitted will not be excessive, $141 / 2-\mathrm{deg}$. involute gears should be satisfactory, and a diametral pitch of 12 (see Table 8-7) should be low enough. The pitch diameters corresponding will be

The diameter of gear $S$ will have to be sufficient to permit a hole center large enough to slip over the crankshaft.

From Table A3-3, the minimum dedendum is

$$
\frac{1.157}{P_{d}}-\frac{1.157}{12}=0.0964 \mathrm{in}
$$

and $3.75-2 \times 0.0964=3.5572>3$ in., hence the sun gear $S$ will be sufficient. The gear $P_{G}$ will have to fit in place without touching the crankshaft, and from Table A3-3 the addendum is

$$
\frac{1}{P_{d}}=\frac{1}{12}=0.0833 \mathrm{in}
$$

The center distance between the crankshaft and $P_{G}$ is

$$
\frac{D_{G}}{2}
$$

$$
\frac{D_{P G}}{2}=\frac{9}{2}-\frac{1.5}{2}=3.75 \mathrm{in}
$$



Fig. 10-24.-Layout for the radial-engine cam-ring drive, Par. 10-10.
and as $3.75>(1.5 / 2)+0.0833+3 / 2=2.3333$ in., the pinion gear $P_{G}$ will fit in place without interference. The layout of the pitch circles for the various gears is shown in Fig. 10-24.

The cam ring is usually made a part of the internal gear $G$ either integrally or by attachment; hence a logical value for the radius of the base circle (Fig. 10-24) is $R_{B}=5 \mathrm{in}$.

From Eq. (10-28),

$$
\frac{15+180+65}{2 \times 6}=21.666^{\circ}=21^{\circ} 40^{\prime}
$$

$$
\begin{aligned}
& D_{P G}=18 / 12=1.5 \text { in., } \quad D_{P S}: 45 / 12=3.75 \mathrm{in} ., \\
& D_{S}: 45 / 12=3.75 \mathrm{in} ., \\
& D_{G}=108 / 12=9 \mathrm{in} .
\end{aligned}
$$

Assume the radius of the nose circle is $R_{N}=1.25 \mathrm{in}$. Then from Eq. (10-29)

$$
h=5+0.5-1.25=4.25 \mathrm{in}
$$

From Eq. (10-30), the radius of the flank circle is

$$
R_{F L}=\frac{4.25^{2}+5^{2}-1.25^{2}-2 \times 5 \times 4.25 \times 0.9293}{2(1.25-5+4.25 \times 0.9293)}=5.05 \mathrm{in}
$$

From Eq. (10-31),

from which

$$
\begin{aligned}
& \theta_{M}=11^{\circ} 19^{\prime} \\
& \phi_{M}=21^{\circ} 40^{\prime}-11^{\circ} 19^{\prime}=10^{\circ} 21^{\prime}
\end{aligned}
$$

Cam-ring dimensions and the general arrangements are shown in Fig. (10-25).


Fig. 10-25.-Cam-ring layout for the radial engine in the Example of Par. 10-10.

The acceleration on the flank circle may be found by means of Eq. (10-27). For example at $\theta=11^{\circ} 19^{\prime}$

$$
\begin{aligned}
& A_{x}=0.000914\left(\frac{2,000}{6}\right)^{2}(5+5.05) \\
&\left\{\begin{array}{r}
(5+5.05) \times 0.9230 \\
{\left[(5.05-0.5)^{2}-(5+5.05)^{2} \times 0.1962^{2}\right]^{1 / 2}}
\end{array}\right. \\
&\left.+\frac{(5+5.05)^{3} \times 0.1962^{2} \times 0.9806^{2}}{\left[(5.05-0.5)^{2}-(5+5.05)^{2} \times 0.1962^{2}\right]^{3 / 2}}-0.9806\right\} \\
& A_{x}=1,788 \text { ft. per sec. }{ }^{2}
\end{aligned}
$$

The acceleration on the nose circle may be found from Eq. (10-6). For example at $\phi=10^{\circ} 21^{\prime}$,

$$
\begin{gathered}
A_{Y}=-0.000914\left(\frac{2,000}{6}\right)^{2} 4.25\left[0.98375 \quad \begin{array}{c}
4.25 \times 0.9354 \\
\left(1.75^{2}-4.25^{2} \times 0.1797^{2}\right)^{1 / 2} \\
4.25^{3} \times 0.3535^{2}
\end{array}\right. \\
\left.\begin{array}{c}
4\left(1.75^{2}-4.25^{2} \times 0.1797^{2}\right)^{3 /}
\end{array}\right]
\end{gathered}
$$

These values of $A_{x}$ and $A_{Y}$ together with the accelerations for other values of $\theta$ and $\phi$ are shown in Fig. 10-26. In addition, Fig. 10-26 shows the effect of reducing the radius of the nose circle from $R_{N}=1.25$ to $R_{N}=0.5$ in. In this latter case, it is seen that spring loads increase quite rapidly indicating that a period of dwell would be limited by the ability of the spring to keep the follower on the cam.

## 10-11. Cam Ramps.-Ow-

 ing to difference in temperature rise from cold, or idling, conditions to hot, or fullthrottle, conditions of the various parts of the valve gear and the cylinder, a difference in expansion of the parts usually results which necessitates providing for valve clearance to prevent the valve being held

Cam ring rotation, deg.
Frg. 10-26.- (A) Acceleration curve for the radial-engine cam in the Example of Par. 10-10. (B) Effect of reducing the radius of the nose circle from $R_{N}=1.25$ to $R_{N}=0.5 \mathrm{in}$. slightly off its seat at some conditions of engine operation. This clearance is of the order of 0.005 to 0.015 in ., depending upon the arrangement of parts, and it is sufficient to change the valve timing appreciably between the cold and hot conditions of
operation. For engines in which quietness of operation is a factor as well as more accurate valve timing and reduced shock loading on the cam, cam ramps are used. These quieting ramps may be made in various ways, ${ }^{1,2}$ and in general they consist of an incline occupying 15 to 30 deg . of camshaft travel and a rise equal to the clearance. They may be incorporated by reducing $R_{B}$ by the amount of the clearance and then connecting this undercut base circle with the point $\theta=0$ by means of the ramp.

Figure $10-27$ shows the effect of a cam ramp without clearance, wherein the follower rides on the base circle $R_{B}$, but with clear-


Fig. 10-27.-Effect of cam ramp in reducing shock and noise. (Note: See page 112 of Reference 10 for ramp formula.)
ance, the follower will not bear against the base circle. For instance, with $0.010-\mathrm{in}$. clearance the follower will strike the flank at $B$ or $C$ at a much sharper angle than it would at $A$ without clearance. Hence the shock will be greater with clearance, and it is seen from the figure that the shock with mushroom cams is greater than with comparable tangent cams because $\beta_{M}<\beta_{T}$. With the cam ramp and anywhere from 0 - to $0.010-\mathrm{in}$. clearance, the follower will strike the flank at $A$ and the shock will be less severe because $\beta$ is much greater than $\beta_{M}$ or $\beta_{T}$. This, in turn will mean quieter operation.

In aircraft engines, cam ramps are probably less important than in automobile engines (a) because quiet idling is less essential, (b) because the noise of the cam cannot be heard
above the roar of the unmuffled motor and propeller, (c) because the clearance can usually be set correctly for the much narrower operating range, and (d) because aircraft engines most commonly use tangent or hollow-faced cams that are inherently less noisy from this source.

Automatic clearance adjusters are of interest in this connection since they maintain the clearance at zero without danger of


Fig. 10-28.-Method of determining inlet- and exhaust-cam spacing. (A) Valve-timing diagram referred to crankshaft. (B) Cam spacing for opposite rotation of crankshaft and camshaft, and (C) for same direction of rotation.
holding the valves off their seats and are therefore probably the best solution to the problem. Figure 10-2 shows one type of adjuster as used on the Franklin engine.

10-12. Cam Spacing.-The angular spacing of the inlet and exhaust cams on the camshaft or cam ring depends upon the valve timing, ratio $R$ of crankshaft to camshaft or cam-ring speed, and upon the firing order. Referring to Fig. 10-28,
$\gamma_{I}=$ the angular travel of the crankshaft from inletvalve opening (I.V.O.) to inlet-valve closing (I.V.C.).
$\gamma_{E}=$ the angular travel of the crankshaft from exhaustvalve opening (E.V.O.) to exhaust-valve closing (E.V.C.).
M.O.I. = mid-opening position of the inlet valve.
M.O.E. $=$ mid-opening position of the exhaust valve.
$\lambda=$ the angle between M.O.E. and M.O.I. measured according to cyclic sequence.
From the figure,

$$
360-\lambda=\frac{\gamma_{I}}{2}-\text { I.V.C. }+\frac{\gamma_{E}}{2}-\text { E.V.O. }
$$

or

$$
\begin{equation*}
\lambda=\text { I.V.C. }+ \text { E.V.O. }-\left(\frac{\gamma_{I}+\gamma_{E}}{2}\right)+360 \tag{10-40}
\end{equation*}
$$

and

$$
\begin{equation*}
\epsilon=\frac{\lambda}{\bar{R}} \tag{10-41}
\end{equation*}
$$

where $\epsilon=$ the angle between the exhaust and inlet cam measured according to cyclic sequence.

$$
R=\frac{\text { crankshaft r.p.m. }}{\text { camshaft (or ring) r.p.m. }}
$$

For example, in a four-cylinder opposed engine having a valve timing of inlet-valve opening, 15 deg . before top center; inlet-valve closing, 65 deg. after bottom center; exhaust-valve opening, 60 deg. before bottom center; and exhaust-valve closing, 20 deg. after top center,

$$
\begin{aligned}
& \gamma_{I}=15+180+65=260 \mathrm{deg} . \\
& \gamma_{E}=60+180+20=260 \mathrm{deg} .
\end{aligned}
$$

and from Eq. (10-40)

$$
\lambda=65+60-\left(\frac{260+260}{2}\right)+360=225 \mathrm{deg} .
$$

From Eq. (10-41),

$$
\epsilon=225 / 2=112.5 \mathrm{deg} .
$$

For a seven-cylinder radial engine using the preceding valve timing and opposite rotation of the crankshaft and cam ring,
$R=6$ [Eq. (10-34)], and

$$
\epsilon=225 / 6=37.5 \mathrm{deg} .
$$

To permit closer axial spacing of the inlet- and exhaust-cam races and to place the center lines of the followers more nearly coin-


Fig. 10-29.-Layout for locating inlet and exhaust cams on radial-engine cam rings.
cident with the center lines of the push rods, radial-engine followers are usually offset so that their axes form a small angle to the plane containing the corresponding cylinder center line and the crankshaft center line. Thus in Fig. 10-29, the angle $\tau / 2$ represents the amount of offset. Obviously, from the geometry of this figure, the angular spacing between inlet and exhaust cams is $\epsilon \pm \tau$, and since all inlet cams are equally spaced,
this locates all cams on the cam ring. For the foregoing sevencylinder engine, if $\tau=20 \mathrm{deg}$.,

$$
\epsilon+\tau=37.5+20=57.5 \mathrm{deg}
$$

In in-line and opposed engines, usually all cams for all cylinders are on the same camshaft, and the angular spacing of like cams Firing order: 1-4-2-3


Fig. 10-30.-Method of locating the cams on the camshaft of a four-cylinder opposed engine.
must be determined from a consideration of firing order, arrangement of the crank arms, and, as applies, the angle of the cylinder banks. Thus for a four-cylinder opposed engine having the usual crank-arm arrangement (Fig. 5-13), and a firing order of 1-4-2-3, the cams will be as in Fig. 10-30. Frequently, to provide clearance between the camshaft and crank arms, the
camshaft is offset so that the center lines of the cam followers form an angle $\mu$ with the plane of the cylinder banks. Then the angle $\eta$ between the planes of the cam followers is not equal to 180 deg. To locate the cams (Fig. 10-30), center exhaust cam 1 on cam-follower center line 1. Locate inlet cam 1 back against camshaft rotation an amount equal to $\epsilon$ [see Eq. (10-41)].

Cylinder 4 fires 180 deg. of crankshaft travel after cylinder 1. Hence exhaust cam 4 will be located $180 / 2=90 \mathrm{deg}$. back against rotation from the center line of follower 4 . Inlet cam 4 will be located $\epsilon$ deg. against rotation from exhaust cam 4. Cylinder 2 fires 360 deg. after cylinder 1. Hence exhaust cam 2 will be located 180 deg . against rotation from the center line of inlet follower 2, and inlet cam 2 will be back $\epsilon$ deg. against rotation from exhaust cam 2. Number 3 cylinder fires 540 deg. after No. 1 cylinder. Hence exhaust cam 3 will be located 270 deg . back against rotation from the center line of exhaust follower 3, and, as before, inlet cam 3 will be $\epsilon$ deg. back of exhaust cam 3. In Fig. $10-30, \epsilon=112.5$ deg., $\mu=5 \mathrm{deg}$., and

$$
\eta=180-2 \times 5=170 \mathrm{deg} .
$$

Location of cams on in-line engine camshafts differs from the preceding mainly in that $\eta=0$ deg., i.e., all cam followers are in the same plane and point in the same direction. For more than four cylinders in a line, however, the angle of the engine cranks is not usually 180 deg. V-engines using a separate camshaft for each bank of cylinders may be treated similarly to in-line engines. $V$-engines having one camshaft may be treated as opposed engines with the added consideration of angle of the banks different from 180 deg.

10-13. Cam Loads.-The load on a cam is a force normal to the common


Fic. 10-31.-Forces acting on tangent cam flank. tangent to the cam and follower. This normal force may be broken down into a force along the cam-follower axis and a side-thrust force perpendicular to the cam-follower axis and in the plane of the cam. Thus in Fig. 10-31, $F_{A}$ is the force along the cam-follower axis, $F_{N}$ is the force normal to the cam, and
$F_{S T}$ is the resultant side thrust. For the straight flanks of tangent cams, the relations between the forces are

$$
\begin{equation*}
F_{N}=\stackrel{F_{A}}{\cos \theta} \tag{10-42}
\end{equation*}
$$

and

$$
\begin{equation*}
F_{S T}=F_{N} \sin \theta \tag{10-43}
\end{equation*}
$$

where $\theta=$ angular cam travel from initial opening.
For mushroom cams with flat-faced followers, $F_{N}=F_{A}$ and $F_{S T} \approx 0$.

For the flanks of hollow-faced cams (Fig. 10-32), the angle $\psi$


Fig. 10-32.-Forces acting on relating $F_{A}, F_{S T}$, and $F_{N}$ is a function of $\theta$. Thus, in Fig. 10-20

$$
C K=\left(R_{F L}+R_{B}\right) \sin \theta
$$

also

$$
C K=\left(R_{F L}-R_{F}\right) \sin \psi
$$

hence
$\psi=\arcsin$

$$
\left\lfloor\left(\overline{R_{F L}-R_{F}}\right)^{\text {sill } v\rfloor \quad(10- \pm \pm) ~}\right.
$$

And from Fig. 10-32,

$$
\begin{align*}
F_{N} & =\frac{F_{\Lambda}}{\cos \psi}  \tag{10-45}\\
F_{S T} & =F_{N} \sin \psi \tag{10-46}
\end{align*}
$$

. The total force along the camfollower axis $F_{A}$ is the resultant of the equivalent mass (referred to the cam) of the reciprocating part of the valve gear times the acceleration of the follower plus the spring load plus the gas pressure acting on the valve head. Considering these in order, the equivalent mass of the reciprocating parts of the valve gear may be found as follows:

Let $M_{E C}=$ equivalent mass of the reciprocating parts referred to the cam (i.e., $M_{E c}$ is a mass such that it will produce the same force along the cam-follower axis that all the various individual masses together produce).
$W_{1}=$ weight of cam follower + one-half weight of push rod considered concentrated at the cam, lb.
$W_{2}=$ one-half weight of push rod considered concentrated at the push-rod end of the rocker arm, lb.
$W_{3}=$ weight of the rocker arm.
$W_{4}=$ weight of valve + spring retainer + one-third of the valve spring considered concentrated at the valve end of the rocker arm, lb .
$K=$ radius of gyration of the rocker arm, in.
$d_{h}=$ distance at mid lift of the valve between the rocker-arm fulcrum and the axis of the push rod.
$d_{i}=$ distance at mid lift of the valve between the rocker-arm fulcrum and the axis of the valve stem.
$R_{R A}=d_{i} / d_{h}(\approx$ valvelift/cam lift when $\Lambda$ is small).
$\Lambda=$ the angle between the center line of the cam follower and the center line of the push rod at mid-lift position.
The arrangement of the various weights, dimensions, etc., is shown diagrammatically in Fig. 10-33.

For the equivalent mass $M_{E 3 C}$ referred to the cam follower (axis $A$ ), the kinetic energy of rotation

$\omega^{\prime}$

$$
M_{T}
$$

Fig. 10-33.-Diagrammatic arrangement for push-rod and rocker-arm type of overhead valve gear. . of the rocker arm must be considered. Thus the torque at the push-rod end of the rocker arm to accelerate mass $M_{3}$ is
$T_{3}=F_{3 B} \times d_{h}=\frac{F_{3 A}}{\cos \Lambda} \times d_{h}=I_{3} \times \alpha_{a}=\frac{W_{3}}{g} \times K_{\cdot}^{2} \times \frac{A_{A} \cos \Lambda}{d_{h}}$
where subscripts $A$ and $B$ refer to axis $A$ and $B$ and subscript 3 refers to mass 3 .
$F=$ force along an axis.
$A=$ acceleration along an axis.
$I_{3}=$ moment of inertia of mass $M_{3}$.
$\alpha_{a}=$ angular acceleration of the rocker arm:
Hence

$$
\begin{equation*}
M_{E 3 C}=\frac{F_{3 A}}{A_{\Delta}} \quad \frac{W_{3} K^{2}}{g d_{h}^{2}} \cos ^{2} \Lambda \tag{a}
\end{equation*}
$$

where $M_{E 3 C}=$ the equivalent of mass $M_{3}$ referred to the cam.

For the part of the push rod considered concentrated at the rocker arm, i.e., mass $M_{2}$,

$$
\begin{align*}
T_{2} & =\frac{F_{2 A}}{\cos \Lambda} \times d_{h}=I_{2} \times \dot{\alpha_{a}}=\frac{W_{2}}{g} \times d_{h}^{2} \times \frac{A_{A} \cos \Lambda}{d_{h}} . \\
M_{E 2 C} & =\frac{F_{2 A}}{A_{A}}=\frac{W_{2} \cos ^{2} \Lambda}{g} \tag{b}
\end{align*}
$$

where $M_{E 2 C}=$ equivalent of mass $M_{2}$ referred to the cam.
For the valve, spring retainer, etc., considered concentrated at the valve end of the rocker arm, i.e., mass $M_{4}$,

$$
\frac{F_{4 A}}{\cos \Lambda} \times d_{h}=I_{4} \times \alpha_{a}=\frac{W_{4}}{g} \times d_{i}^{2} \times \frac{A_{A} \cos \Lambda}{d_{h}}
$$

or

$$
\begin{equation*}
M_{E 4 C}=\frac{F_{4 A}}{A_{A}}=\frac{W_{4}}{g} \times \frac{d_{i}^{2}}{d_{h}^{2}} \times \cos ^{2} \Lambda=\frac{W_{4} R_{R A}^{2} \cos ^{2} \Lambda}{g} \tag{c}
\end{equation*}
$$

For the cam follower, tappet, and one-half of the push rod,

$$
\begin{equation*}
M_{E 1 C}=\frac{W_{1}}{g} \tag{d}
\end{equation*}
$$

The total equivalent mass at the cam is

$$
M_{E C}=M_{E 3 C}+M_{E 2 C}+M_{E 4 C}+M_{E 1 C}
$$

or

$$
\begin{equation*}
M_{E C}=\frac{1}{g}\left[\left(\frac{W_{3} K^{2}}{d_{h}^{2}}+W_{2}+W_{4} R_{R A}^{2}\right) \cos ^{2} \Lambda+W_{1}\right] \tag{10-47}
\end{equation*}
$$

During the acceleration period $X$, the inertia force along the cam-follower axis is

$$
\begin{equation*}
F_{A X}=A_{X} \times M_{E C} \tag{10-48}
\end{equation*}
$$

where $A_{x}=$ acceleration as in Eqs. (10-3), (10-16), or (10-27) as applies.
$M_{E C}=$ equivalent mass at the cam as in Eq. (10-47).
$F_{A X}=$ accelerating or inertia force, lb.
During the deceleration period $Y$, the force along the camfollower axis is

$$
\begin{equation*}
F_{A Y}=A_{Y} \times M_{E C} \tag{10-49}
\end{equation*}
$$

where $A_{Y}=$ deceleration as in Eqs. (10-6), or (10-19), as applies.
$M_{E C}=$ equivalent mass at the cam as in Eq. (10-47).
$F_{A Y}=$ decelerating or inertia force, lb.

During the deceleration, the maximum force $F_{A Y M}$ necessary to hold the follower on the cam is the resultant of the maximum force $F_{V Y M}$ exerted along the valve axis $V$ by the valve spring. From Fig. 10-33,

$$
F_{V Y M} \times d_{i}=F_{B Y M} \times d_{h}=\frac{F_{A Y M}}{\cos \Lambda} \times d_{h}+F_{F}
$$

or the force necessary at the valve spring is

$$
\begin{equation*}
F_{V Y M}=e_{e_{m}} \times \frac{F_{A Y M}}{R_{R A} \times \cos \Lambda}-\frac{A_{Y M} \times M_{E C}}{e_{m} \times R_{R A} \times \cos \Lambda} \tag{10-50}
\end{equation*}
$$

where $F_{F}=$ force necessary to overcome friction in the valve linkage.
$e_{m}=$ mechanical efficiency of the valve linkage and may be taken as 85 to 90 per cent.
subscript $M$ denotes maximum values.
The spring rate is

$$
\begin{equation*}
S_{R}=Q\left(\frac{F_{V Y M}-S_{c}}{L_{V^{\prime}}}\right) \tag{10-51}
\end{equation*}
$$

where $S_{R}=$ spring rate, lb. per in.
$S_{c}=$ load on the spring when the valve is closed.
$L_{V^{\prime}}=$ lift of the valve corresponding to $A_{Y M}$.
$Q=1.1$ to 1.5 usually.
The initial load must be (for exhaust valves) sufficient to hold the valve on its seat at maximum intake depression in the cylinder. This intake depression is of the order of $20 \mathrm{in} . \mathrm{Hg}$ ( $\approx 10 \mathrm{lb}$. per sq. in.). Hence $S_{c} \geqq 10 \times A_{v}$ where $A_{v}$ is the area of the valve head. However, the initial spring load may have to be $S_{c}=1$ to $3 \times 10 \times A_{v}$ in order to satisfy the requirements for a suitable valve spring (see Par. 10-18).

From Fig. 10-33,

$$
L_{V^{\prime}}=L_{B^{\prime}} \times R_{R A}=L_{A^{\prime}} \times R_{R A} \times \cos \Lambda
$$

and

$$
L_{A^{\prime}}=L_{Y^{\prime}}=L_{Y} \text { for } \phi \text { corresponding to } A_{Y M}
$$

where $L_{Y}$ is as in Eq. (10-4) or (10-17) as applies.
Then Eq. (10-51) becomes

$$
\begin{equation*}
S_{R}=\frac{Q\left(F_{V Y M}-S_{c}\right)}{L_{Y^{\prime}} \times R_{R A} \times \cos \Lambda} \tag{10-52}
\end{equation*}
$$

With the spring rate $S_{R}$ and the initial loading $S_{c}$ known, the force exerted by the spring along the valve axis $V$ for any value of valve lift $L_{V}$ becomes

$$
F_{V}=S_{R} \times L_{V}+S_{c}
$$

and the corresponding force along the cam-follower axis $A$ due to the spring is

$$
\overline{e_{m} \times R_{R A}} \times \cos \Lambda=S_{R} \times L_{A} \times R_{R A} \times \cos \Lambda+S_{c}
$$

From which

$$
\begin{equation*}
F_{A S}=e_{m}\left(S_{R} \times L_{A} \times R_{R A} \times \cos \Lambda+S_{c}\right) R_{R A} \times \cos \Lambda \tag{10-53}
\end{equation*}
$$

where $F_{A S}=$ force along axis $A$ due to the spring, lb.
Thus the total force along the inlet cam-follower axis $A$ during acceleration is

$$
\begin{equation*}
F_{A I T X}=F_{A X}+F_{A S} \tag{10-54}
\end{equation*}
$$

where $F_{A X}$ is as in Eq. (10-48).
$F_{A S}$ is as in Eq. (10-53).
And the total force along the inlet valve cam-follower axis $A$ during deceleration is

$$
\begin{equation*}
F_{A I T Y}=F_{A Y}+F_{A S} \tag{10-55}
\end{equation*}
$$

where $F_{A Y}$ is as in Eq. (10-49). .

$$
F_{A S} \text { is as in Eq. }(10-53) .
$$

To keep the follower in contact with the cam during the deceleration, $F_{A T T Y}$ must be greater than zero.

For the exhaust valve, in addition to the inertia force and spring force on the cam, there will be a gas-pressure force during the first few degrees of the lift period due to the pressure in the cylinder being greater than in the exhaust manifold. This pressure $P_{E X} \approx P_{D}-P_{A}$ [see Eq. (3-2)] and the corresponding force along the cam-follower axis $A$ is

$$
\begin{equation*}
F_{A E X}=e_{m} \times P_{E X} \times A_{E X V} \times R_{R A} \times \cos \Lambda \tag{10-56}
\end{equation*}
$$

where $A_{E X V}=$ area of the exhaust valve head, sq. in., and the total initial force on the exhaust valve cam is

$$
\begin{equation*}
F_{A E T X}=F_{A X}+F_{A S}+F_{A E X} \tag{10-57}
\end{equation*}
$$

where $F_{A X}$ is as in Eq. (10-48), lb.
$F_{A S}$ is as in Eq. (10-53), lb.
$F_{A E X}$ is as in Eq. (10-56), lb.
The gas pressure $P_{E X}$ drops quickly to zero after the exhaust valve has started to open so that $F_{A E X} \approx 0$ for $\theta \geqq 5$ to 10 deg . of cam motion.

10-14. Example of Cam-load Calculations.-Determine (a) the valve spring rate and (b) the cam loads for an overhead-valve engine using push rods and rocker arms. Available data are as follows: maximum cam lift, 0.5 in.; length of rocker arm from fulcrum to push rod, 1.5 in.; length of rocker arm from fulcrum to valve, 2 in.; angle between cam-follower axis and push-rod axis at mid lift, 5 deg .; weight of cam follower, 0.4 lb .; weight of push rod, $0: 3 \mathrm{lb} . ;$ weight of rocker arm, $0.5 \mathrm{lb} . ;$ weight of valve springs, 0.24 lb .; weight of valve, 0.7 lb .; weight of spring retainer, $0.1 \mathrm{lb} . ;$ radius of gyration of rocker arm, 0.3 in . Cam same as for Par. 10-5, Example $a$; diameter of valve head, 2 in .

Procedure a.-For Eq. (10-47), $g=32.2 \mathrm{ft}$. per sec. ${ }^{2}, W_{\mathrm{z}}=0.5 \mathrm{lb}$., $K=0.3 \mathrm{in} ., d_{h}=1.5 \mathrm{in} ., d_{i}=2 \mathrm{in} ., R_{R A}=\frac{2}{1.5}=1.33, W_{2}=0.15 \mathrm{lb} .$, $\dot{W}_{4}=0.7+0.1+(0.24 / 3)=0.88 \mathrm{lb} ., \Lambda \quad 5$ deg.,

$$
W_{1}=0.4+0.15=0.55 \mathrm{lb} .
$$

Then

$$
\begin{aligned}
& M_{E C}=\frac{1}{32.2}\left[\left(\frac{0.5 \times 0.3^{2}}{1.5^{2}}+0.15+0.88 \times 1.33^{2}\right) \times 0.9962^{2}+0.55\right] \\
& M_{E C}=0.0702 \text { slugs }
\end{aligned}
$$

For Eq. (10-50), $A_{Y M}=1,488 \mathrm{ft}$. .per sec. ${ }^{2}$ (see Fig. 10-13), assume $e_{m}=0.9$. Then

$$
F_{V Y M}: \frac{1,488 \times 0.0702}{0.9 \times 1.33 \times 0.9962}: 87.5 \mathrm{lb} .
$$

For Eq. (10-52), $S_{c}=2 \times 10 \times 0.785 \times 2^{2} \approx 63 \mathrm{lb} ., L_{Y^{\prime}}=0.5 \mathrm{in}$. ( $\phi=0$ for $A_{Y M}=1,488$, from Fig. 10-13). Then, assuming $Q=1.3$

$$
S_{R}=1.3\left(\frac{87.5-63}{0.5 \times 1.33 \times 0.9962}\right): 48 \mathrm{lb} . \text { per in. }
$$

Procedure b.-For the inlet-valve cam loads, for Eqs. (10-48) and (10-49), values of $A_{X}$ and $A_{Y}$ were read from Fig. 10-13 (more accurately from the data for Fig. 10-13) and multiplied by $M_{E C}$ to get the values of $F_{A X}$ and $F_{A Y}$ shown in Table 10-3.

For Eq. (10-53), $e_{m}=0.9, S_{R}=48, R_{R A}=1.33, \cos \Lambda=0.9962, S_{c}=63$, and $L_{A}$ read from Fig. 10-13 (or more accurately from the data for Fig. 10-13) is given in Table 10-3. Then for $L_{A}=0.5 \mathrm{in}$. (corresponds to $A_{Y M}$ ),
$F_{A S}=0.9[(48 \times 1.33 \times 0.9962 \times 0.5)+63] 1.33 \times 0.9962=109.5 \mathrm{lb}$. From Eq. (10-55),

$$
F_{A I T Y}=-104.4+109.5=5.1 \mathrm{lb} .
$$

Since $F_{A I T Y}$ is positive, it indicates that the spring is adequate, but to be certain of contact between the follower and the cam at all values of $\phi$, assume $S_{R}=50 \mathrm{lb}$. per in. and calculate the corresponding values of $F_{A I T Y}$. In Table 10-3, it is seen that the follower will not leave the cam at any point during deceleration.

For the exhaust valve at the start of lift, assuming a cylinder pressure of $P_{E X}=50 \mathrm{lb}$. per sq. in. gage, from Eq. (10-56)

$$
F_{A E X}=0.9 \times 50 \times 0.785 \times 2^{2} \times 1.33 \times 0.9962=187 \mathrm{lb}
$$

Assuming the pressure equalizes in 10 deg. of cam travel, for $\theta=5 \mathrm{deg}$. $F_{A B X} \approx 93.5 \mathrm{lb}$. Values of $F_{A E T X}$ [from Eq. (10-57)] are shown in Table 10-3. Values of the force normal to the cam as shown in Table 10-3 were found by means of Eq. (10-42). The results are shown in graphical form in Fig. 10-34.

Table 10-3.-Data for Example, Par. 10-14

| $\theta$ | $A_{x}$ | $F_{A X}$ | $L_{\text {A }}$ | $F_{A S}$ | $F_{\text {AITX }}$ | $F_{\text {AETX }}$ | $F_{N}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0. | 1235 | 86.9 | 0 | 72.5 | 159.4 | 346.4 | 346.4 |
| 5. | 1260 | 88.5 | 0.004 | 73.0 | 161.5 | 255.0 | 256 |
| 10. | 1365 | 96.0 | 0.024 | 74.5 | 170.5 | 170.5 | 173 |
| 15. | 1460 | 102.8 | 0.051 | 76.5 | 179.3 | 179.3 | 186 |
| 20. | 1665 | 117.0 | 0.092 | 79.7 | 196.7 | 196.7 | 210 |
| 25. | 1958 | 137.8 | 0.140 | 83.3 | 221.1 | 221.1 | 244 |
| 30. | 2378 | 167.0 | 0.2105 | 88.6 | 255.6 | 255.6 | 295 |
| $30^{\circ} 9.5^{\prime}$ | 2395 | 168.1 | 0.216 | 89.4 | 257.6 | 257.6 | 298 |


| $\phi$ | $A_{Y}$ | $F_{A Y}$ | $L_{A}$ | $F_{A S}$ | $F_{\text {AITY }}$ | $F_{\text {AETY }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | -1488 | -104.4 | 0.5 | 111.2 | 6.8 | 6.8 |
| 5 | -1480 | -104.0 | 0.494 | 110.8 | 6.8 | 6.8 |
| 10 | -1460 | -102.7 | 0.473 | 109.5 | 6.8 | 6.8 |
| 15. | -1420 | - 99.9 | 0.442 | 106.8 | 6.9 | 6.9 |
| 20. | -1368 | - 96.1 | 0.3995 | 103.5 | 7.4 | 7.4 |
| 25. | -1293 | - 91.0 | 0.349 | 99.7 | 8.7 | 8.7 |
| 30 | -1211 | $-85.3$ | 0.284 | 94.6 | 9.3 | 9.3 |
| $30^{\circ} 50.5{ }^{\prime}$ | -1112 | $-78.4$ | 0.216 | 89.4 | 11.0 | 11.0 |

10-15. Camshaft Stiffness.-For in-line and V-engines, the camshaft acts as a beam supported by two or more bearings, and to minimize noise and distortion of parts, the deflection
should not exceed 0.002 to 0.004 in. The loads causing deflection are the cam reactions from moving the valves, and for one cam between bearings, the maximum deflection would occur when $F_{N}$ was a maximum. For several cams between bearings, the maximum deflection occurs at the worst vector combination of $F_{N}$ for the several cams taken together. An accurate analysis is long and tedious; and for the usual arrangement, the designer will generally be on the safe side if he selects a shaft diameter


Frg, 10-34.-Forces acting along the cam-follower axis in the Example of Par. 10-14.
such that the deflection does not exceed the allowable value when a force of $F_{N}$ maximum is applied midway between the bearings. For the simple beam with a concentrated load at the middle, the deflection is

$$
Y=\frac{P L^{3}}{48 E I}
$$

where $Y=$ deflection, in.
$P=$ load, lb.
$L=$ length between supports, in.
$E=30,000,000$ (for steel).
$I=$ moment of inertia of the section.
For hollow circular sections,

$$
I=\frac{\pi}{64}\left(D^{4}-d^{4}\right)
$$

where $D=$ outside diameter, in.
$d=$ internal diameter, in.
Hence

$$
\left(D^{4}-d^{4}\right)=\frac{0.425 P L^{3}}{E Y}
$$

usually $d \approx 0.5 \times D$, and on this basis

$$
\begin{equation*}
D=\left(\frac{0.454 P L^{3}}{E Y}\right)^{0.25} \tag{10-58}
\end{equation*}
$$

For the data of Par. $10-14, P=346 \mathrm{lb}$., and if we assume $Y=0.003 \mathrm{in}$., and $L=15 \mathrm{in}$.

$$
D=\left(\frac{0.454 \times 346 \times 15^{3}}{30,000,000 \times 0.003}\right)^{0.25} \approx 1.56 \mathrm{in}
$$

This leaves $2 \times R_{B}-1.56=2 \times 0.85-1.56=0.14 \approx 1 / 8 \mathrm{in}$., the originally assumed value for cam-follower clearance (see Par. 10-5).

10-16. Cam and Follower Details.-The width of the cam parallel to the camshaft or cam-ring axis should be such that, at the line of contact between the cam and follower, the material is not stressed beyond the fatigue limit in compression.

For a cylinder on a flat plate, Roark ${ }^{5}$ suggests

$$
\begin{equation*}
\max S_{C}=0.591\left(\frac{P E}{D}\right) \tag{10-59}
\end{equation*}
$$

where $\max S_{c}=$ maximum allowable compressive stress, lb. per sq. in. (see Table 8-6).
$P=$ load per linear inch.
$E=$ modulus of elasticity ( $=30,000,000$ for steel).
$D=$ diameter of the cylinder.
Applying Eq. (10-59) to a tangential cam with the roller on the straight flank, $D=2 R_{F}, P \times W_{c}=F_{N}$, and assuming the cam and follower are made of steel, * for tangential cams

$$
\begin{equation*}
\max S_{C}=2,295\left(\frac{\max F_{N}}{W_{c} \times R_{F}}\right)^{3 / 2} \tag{10-60}
\end{equation*}
$$

[^15]where $\max F_{N}=$ maximum force normal to the cam [see Eq. (10-42)], lb.
$W_{c}=$ width of the cam parallel to the camshaft or cam ring axis, in.
$R_{F}=$ radius of the roller follower, in.
Applying Eq. (10-60) to the example of Par. 10-14, $F_{N}=346$ lb., $R_{F}=1$ in., and if we assume $W_{c}=0.25 \mathrm{in}$., the maximum stress is
$$
\max S_{c}=2,295\left(\frac{346}{0.25 \times 1}\right)^{32}=85,500 \mathrm{lb} . \text { per sq. in. }
$$

From Table 8-6, it is seen that a cam width of $1 / 4 \mathrm{in}$. would require hardened or heat-treated steel.

Applying Eq. (10-59) to a mushroom cam with flat follower on the flank circle, $P=2 R_{F L}, P \times W_{c}=F_{N}$, and $E=30,000,000^{*}$ as before; for mushroom cams

$$
\begin{equation*}
\max S_{C}=2,295\left(\frac{F_{N}}{W_{c} \times R_{F L}}\right)^{3 / 2} \tag{10-61}
\end{equation*}
$$

where $F_{N}$ and $W_{c}$ are as in Eq. (10-60).
$R_{F L}=$ radius of the flank circle, in.
For a cylinder in a circular groove, Roark ${ }^{5}$ suggests

$$
\begin{equation*}
\max S_{c}=0.591\left(P E \frac{D_{1}-D_{2}}{n \vee n}\right)^{3 / 2} \tag{10-62}
\end{equation*}
$$

where $P$ and $E$ are as in Eq. (10-59).
$D_{\mathrm{i}} \doteq$ diameter of the circular groove.
$D_{2}=$ diameter of the cylinder.
Applying Eq. (10-62) to hollow-faced cams with a roller follower on the flank circle, $D_{1}=2 R_{F L}, D_{2}=2 R_{F}, P \times W_{c}=F_{N}$, and $E=30,000,000 .^{*}$ For hollow-faced cams,

$$
\begin{equation*}
\max S_{c}=2,295\left[\frac{F_{N}\left(R_{F L}-R_{F}\right)}{\bar{W}_{c} \times R_{F L} \times R_{.} .}\right]^{3 / 2} \tag{10-63}
\end{equation*}
$$

where $F_{N}, W_{c}$, and $R_{F}$ are as in Eq. (10-60).
$R_{F L}=$ radius of the flank circle, in.
For mushroom cams, the diameter of the flat-faced follower should be sufficient to provide full line contact at all cam angles.

* If the camshaft or cam ring is to be made of cast iron, use $E=15,000,000$ and alter Eqs. (10-60), (10-61), and (10-63).

To attain this condition, the diameter of the flat face on the follower will have to be greater than the contact width, $W_{D}$ (Fig. 10-35). From Fig. 10-17,

$$
\begin{equation*}
W_{D}=2\left(R_{F L}-R_{B}\right) \sin \theta_{M} \tag{10-64}
\end{equation*}
$$

The axis of the follower should be in the same plane as the axis of the camshaft, but the follower may be symmetrical with the cam as in Fig. 10-35A or offset as in Fig. 10-35B to produce rotation of the follower about its own axis and distribute wear. Case $B$ is the more common arrangement.


Fig. 10-35.-Dimensions of flat-faced follower for mushroom cams.
For the symmetrical follower, Fig. 10-35A,

$$
\epsilon_{1}=\arctan \frac{W_{c}}{W_{D}}
$$

and

$$
\begin{equation*}
R_{F F}=\frac{W_{c}}{2 \sin \epsilon_{1}} \tag{10-65}
\end{equation*}
$$

where $R_{F F}=$ radius of the flat follower surface, in.
$W_{c}=$ width of the cam parallel to the camshaft axis, in. [see Eq. (10-61)].
$W_{D}=$ contact width, in.

For the offset follower, Fig. 10-35B,

$$
\epsilon_{2}=\arctan \frac{\left(W_{c} / 2\right)+J}{W_{D} / 2}=\arctan \frac{W_{c}+2 J}{W_{I}}
$$

and

$$
\begin{equation*}
R_{F H}^{\prime}=\frac{W_{D}}{2 \cos \epsilon_{2}} \tag{10-66}
\end{equation*}
$$

where $R_{F F}^{\prime}=$ radius of the offset flat follower surfaces, in.
$W_{c}=$ width of the cam parallel to the camshaft axis, in. [see Eq. (10-61)].
$W_{D}$ contact width, in.
$J=$ offset of the center line of the follower to the center line of the cam measured parallel to the camshaft axis, in.
10-17. Push Rods and Rocker Arms.-Push rods as used with overhead valve-gear arrangements generally have a slenderness ratio such that they fall into the classification of long columns. Hence the Euler column formula may be used to analyze them, and since they usually use spherical seated bearings, they may also be classed as pin end columns. Thus :

$$
\begin{equation*}
P=\frac{\pi^{2} E I}{L^{2}} \tag{10-67}
\end{equation*}
$$

where $P=$ load at which the rod buckles, lb .
$E=$ modulus of elasticity, lb. per sq.in. $(=30,000,000$ for steel and $10,000,000$ for aluminum alloys).
$I=$ moment of inertia of the push rod-section, in. ${ }^{4}$
. $L=$ length of the push rod, in.
For tubular push-rod sections,

$$
I=\frac{\pi}{64}\left(D^{4}-d^{4}\right)
$$

where $D=$ diameter of the push rod, in.
$d=$ diameter of the hole through the push rod, in.
Assuming $d=0.8 \times D$, and the allowable load $=0.5 P$, Eq. (10-67) reduces to

$$
\begin{equation*}
D=1.625\left(\frac{P L^{2}}{\pi}\right)^{3 / 4} \tag{10-68}
\end{equation*}
$$

For the example of Par. 10-14, the maximum force along the
push-rod center line is

$$
P \approx F_{A E T X} \times \cos \Lambda \approx 346^{\circ} \times 0.9962 \approx 345 \mathrm{lb}
$$

Hence, for a length of 14 in., a hollow steel push rod having a diameter of

$$
D=1.625\left(\frac{345 \times 14^{2}}{30,000,000}\right)^{0.25}=0.353 \approx \frac{3}{8} \mathrm{in}
$$

should be satisfactory. By the same procedure, an aluminumalloy rod would have a diameter of $D \approx 1 / 2 \mathrm{in}$. The diameter of the spherical or ball ends of the push rod may be made approximately equal to the diameter of the push rod.

Rocker arms are essentially cantilever beams usually tapered and having a $T$ section. Generally, when they are large enough to meet other requirements, they are not critical in bending, but if there is any doubt, they may be analyzed by simple beam formulas. Frequently, small rollers are fitted to the valve-stem end of the rocker arm, and the size of these rollers may be found by the same formulas used for cam-follower rollers [i.e., the equivalent of Eq. (10-60)]. Clearance adjustment screws with locking nuts are usually built into the push rod end of the rocker arms.

Rocker-arm bearings are either plain or antifriction (i.e., ball or needle bearings). The maximum load is approximately the force in the push rod times the rocker-arm leverage ratio. In addition, an end thrust exists when the push-rod axis is not in the plane of the rocker arm and valve stem.

For the example of Par. 10-14, the maximum rocker-arm bearing reaction is

$$
F_{R A} \approx 345 \times \frac{1.5+2}{2} \approx 600 \mathrm{lb}
$$

On the assumption that a ball bearing is to be used, from Table A1-22, $F_{R A}=L=600 \mathrm{lb} ., Z \approx 0.9, K \approx 2$, and if it is assumed that the end thrust will not exceed 10 per cent of the radial load, $F=0.99$ for nonfilling notch-type bearings. Then, $C=600 \times 0.99 \times 0.9 \times 2=1,070 \mathrm{lb}$. Since the equivalent r.p.m. of the rocker arm should be low (say 200 r.p.m.), S.A.E. bearing 304 should be adequate (see Table A1-22I). However, before final selection is made, the recommendations of the bearing manufacturer should be obtained.

10-18. Valve Springs.-Nearly all modèrn aircraft engines use cylindrical helical compression springs of round wire, and most engines use two or three concentric springs per valve. Final approval for a proposed design should be made by a spring manufacturer, but the engine designer should make preliminary calculations if for no other reason than to determine necessary dimensions of adjacent parts of the valve gear.

For cylindrical helical compression springs of round wire, let
$G=$ torsional modulus of elasticity ( $\approx 11,500,000$ for steel ).
$S=$ stress, lb. per sq. in.
$S_{A}=$ maximum allowable stress, lb. per sq. in.
$f=$ deflection per turn, in.
$n=$ number of effective turns.
$f_{n}=$ total deflection, in.
$L_{M W}=$ minimum working length, in.
$S_{R}=$ spring rate, lb. per in. deflection.
$d=$ diameter of the wire, in.
$D_{o}=$ outside diameter of the spring, in.
$D_{i}=$ inside diameter of the spring, in.
$L_{s}=$ solid length, in..
$L_{F}=$ free length, in.
$F_{V}=$ force along the valve axis, lb .
$F_{V O}=$ force along valve axis when valve is open, lb .
$F_{v C}=$ force along the valve axis when valve is closed, lb .
$P_{S}=$ pitch of spring, in.
$F_{V A}=$ maximum allowable force on the spring, lb .
$Z=$ Wahl factor.

$$
C=\frac{D_{o}-d}{d}
$$

Then ${ }^{6}$

$$
\begin{align*}
L_{M W} & =1.1 d n+2.25 d  \tag{10-69}\\
L_{S} & =(n+2.25) d  \tag{10-70}\\
L_{F} & =f_{n}+L_{M W}  \tag{10-71}\\
S_{R} & =\frac{F_{V O}}{f_{n}}  \tag{10-72}\\
P_{S} & =\frac{L_{F}-2.25 d}{n}  \tag{10-73}\\
n_{\max } & =\frac{L_{M W}-2.25 d}{1.1 d}  \tag{10-74}\\
f_{n} & =\frac{8 \times n \times F_{V o}\left(D_{o}-d\right)^{3}}{G \times d^{4}} \tag{10-75}
\end{align*}
$$

$$
\begin{align*}
F_{V A} & =\frac{0.3927 \times S_{A} \times d^{3}}{\left(D_{o}-d\right) Z}  \tag{10-76}\\
Z & =\frac{4 C-1}{4 C-4}+\frac{0.615}{C}  \tag{10-77}\\
S & =\frac{\left(D_{o}-d\right) \times F_{V} \times Z}{0.3927 \times d^{3}} \tag{10-78}
\end{align*}
$$

Valve springs are subjected to rapidly varying loads, hence the allowable stress $S_{A}$ should be based on the torsional endurance limit rather than on the torsional elastic limit. This torsional

(A)

(C)

(B)

(D)

Frg. 10-36.-(A), (B) and (C) Allowable torsional-stress range for the most commonly used valve-spring steels. (D) Values of the Wahl stress factor. (From Griffith, " Standards for Spring Design," Product Engineering Design Work Sheets, Fourth Series.)
endurance limit depends upon the range of stress; diameter of the wire, and material of which the wire is made. Steel wire is usually drawn to Washburn and Moen gage (Table 10-4), and where possible standard wire diameters should be used. Materials most commonly used are medium- or high-carbon steel, Swedish steel, or chrome-vanadium steel (S.A.E. 6150). Allow-
able ranges of torsional stress as determined by Griffith ${ }^{6}$ are shown in Fig. $10-36 A, B$, and $C$. Stresses increase rapidly at low values of the spring index $\left(=D_{o} / d\right)$ as is seen in Fig. 10-36D, hence the spring index should be relatively large. Griffith ${ }^{6}$ recommends a value of $D_{o} / d=9$ as optimum, but some departure from this value may be necessary.

Table 10-4.-Washburn and Moen Steel-wire Gage Diameters

| Gage <br> No. | Wire diam- <br> eter, in. | Gage <br> No. | Wire diam- <br> eter, in. | Gage <br> No. | Wire diam- <br> eter, in. | Gage <br> No. | Wire diam- <br> eter, in. |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 000 | 0.3625 | 3 | 0.2437 | 8 | 0.1620. | 13 | 0.0915 |
| 00 | 0.3310 | 4 | 0.2253 | 9 | 0.1483 | 14 | 0.0800 |
| 0 | 0.3065 | 5 | 0.2070 | 10 | 0.1350 | 15 | 0.0720 |
| 1 | 0.2830 | 6 | 0.1920 | 11 | 0.1205 | 16 | 0.0625 |
| 2 | 0.2625 | 7 | 0.1770 | 12 | 0.1055 | 17 | 0.0540 |

Spring surging or vibration is a frequent cause of valve-gear trouble and may result in noisy operation owing to the follower jumping off the cam, and this in turn may affect the performance. Severe vibration can cause spring breakage. The usual methods of vibration control are (a) friction dampers, (b) design for high natural frequency of the spring, and (c) use of multiple springs having different natural frequencies.

The natural frequency of a valve spring in vibrations per minute is ${ }^{7}$

$$
\begin{equation*}
f_{v} \approx \frac{250 \times d \times G^{3 / 2}}{\left(D_{o}-d\right)^{2} \times n} \tag{10-79}
\end{equation*}
$$

where $d=$ diameter of the wire, in.
$D_{o}=$ outside diameter of the spring, in.
$n=$ number of effective turns.
$G=$ torsional modulus of elasticity $(\approx 11,500,000$ for steel).
Values of $f_{v}$ should be as high as possible, preferably above 15,000 , but this is often quite difficult to attain. By using two or more springs per valve which have different natural frequencies, erratic operation and damage from spring breakage will be less likely. Determination of the best possible combination of design factors is usually a long and tedious problem and one which specialists in spring manufacture are best qualified
to solve. The following example, however, indicates some of the steps involved.

10-19. Example of Valve-spring Calculations.-Determine (a) dimensions of a carbon-steel valve spring for the engine in the example of Par. 10-14, (b) dimensions if two concentric springs are to be used.

Procedure a.-From Par. 10-14, $S_{R}=50 \mathrm{lb}$. per in., maximum lift of the valve $=L_{V O}\left(=L_{V^{\prime}}\right.$ for this example $)=L_{A^{\prime}} \times R_{R A} \times \cos \Lambda=0.5 \times 1.33$ $\times 0.9962=0.663 \mathrm{in} ., F_{V c}=S_{c}=63 \mathrm{lb} ., F_{v o}=F_{V c}+S_{R} \times L_{V O}=96.2 \mathrm{lb}$.

Assume $D_{0}=2 \mathrm{in}$. ( $=$ diameter of valve), and for the optimum value of $Z$, the spring index $D / d \approx D_{o} / d=9$. Hence $d=2 / 9=0.222 \mathrm{in}$. Let $d=0.2253$ in. which corresponds to Washburn and Moen gage 4 (see Table $10-4$ ). From Fig. $10-36 D$, for $D_{o} / d=2 / 0.2253=8.88, Z=1.19$. From Eq. (10-78), for the valve closed

$$
S=\frac{(2-0.2253) \times 63 \times 1.19}{0.3927 \times 0.2253^{3}}=29,550 \mathrm{lb} . \text { per sq. in. }
$$

and for the valve open

$$
S=\frac{(2-0.2253) \times 96.2 \times 1.19}{0.3927 \times 0.2253^{3}}=45.200 \mathrm{lb} . \text { per sq. in. }
$$

From Fig. 10-36A, reading up from $S=29,550$ to the wire size (interpolated between 0.192 and 0.2625 ), it is seen that the allowable stress is $S_{A} \approx 57,000 \mathrm{lb}$. per sq. in. Hence the spring stresses are within the allowable range.

From Eq. (10-72),

$$
f_{n}=\frac{F_{V O}}{S_{R}}=\frac{96.2}{50}=1.925 \mathrm{in} .
$$

From Eq. (10-75),

$$
n=\frac{1.925 \times 11,500,000 \times 0.2253^{4}}{8 \times 96.2 \times(2-0.2253)^{3}}=7.45 \text { effective turns }
$$

From Eq. (10-79),

$$
f_{v}=\frac{250 \times 0.2253 \times 11,500,0001 / 2}{(2-0.2253)^{2} \times 7.45}=8,120 \text { vibrations per minute }
$$

This value of $f_{v}$ is lower than is desirable and might cause trouble from noise or even spring breakage.

From Eq. (10-69),

$$
L_{M W}=1.1 \times 0.2253 \times 7.45+2.25 \times 0.2253=2.347 \mathrm{in} .
$$

From Eq. (10-70),

$$
L_{S}=(7.45+2.25) \times 0.2253=2.181 \mathrm{in} .
$$

From Eq. (10-71),

$$
L_{F}=1.925+2.347=4.272 \mathrm{in}
$$

From Eq. (10-73),

$$
P_{S}=\frac{4.272-2.25 \times 0.2253}{7.45}=0.505 \mathrm{in}
$$

Layout of the spring is shown in Fig. 10-37A.
Procedure b.-Assuming two concentric springs per valve with the outside diameter $D_{o} \leq 2 \mathrm{in}$. for the outside spring and $D_{i} \geq 0.8^{\circ} \mathrm{in}$. for the inside spring (to ensure clearance with the valve guide), then for the inside spring $D_{o}-D_{i}=2 d$ and $D_{o} / d \approx 9$. From these relations and assumptions, $d=0.1142$, say 0.1055 in . ( $=$ Washburn and Moen gage 12, Table 10-4).
$D_{o}=2 \times 0.1055+0.8=1.011$ in.
$D_{o} / d=1.011 / 0.1055=9.58$
and from Fig. $10-36 D, Z=1.175$.
The combined force of the two springs (valve open) should be not less than $F_{v o}=96.2 \mathrm{lb}$., and (valve closed) $F_{V C}=63 \mathrm{lb}$. The minimum working length of the two springs can be somewhat different by step cutting the spring retainers, and this may aid in properly proportioning the springs.

Assume an allowable stress $S_{A}=60,000 \mathrm{lb}$. per sq. in. From Eq. (10-78), the corresponding load that the inner spring can carry is

$$
F_{V O}=\frac{0.3927 \times 60,000 \times 0.1055^{3}}{(1.011-0.1055) \times 1.175}=26 \mathrm{lb}
$$

Assume $n=10$ effective coils. From Eq. (10-75),

$$
f_{n}=\frac{8 \times 10 \times 26 \times(1.011-\dot{0} .1055)^{3}}{11,500,000 \times 0.1055^{4}} \quad 1.08 \mathrm{in}
$$

From Eq. (10-72),

$$
S_{R}=\frac{26}{1.08}=24 \mathrm{lb} . \text { per in. }
$$

The load that the inner spring can carry, valve closed, is

$$
F_{V C}=F_{V o}-S_{R} \times L_{V o}=26-24 \times 0.663=10 \mathrm{lb}
$$

The stress, valve closed, is, from Eq. (10-78)

$$
S=\frac{(1.01 \mathrm{i}-0.1055) \times 10 \times 1.175}{0.3927 \times 0.1055^{3}}=23,100 \mathrm{lb} . \text { per sq. in. }
$$

From Fig. $10-36 A$ reading up from 23,100 to the wire size,

$$
S_{A}^{\prime} \approx 60,000 \mathrm{lb} . \text { per sq. in. }
$$

Therefore the originally assumed value for maximum stress is satisfactory.
From Eq. (10-79),

$$
f_{v} \quad \frac{250 \times 0.1055 \times 11,500,0000^{1 / 2}}{(1.011-0.1055)^{2} \times 10} \quad 10,900
$$

This frequency is still less than desirable but better than for case $a$. From Eq. (10-69), the minimum working length is

$$
L_{M W}=1.1 \times 0.1055 \times 10+2.55 \times 0.1055=1.429 \mathrm{in} .
$$

From Eq. (10-71), the free length is

$$
L_{F}=1.08+1.429=2.509 \mathrm{in} .
$$

From Eq. (10-73), the pitch is

$$
P_{S}=\frac{2.509-2.25 . \times 0.1055}{10}=0.224 \mathrm{in} .
$$

The outside spring must be capable of carrying a load (valve open) of $F_{V O}=96.2-26=70.2 \mathrm{lb}$., and (valve closed) $F_{V C}=63-10=53 \mathrm{lb}$. Hence, the spring rate must be

$$
S_{R}=\frac{70.2-53}{0.663}=26 \mathrm{lb} . \text { per in. }
$$

From Eq. (10-72), the total deflection is

$$
f_{n}=\frac{70.2}{26}=2.7 \mathrm{in} .
$$

The inside diameter of the outside spring must be greater than the outside diameter of the inside spring. Assuming this difference is 0.25 in .; for the outside spring

$$
D_{i}=1.011+0.25=1.261 \mathrm{in} .
$$

also

$$
D_{o}-D_{i}=2 d \quad \text { and } \quad D_{o} / d \approx 9 .
$$

Hence

$$
\begin{aligned}
d & =0.18, \text { say } 0.177 \mathrm{in} . \\
D_{0} & =2 \times 0.177+1.261=1.615 \mathrm{in} . \\
\frac{D_{o}}{d} & -\frac{1.615}{0.177} \quad 9.11
\end{aligned}
$$

From Fig. $10-36 D, Z=1.18$
From Eq. (10-78), for the valve closed

$$
S=\frac{(1.615-0.177) \times 53 \times 1.18}{0.3927 \times 0.177^{3}}=41,500 \mathrm{lb} . \text { per sq. in. }
$$

and for the valve open

$$
S=\frac{(1.615-0.177) \times \$ 8 \times 1.18}{0.3927 \times 0.177^{3}}=55,000 \mathrm{lb} . \text { per sq. in. }
$$

From Fig. 10-36A, reading up from $S=41,500$ to the wire size, it is seen that the allowable stress is $S_{A} \approx 66,500 \mathrm{lb}$. per sq. in. Therefore the spring stresses are within the allowable range.

Assume $n=8$ effective coils. Then from Eq. (10-79),

$$
f_{v}=\frac{250 \times 0.177 \times 11,500,00011}{(1.615-0.177)^{2} \times 8} \quad 9,060 \text { vibrations per min. }
$$

This is lower than desirable but better than case $a$, and since $f_{v}$ (outside spring) $\neq f_{v}$ (inside spring), vibration in either spring will tend to be neutralized by the other.


Fig. 10-37.-Layout for the valve springs in the Example of Par. 10-19. (A) Single spring for case (a). (B) and (C) Inner and outer springs for case (b).

From Eq. (10-69), the minimum working length is

$$
L_{M W}=1.1 \times 0.177 \times 8+2.25 \times 0.177=1.953 \mathrm{in} .
$$

From Eq. (10-71), the free length of the outside spring is

$$
L_{F}=2.7+1.953=4.653 \mathrm{in}
$$

From Eq. (10-73), the pitch is

$$
P_{S}=4.653-2.25 \times 0.177 \quad 0.532 \mathrm{in}
$$

The layout of the two springs for case $b$ is shown in Fig. $10-37 B$ and $C$.

Since $L_{M W}=1.429 \mathrm{in}$. for the inside spring and 1.953 in . for the outside spring, the spring retainers will have to be step cut. If the difference is equally divided, each retainer will have an offset of

$$
\frac{1.953-1.429}{2}=0.262 \mathrm{in}
$$

The chief weakness of the springs in this example is the low frequency of vibration, and this may be increased by reducing the number of effective turns (Eq. 10-79). Thus, commonly used values of $n=4$ to 6 would reduce the chances of vibration failure, but to avoid exceeding the allowable stress of the wire, a larger over-all diameter would be necessary. In general, a short, large-diameter spring with very few turns is the best answer.

10-20. Valve-gear Details.-With the dimensions of the principal parts of the valve gear determined, the detail dimension of the valve-spring retainers, valve-stem length, rocker-arm bearing supports; and rocker-arm housing may be determined, and the completion of the drawings of the cylinder (Suggested Design Procedure, items 9, 10, and 11, page 210) can be made. . Lubrication of the rocker arms, etc., formerly was intermittent, but continuous circulation of oil is preferable and is now quite common practice. One method of doing this is to provide a passageway to the cam-follower tappet and through the hollow push rod. A tubular sleeve and rocker-arm cover or rocker box may be used to enclose the gear. Detail arrangements may be best studied by reference to available sectioned drawings of successful engines.

All supports for the valve gear should be as rigid as possible, and such parts as rocker-arm bearing supports should be designed with this requirement in mind. In general, the best arrangement is one that, with the least complexity, fulfills all requirements.

## Suggested Design Procedure

Important. Include sample calculations of all items (as applies). Make layouts to a large enough scale to permit accuracy of measurements.

1. Make preliminary pencil sketches approximately to scale showing the desired arrangement of the valve gear to be used. Check to be sure the arrangement represents good practice and that the parts will fit together without interference.
2. Determine all necessary dimensions for the cam drive to be used including gear tooth numbers, and layout the arrangement to large (preferably full) scale.
3. Determine all necessary dimensions for the cams, and make a dimensioned drawing of the cams.
4. Calculate data, and plot lift, velocity, and acceleration curves for the cams to be used. Alter the cam dimensions as necessary to avoid excessively high accelerations.
5. Determine the proper spacings for inlet and exhaust cams, and make a dimensioned drawing showing positions of all cams on the camshaft or cam ring.
6. Determine cam loads, and plot curves of forces acting along the cam-follower axes.
7. Determine all remaining dimensions of the camshaft or cam ring, and alter the dimensioned drawing of the camshaft or cam ring (item 5) as necessary.
8. Determine all necessary dimensions of the cam follower and tappet, and make a dimensioned drawing.
9. Determine all necessary dimensions of the push rods and rocker arms, and make dimensioned drawings.
10. Determine all necessary dimensions for suitable valve springs, and make dimensioned drawings.
11. Complete the details of the valve gear, and make dimensioned drawings of all detail parts.
12. Complete the detailed dimensioned drawing of the cylinder head as started under item 10 of Suggested Design Procedure, page 210.
13. Complete the assembly drawing of the cylinder as started under item 11 of Suggested Design Procedure, page 210.
14. When items 1 to 13 have been completed and put in proper form, submit for checking and approval.

## Problems

1. Determine the dimensions, layout the cam, and plot curves of lift, velocity, and acceleration for the tangent cam of Par. 10-5, use the same data but increase the diameter of the roller follower to 1.5 in . Compare the results with the answers in Par. 10-5.
2. Determine dimensions, layout the cam, and plot curves of lift, velocity, and acceleration for a hollow-faced cam to operate the inlet valves on a fivecylinder radial engine. Available data are as follows: inlet-valve opening, 15 deg . before top center; inlet-valve closing, 65 deg. after bottom center; maximum lift of the roller follower, 0.5 in .; diameter of roller follower, 1.5 in .; diameter of the engine crankshaft, 2.5 in .; opposite rotation of crankshaft and cam ring; speed of engine, 2,000 r.p.m.
3. Repeat Problem 2 for a nine-cylinder radial engine, use the same data but increase the diameter of the engine crankshaft to 3.25 in .
4. Determine the necessary data, and layout a cam ring for the inlet and exhaust cams of the five-cylinder engine in Problem 2. Additional data are as follows: exhaust-valve opening, 50 deg. before bottom center; exhaustvalve closing, 10 deg . after top center; cam follower offset to the plane containing the cylinder and crankshaft center lines, 15 deg .
5. Determine the necessary data, and layout a camshaft showing the location of the cams on a six-cylinder in-line engine camshaft. Available data are as follows: inlet-valve opening, 10 deg . before top center; inlet-valve closing, 50 deg . after bottom center; exhaust-valve opening, 55 deg . before bottom center; exhaust-valve closing, 15 deg. after top center; crank-arm arrangement as in Fig. 7-15; firing order 1-5-3-6-2-4; angle of plane of follower center lines to plane of cylinder center lines, 8 deg. Opposite rotation of camshaft and crankshaft.
6. Prove that the flank and nose portions of a constant-acceleration cam are parabolas. Hint, see reference 1.
7. Derive expressions for the relation of parts of a constant acceleration cam. Hint, see reference 1.
8. By using the same valve timing and any other data that applies, determine the necessary data, layout the cam, and plot curves of lift, velocity, and icceleration for a constant-acceleration cam to replace the hollow-faced cams in Problems 2 and 4.
9. Prove that, for the same direction of rotation of cam ring and crankshaft, the number of inlet cams required will be as in Eq. (10-36) and the ratio crankshaft to cam-ring speed will be as in Eq. (10-37).

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## CHAPTER 11

## THE CRANKCASE, SUPERCHARGERS, AND ACCESSORIES

11-1. Crankcase Materials and Arrangements.-The crankcase serves to hold the various parts of the engine in proper position, to retain part or all of the lubricant, and usually, though not always, to transfer the external forces to the engine mounting. The crankcase should have a high rigidity-weight ratio and high fatigue resistance.


Fig. 11-1.-American Magnesium Corporation, magnesium alloy, AM7-4HT, crankcase for a Lycoming nine-cylinder radial engine.

Rigidity or crankcase stiffness with low weight may be attained by

1. Compact arrangement.
2. Adequate trussing.
3. Arrangement for straight-line transmittal of forces.
4. Use of materials having a high ratio of modulus of elasticity and modulus of rigidity to specific weight.

The crankcase, like the piston, cylinder head, and numerous other stressed parts, is so complex in shape and subjected to
such a variety of varying forces as to make the exact calculation of stresses in its parts very difficult if not impossible. Hence the designer will find useful the procedure suggested in connection with the design of connecting-rod ends, i.e., refer the complex structures to similar simple structures with known relations between external forces, dimensions, stresses, deflection, etc. Thus the crankcase may be likened to a cantilever box beam subjected to varying bending and twisting forces and designed for stiffness.


Fig. 11-2.-Aluminum Company of America forged aluminum-alloy crankcase for a Pratt and Whitney 14-cylinder radial engine.

The deflection of simple cantilever beams varies with the cube of the length; hence we would expect the in-line and V-engines to be at a weight disadvantage with a radial engine having the same crankcase stiffness. This disadvantage can, however, be at least partly offset in liquid-cooled designs by using a cooling jacket common to all cylinders in a bank and designing the jacket for stiffness. Deflection also varies directly with the load and inversely with the modulus of elasticity and moment of inertia of the section. This variation indicates the desirability of a larger number of smaller cylinders and large transverse dimensions for the crankcase. Modulus of elasticity is greater for steel than for other possible crankease materials, but here the lower unit weight of less rigid materials must be considered. Also
buckling of very thin sections and fabrication difficulties in forging thin steel sections make it difficult to take full advantage of steel characteristics.

Table 11-1 indicates that on a specific-weight basis, steel has little if any advantage over aluminum forgings, and for small production where forging dies are not justified, aluminum- and magnesium-alloy castings are definitely superior to cast iron.


Fig. 11-3.- Machining operation on a Pratt and Whitney forged aluminum-alloy crankcase.

However, as the engine size goes up, the need for thin sections diminishes, and steel compares more favorably. Also, a fair appraisal should take account of the relative corrosion resistance and strength at operating temperatures as well as relative cost. In the first two, steel has some advantage, and in the last cast iron stands out, particularly with reference to magnesium, whereas aluminum is intermediate. Thus present practice which, for stressed crankcase parts, uses cast iron only for lowest
cost engines，cast aluminum and some magnesium for medium－ powered，low－production，and forged aluminum and steel for high－powered，high－production engines appears to be basically


Fig．11－4．－Wright Cyclone steel crankcase showing（left to right）design refinements that have greatly reduced cost and weight．
sound．For lightly stressed parts，light alloy castings are suitable even for high－powered engines．

Table 11－1．－Comparative Data on Crankcase Materials

| Crankcase material | Designation |  |  |  | $E / \delta$ | G／8 |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Aluminum sand－ casting alloy． | 195－T6 | 10.3 | 3.85 | 0.100 | 103 | 38.5 | 6，500 | 65.0 |
| Aluminum sand－ casting alloy． | 355－T6 | 10.3 | 3.85 | 0.097 | 106 | 39.7 | 8，500 | 87.5 |
| Aluminum forg－ ing alloy． | A．51S－T | 10.3 | 3.85 | 0.097 | 106 | 39.7 | 10，500 | 108.2 |
| Magnesium sand－ casting alloy． | AM260－T4 | 6.5 |  | 0.066 | 98.5 |  | 10，000 | 151.5 |
| Steel． |  | 30.0 | 12.0 | 0.308 | 97.5 | 39.0 | 30，000 | 97.5 |
| Cast iron |  | 15.0 | 6.2 | 0.261 | 57.5 | 23.7 | 15，000 | 57.5 |

11－2．Crankcase Details．－In the Suggested Design Procedure of preceding chapters，it has been recommended that，as the designs were completed，detail parts should be transferred
to the assembly drawings. This gradual "assemblying" of the engine aids in checking on errors (no matter how well a part is


Fig. 11-5.-Exploded view of Wright Cyclone engine crankcase sections showing forged aluminum-alloy nose piece, forged main section, cast blower section, and cast rear section.


Fig. 11-6.-Exploded view of Wright cyclone G-200 engine crankease sections showing details of the steel main section.
designed, it is useless if it will not fit into its proper place), gives the designer a better mental picture of what the final design
will look like, and now, for the crankcase, he is able to see what detail shape of the crankcase will be necessary in order to support and hold together the previously designed parts.

As a first step, it is probably best to sketch in the outlines of the crankcase, either directly on the assembly drawings or on superimposed tracing paper. This procedure will aid in fixing



Recommended flange and bolthole proportioning


Methods of blending metal around bolt bosses

Fig. 11-7.-Aluminum Company of America recommendations on details of casting design.
in mind the necessary shape. Then the general arrangement should be carefully scrutinized for possible weak points while keeping in mind that the stiffness, etc., of complex shapes usually can be estimated by comparing them with simpler beams, columns, etc., of known characteristics. Thus the so-called stress path should be as direct as possible, and sharp reentrant corners should be avoided. Thin sections are always possible sources of buckling, and to avoid the excess weight of thicker sections, adequate structural ribbing is a good alternative.

Points at which loads are concentrated are potential sources of local failure, particularly with the nonferrous alloys, and such points should be carefully examined with a view to distributing the load more effectively. For example, too few cylinder holddown studs may put too great a strain on the crankcase metal immediately surrounding the studs, or the threads may be inaccurate and concentrate most of the load on a small portion of the threaded surface. Such possibilities justify an ample number of accurately ground coarse threads on studs to be


Fig. 11-8.-Practical equations commonly used to obtain proper radii and blending in the design of aluminum-alloy parts. (From S. A. E. Jour., Vol. 47, No. 6, December, 1940.)
fitted into soft metal even though the grinding of more parts materially increases the cost.

Corners and section joints in cast parts are frequently sources of casting flaws sufficient to cause failure, but they are often concealed from ordinary methods of inspection or at least escape detection prior to expensive machining operations. Such troubles can be reduced by utilizing the experience of casting specialists and adhering to their recommendations on casting design. Thus for their alloys, the Aluminum Company recommends the proportioning shown in Figs. 11-7 and 11-8.

11-3. Oil Pumps.-Lubricating oil pumps for aircraft engines are, almost without exception, of the spur-gear type. Oil
drawn into the pump (Fig. 11-9) fills the space between the teeth and is carried around to the discharge side where it is squeezed out against the discharge pressure by the meshing of the gear teeth. Pump capacity, for safety, should be appreciably greater than the maximum circulation requirements of the engine, and the excess oil may be by-passed through a pressure relief valve to the inlet side of the pump.

Use of a dry-sump crankcase requires one or more scavenger pumps to transfer the lubricant back to the external supply tank.


Fig. 11-9.-Schematic diagram of a gear-type oil pump. The scavenger pump, also of the spur-gear type, takes the oil from one or more collection points in the bottom of the crankcase; and to ensure a dry sump at all times, it is usually built with a capacity somewhat greater than that of the pressure pump. For simplicity, the scavenger pump is usually combined


Frg. 11-10.-Diagram showing a method of determining the capacity of a gear pump.
with the pressure pump in a common housing and driven from the same shaft. The scavenger pump preferably should be located near the level of the sump collection point to avoid an excessive suction lift.

To arrive at suitable proportions for the gear pump, the displacement may be determined from the volume of space between the teeth. Thus, in Fig. 11-10, the volume of a cylindrical shell having a length equal to the face width and a thickness equal to the working depth is

$$
\begin{equation*}
V=\left[(D+h)^{2}-(D-h)^{2}\right] \frac{\pi}{4} F=\pi D h F \tag{11-1}
\end{equation*}
$$

where $D=$ pitch diameter of the gear, in.
$h=$ working depth of the tooth, in.
$F=$ face width of the gear, in:
Since the volume of space between the teeth is approximately one-half the volume of this cylindrical shell, the theoretical displacement per gear per revolution is $V_{S} \approx \frac{V}{2}$, and since for full-depth teeth (Table A3-3) $h=\frac{2}{P_{d}}$, the displacement of a pump with two gears is

$$
\begin{equation*}
Q=\frac{2 \pi D F N}{P_{d}} \text { cu. in. per min. } \tag{11-2}
\end{equation*}
$$

where $P_{d}=$ diametral pitch.
$N=$ r.p.m. of the gears.
Data on pump proportions for typical engines are given in Table 11-2.

Table 11-2.-Oil-pump Proportions (All dimensions in inches)

| Engine type | Face width | Diam-1 etral pitch | Number of teeth | Pump: Crankshaft |
| :---: | :---: | :---: | :---: | :---: |


| Clearances | Pump dis- <br> placement* <br> cu. in. per |
| :---: | :---: |
| End Side | min. - en- <br> gine displace- <br> ment, cu. in. |

Pressure Pump

| 4 cyl. $\dagger$ opposed | 1.125 | 10 | 13 | 1:2 | 0.0050 .002 | 7.04 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 cyl. radial... | 0.75 | 7 | 7 | 5:4 | 0.0020 .002 | 2.24 |
| 7 cyl. radial.... | 0.875 | 10 | 13 | 5:6 | 0.0040 .003 | 2.355 |
| 9 cyl. radial.... | 0.5625 | 6 | 7 | 1:1 | 0.0030 .005 | 1.135 |
| 12 cyl. V.. | 0.75 | 8 | 10 | 1:1 | $0.0030 .008 \mid$ | 1.406 |
| 14 cyl. radial. . | 1.25 | 6 | 7 | 1.5:1 | 10.004\|0.003 | 3.26 |


| Scavenger Pump |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5 cyl. radial.... | 0.75 | 7 | 7 | 5:4 | 10.0020 .002 | 2.24 |
|  | \{ 0.875 | 10 | 13 | 5:6 | 0.00310 .003 | 2.355 |
| 7 cyl. radial.... | $\{1.25$ | 10 | 13 | 5:6 | 0.0030 .003 | 3.36 |
| 9 cyl. radial.... | 0.9375 | 6 | 7 | 1:1 | 0.0030005 | 1.89 |
| 12 cyl. V..... | 1.125 | 8 | 10 | 1:1 | $0.0030 .008 \mid$ | 2.11 |
|  | $\int 0.375$ | 6 | 7 | 1.5:1 | 0.0040 .003 | 0.978 |
| 14 cyl. radial... | $\{0.9375$ | 6 | 7 | 1.5:1 | 0.0040 .003 | 2.45 |
|  | 0.9375 | 6 | 7 | 1.5:1 | 10.00410.003 | 2.45 |

[^16]11-4. Blowers and Superchargers.-From the relation

$$
\text { b.h.p. }=P_{B} L A N_{p} n_{c} / 33,000=P_{B} D N / 792,000
$$

it is apparent that horsepower is proportional to size, speed, and b.m.e.p. Size is a function of cylinder displacement and number of cylinders. Cylinder diameter in aircraft engines is limited by cooling requirements to about 6 or 7 in ., and stroke, for reasonable


Fig. 11-11.—Roots-type superchargers. Showing two-lobe straight impeller (above) and three-lobe spiral type (below). (From Roots-Connersville Blower Corporation.) stroke-bore ratios, seldom exceeds 6.5 to 7.5 in . Also the stroke is limited by inertia forces.

Speed in direct-drive engines is ordinarily limited by pro-peller-efficiency requirements to 2,600 or 2,800 r.p.m., and in large geared engines, speed is usually limited by valve gear • or other reciprocating parts to 3,200 to 3,800 r.p.m.

Mean effective pressure mainly is limited by detonation characteristics of the fuel, but with present available octane ratings, fuels can withstand mean pressures well in excess of attainable values in naturally aspirated engines. Hence, with the better fuels, considerable supercharging can be used before detonation limitations are reached.

Superchargers are compact and light-weight fluid pumps capable of handling large volumes of air or air-fuel mixture. They may be used to offset pressure losses in the induction manifold and carburetor and thereby maintain atmospheric pressure at the inlet valve at sea level only or up to some predetermined critical altitude, or they may be used to increase the manifold pressure above atmospheric pressure. Some sources maintain that true supercharging constitutes only the increasing of manifold pressure above atmospheric sea-level values, but there is no very definite line of demarkation, and general usage often calls


Fig. 11-12.-Single-stage geared centrifugal supercharger. (From S. A.E. Jour., Vol. 43, No. 5, November, 1938.)


Fig. 11-13.-Two-stage geared centrifugal supercharger. $A$, intake pipe; $B$, super collector ring; $C$, impeller; $D$, air intake; $E$, carburetor; $F$, throttle valve; $G$, super air-pressure gage; $H$, intercooler; $I$, automatic suction valve; J, air inlet. (From S. A.E.Jour., Vol. 43, No. 5, November, 1938.)


Fig. 11-14.-Exhaust-turbine-drive centrifugal supercharger. (From S. A.E. Jour., Vol. 43, No. 5, November, 1938.)
any type of pump for increasing the amount of charge taken into a cylinder a supercharger.

Most applicable types of superchargers are the Roots positivedisplacement pump (Fig. 11-11) and the centrifugal or fan type. Roots-type superchargers are gear driven from the engine shaft, but centrifugal types may be either gear driven from the shaft (Figs. 11-12 and 11-13) or exhaust-turbine driven (Fig. 11-14). At present, the great majority of superchargers are of the geardriven centrifugal type, although there is a definite trend to the exhaust-turbine-driven type for high-altitude operation (20,000 to $35,000 \mathrm{ft}$.).

11-5. Supercharger Power Requirements.-In the Roots supercharger, air at pressure $P_{E}$ is trapped in the spaces between the
$d P$

## Volume

Fig. 11-15.-Theoretical $P-V$ diagram for a Roots supercharger. rotors and the housing and carried from the inlet to the exit side. When the exit opening is uncovered by the rotor, air at pressure $P_{L}$ rushes back and compresses the trapped air. Further movement of the rotors then forces the trapped air at pressure $P_{z}$ into the exit or discharge pipe.

A theoretical pressure-volume diagram for a Roots supercharger is shown in Fig. 11-15. In this figure, net work $\propto$ area $A B C D$ or $W_{\text {net }}=\int_{P_{E}}^{P_{L}} V d P$.
But

$$
V=V_{E}=V_{L}
$$

Hence

$$
\begin{align*}
W_{\mathrm{net}} & =V_{E} \int_{P_{E}}^{P_{L}} d P=V_{E}\left(P_{L}-P_{E}\right)=P_{E} V_{E}\left(R_{p}-1\right) \\
& =W R T_{E}\left(R_{p}-1\right) \tag{11-3}
\end{align*}
$$

where $\dot{V}_{E}=$ volume of entering air, cu. ft. per unit time.
$W=$ weight of entering air, lb. per unit time.
$P_{E}=$ inlet pressure, lb. per sq. ft. abs.
$P_{L}=$ discharge pressure, lb. per sq. ft. abs.
$R_{p}=P_{L} / P_{E}=$ the compression ratio.
$R=$ gas constant ( $=53.3$ for air).
$T_{E}=$ inlet air temperature, deg. F. abs.

If $W$ is in pounds per minute, the theoretical power required is

$$
\begin{equation*}
\mathrm{hp} .=\frac{W R T_{E}}{33,000}\left(R_{p}-1\right) \tag{11-4}
\end{equation*}
$$

For $V_{E}=V_{L}$, the temperature varies directly with the pressure, hence the compression temperature is

$$
\begin{equation*}
T_{L}=T_{z} \times R_{p} \tag{11-5}
\end{equation*}
$$

In the centrifugal supercharger, the air attains a high velocity owing to centrifugal force, and then the kinetic energy acquired contributes to increasing the pressure as the air slows down in the exit space. A

$\cdot{ }^{-}{ }_{E}$
Volume
Fig. 11-16.-Theoretical $P-V$ diagram for a centrifugal supercharger. theoretical $P V$ diagram for a centrifugal supercharger is shown in Fig. 11-16. In this figure, net work $\propto$ area $A B C D$ or

$$
W_{\mathrm{net}}=\int_{P_{s}}^{P_{L}} V d P
$$

But

$$
P V^{K}=P_{E} V_{E}^{K}=P_{L} V_{L}^{K}
$$

From which

$$
\mathrm{V}=\frac{P_{E^{1 / K}} V_{E}}{P^{1 / K}}
$$

Hence

$$
\begin{align*}
W_{\text {net }}= & P_{E^{1 / K}} V_{E} \int_{P_{E}}^{P_{L}} \frac{d P}{P^{1 / K}}=P_{E^{1 / K} V}^{\frac{K-1}{K}} \\
W_{\text {net }}= & \frac{K}{K-1} P_{E} V_{E}\left[R_{p}^{(K-1) / K-P_{E}^{(K-1) / K}} \bar{K}-1\right] \\
& \frac{K}{K-1} W R T_{E}\left[R_{p}^{(K-1) / K}-1\right] \\
W_{\text {net }}= & W J C_{p} T_{E}\left[R_{p}{ }^{(K-1) / K}-1\right] \tag{11-6}
\end{align*}
$$

where $K=C_{p} / C_{V}=$ adiabatic compression exponent ( $=1.4$ for air).
$V_{E}=$ volume of entering air, cu. ft. per unit time.
$P_{E}=$ inlet pressure, lb. per sq. ft. abs.
$P_{L}=$ discharge pressure, lb. per sq. ft . abs.
$R_{p}=P_{L} / P_{E}=$ the compression ratio.
$W=$ weight of entering air, lb. per unit time.

$$
\begin{aligned}
R & =J\left(C_{p}-C_{V}\right)=\text { gas constant }(=53.3 \text { for air }) . \\
T_{E} & =\text { inlet air temperature, deg. F. abs. } \\
J & =778 \mathrm{ft} . \mathrm{lb} . \text { per b.t.u. } \\
C_{p} & =\text { specific heat at constant pressure }(=0.24 \text { for air }) . \\
C_{V} & =\text { specific heat at constant volume }(=0.17 \text { for air }) .
\end{aligned}
$$

If $W$ is in pounds per minute, the power required for theoretical or adiabatic compression in the centrifugal supercharger is

$$
\begin{align*}
\text { Adiabatic } \mathrm{hp} . & =\frac{\frac{K}{K-1} W R T_{E}}{33,000}\left[R_{p}^{\frac{K-1}{K}}-1\right]  \tag{11-7a}\\
& =\frac{W J C_{p} T_{E}}{33,000}\left[R_{p}^{\frac{K-1}{K}}-1\right] \tag{11-7b}
\end{align*}
$$

and the compression temperature is

$$
\begin{equation*}
T_{L}=T_{E} \times R_{p}^{(K-1) / K} \tag{1.1-8a}
\end{equation*}
$$

Frequently it is useful to know the adiabatic temperature rise $\Delta t_{a}$ which is

$$
\begin{equation*}
T_{L}-T_{E}=\Delta t_{a}=T_{E}\left[R_{p}^{(K-1) / K}-1\right] \tag{11-8b}
\end{equation*}
$$

Due to turbulence, friction, etc., the actual fluid horsepower required by the centrifugal supercharger is considerably greater than the adiabatic horsepower. When the actual compression temperature $T_{\nu}$ or the temperature rise $\Delta t_{a}$ is known, a polytropic exponent $n$ may be found from Eq. (11-8) and then used in Eq. ( $11-7 a$ ) to get the actual fluid horsepower. Then

$$
\begin{align*}
e_{a} & =\frac{\text { adiabatic } \mathrm{hp} .}{\text { fluid } \mathrm{hp} .}  \tag{11-9}\\
e_{m} & =\frac{\text { fluid } \mathrm{hp} .}{\text { input hp. to supercharger }}  \tag{11-10}\\
e_{s} & =e_{a} \times e_{m} \tag{11-11}
\end{align*}
$$

where $e_{a}=$ compression or adiabatic temperature efficiency.
$e_{m}=$ mechanical efficiency of the supercharger drive.
$e_{s}=$ over-all adiabatic efficiency.
Values of the polytropic exponent $n$ have been found from practice usually to range between 1.6 and 1.8 , and corresponding adiabatic temperature efficiencies usually range between 70 and 80 per cent. Mechanical efficiencies may be taken as 85 to 90 per cent. Hence, an over-all adiabatic efficiency of 65 per cent is a reasonable assumption for design.

Another efficiency expression sometimes used in connection with Roots superchargers is the Roots-type efficiency which may be defined as the ratio of the work to compress adiabatically, as


Fig. 11-17.-Compression, temperature, and theoretical horsepower required to compress 1 lb . of air per sec. from standard pressure and temperature at altitude to 29.92 in. Hg. (Data from NACA Tech. Rept. 384.)
in the centrifugal supercharger, to the work required at constant volume, as in the Roots supercharger. Thus, from Fig. 11-16,

$$
\text { Area } A B C D \propto W_{\text {net }}=\frac{K}{K-1} P_{E} V_{E}\left[R_{p}^{(K-1) / K}-1\right]
$$

And from Fig. 11-15,

$$
\text { Area } A B C D \propto W_{\text {net }}=P_{E} V_{E}\left(R_{p}-1\right)
$$

or

$$
\begin{equation*}
\text { Roots-type efficiency }=\frac{K}{K-1}\left[\frac{R_{p}^{(K-1) / K}-1}{R_{p}-1}\right] \tag{11-12}
\end{equation*}
$$

Inspection of Eq. (11-12) shows that the centrifugal supercharger is less wasteful of power than the Roots and becomes increasingly so as the compression ratio is increased. Inlet pressure $P_{E}$ decreases with altitude; hence to maintain sea-level power, $R_{p}$ must be increased with altitude. Thus, the centrifugal supercharger is preferable for engines with high critical altitudes (Fig. 11-17).

Example 1.-A $5.25-$ by $5.25-\mathrm{in} ., 2,300-\mathrm{r} . \mathrm{p} . \mathrm{m} .$, nine-cylinder, 5.5:1-com-pression-ratio engine rated $500 \mathrm{~b} . \mathrm{hp}$. at $5,000 \mathrm{ft}$. altitude ( $P_{\mathrm{atm}}=24.9 \mathrm{in}$. Hg abs., $t_{\mathrm{atm}}=41.2^{\circ} \mathrm{F}$.) has a fuel rate of 0.53 lb . per b.hp. hr. and an airfuel ratio of 12.5 : 1 by weight, an over-all adiabatic efficiency of 65 per cent being assumed, estimate the horsepower required to drive the supercharger.

Solution.-The b.m.e.p. is

$$
P_{B}=\frac{500 \times 33,000 \times 12 \times 12}{5.25^{3} \times 0.785 \times 2,300 \times 9}=169 \mathrm{lb} . \text { per sq. in. }
$$

From Fig. 1-9A, the intake-manifold pressure is approximately $42 \mathrm{in} . \mathrm{Hg}$ abs. $=P_{L}$, hence

$$
R_{p}=\frac{42}{24.9^{*}}=1.6
$$

The weight of charge is $\dagger$

$$
W=\frac{500 \times 0.53 \times(12.5+1)}{60}=59.5 \mathrm{lb} . \text { per } \mathrm{min}
$$

From Eq. (11-7b),

$$
\begin{aligned}
\text { Adiabatic hp. } & =\frac{59.5 \times 778 \times 0.24 \times(41.2+460)}{33,000}\left[1.688^{(1.4-1) / 1.4}-1\right] \\
& =27.45
\end{aligned}
$$

And for an over-all efficiency of 65 per cent

$$
\text { Input hp. }=\frac{27.45}{0.65}=42.2
$$

11-6. Impeller Speed.-To attain desired pressure ratios with compactness and light weight, it is necessary to rotate centrifugal impellers at speeds of the order of 15,000 to 30,000 r.p.m. At such speeds, centrifugal stresses are very high, and to attain the

[^17]necessary strength and precision of balance, impeller forms must be used that are structurally strong and can be accurately fabricated without prohibitive cost. These requirements appear to be most feasible of attainment with forged-steel or aluminumalloy impellers having straight radial blades even though theory indicates that a suitably curved blade may be superior from a fluid-flow standpoint.

(B)

Fig. 11-18. -Vector diagram of air flow into and out of a centrifugal-supercharger impeller.

Referring to Fig. 11-18, let
$V_{1}=$ velocity of the air in the inlet pipe to the impeller, f.p.s.
$\alpha_{1}=$ angle between the direction of the incoming air and the plane of rotation of the impeller.
$U_{1}=$ tangential velocity of the impeller at the point of entry of the air to the impeller, f.p.s.
$U_{1}=\pi D_{1} N$.
$D_{1}=$ diameter of the impeller at the point of entry of the air, ft.
$N=$ impeller speed, r.p.s.
$V_{R 1}=$ velocity of the air relative to the impeller at the point of entry of the air to the impeller, f.p.s.
$\beta_{1}=$ angle between $V_{R 1}$ and a line normal to the blades at the point of entry of the air to the impeller.
$V_{R 2}=$ velocity of the air relative to the impeller at the point of exit from the impeller, f.p.s.
$\beta_{2}=$ angle between $V_{R 2}$ and a line normal to the blades at the point of exit of the air from the impeller.
$U_{2}=$ tangential velocity of the impeller at the point of exit of the air from the impeller, f.p.s.
$U_{2}=\pi D_{2} N$.
$D_{2}=$ diameter of the impeller at the point of exit of the air, ft.
$V_{2}=$ velocity of the air at the point of entry to the diffuser space, f.p.s.
$\alpha_{2}=$ angle between $V_{2}$ and $U_{2}$.
Considering first an ideal frictionless case and using a unit weight of 1 lb . of air as a basis, the impulse force given the air leaving the impeller will be

$$
F_{2}=\frac{V_{2} \cos \alpha_{2}}{g}
$$

The torque to produce this force is

$$
Q_{2}=\frac{D_{2}}{2} \times \frac{V_{2} \cos \alpha_{2}}{g}
$$

But

$$
U_{2}=\pi D_{2} N
$$

and the work required is

$$
W_{2}=2 \pi N Q_{2}
$$

Hence

$$
\begin{equation*}
W_{2}=\frac{U_{2} V_{2} \cos \alpha_{2}}{g} \tag{11-13}
\end{equation*}
$$

The tangential velocity $U_{2}$ is quite large in terms of the relative velocity $V_{R 2}$, so $\alpha_{2}$ is small. If the air leaves in a true radial direction relative to the impeller, $\beta_{2}=90 \mathrm{deg}$. and $V_{2} \cos \alpha_{2} \approx U_{2}$; hence

$$
\begin{equation*}
W_{2} \approx \frac{U_{2}^{2}}{g} \tag{11-14}
\end{equation*}
$$

Actually, the air passing through the impeller tends to pile up against the following blade (Fig. 11-19) so that $\beta_{2}<90$ deg., and this effect combined with a finite value for $V_{R 2}$ (i.e., $\alpha_{2}>0$ ) results, for radial blades, in $V_{2} \cos \alpha_{2}$ always being less than $U_{2}$. According to Pye, ${ }^{6} V_{2} \cos \alpha_{2}=0.85$ to $0.98 \times U_{2}$; hence

$$
\begin{equation*}
W_{2}=C \frac{U_{2}^{2}}{g}=C^{\pi^{2} D_{2}^{2} N^{2}} \tag{11-15}
\end{equation*}
$$

where $C=0.85$ to 0.98 and varies inversely with the quantity of flow.

Air entering the impeller (Fig. 11-18A) meets the blades at the relative velocity $V_{R 1}$ and at an angle $\beta_{1}$ to a line normal to the


Fig. 11-19.-Air-flow path between the blades of a centrifugal supercharger impeller: ( $A$ ) with flat radial blades; ( $B$ ) with curved entering edges.
blade surface. Hence the component of relative entering velocity normal to the blade is $V_{R 1} \cos \beta_{1}$, and the impact per unit weight of air is $V_{R 1}^{2} \cos ^{2} \beta_{1} / 2 g$. If this force is considered to act at the 'center of area of the passageway between the entering edges of the blades, the work to overcome this impact loss will be

$$
W_{1}=2 \pi N Q \approx \pi D_{A} N \begin{gather*}
V_{R 1}^{2} \cos ^{2} \beta_{1}  \tag{11-16}\\
2 g
\end{gather*}
$$

If flat radial blades are used and the air approaches the impel-
ler from a direction normal to the plane of rotation (i.e., $\alpha_{1}=90$ deg.), the impact component $V_{R 1} \cos \beta_{1}$ will be equal to $U_{1}$ and

$$
\begin{equation*}
W_{1} \approx \pi D_{A} N \frac{U_{1}^{2}}{2 g} \approx \frac{\pi^{3} D_{A}^{3} N^{3}}{2 g} \tag{11-17}
\end{equation*}
$$

Several methods may be used to reduce entering-impact losses. (a) By giving the air a helical or whirling motion in the inlet passageway to the impeller, $\alpha_{1}$ can be made less than 90 deg . This will reduce $V_{R 1}$, but the pressure loss in the inlet passage incident to producing this whirling will reduce $P_{1}$, and for a


Fig. 11-20.-Impeller and diffuser arrangement for a Pratt and Whitney centrifugal supercharger.
given desired manifold pressure, increase the compression ratio $R_{p}$, hence the work of compression [Eq. (11-6)], so that the net gain may be small. (b) $V_{1}$ may be increased with resulting increase in $\beta_{1}$ and decrease in $\cos \beta_{1}$, but here again an accompanying pressure loss in the inlet pipe will be had. (c) Probably the most effective way to reduce the entering-impact loss is to curve the entering edges of the blades (Fig. 11-19B) so that they are in line with $V_{R 1}$. This amounts to increasing $\beta_{1}$ to 90 deg., and as $\cos 90 \mathrm{deg} .=0$, this theoretically would eliminate the entering-impact loss. Actually, with blades of finite thickness and a practical radius of curvature, some turbulence would
remain, but by using thin warped blades,* i.e. by varying the curvature with the distance from the impeller sum

$$
\left[\beta_{1}=f\left(U_{1}\right)=f\left(D_{1}\right)\right],
$$

the net gain would still be considerable. This warping may be accomplished without curvature in the plane of rotation (i.e., without sacrifice in strength) by the arrangement shown in Figs. 11-20 and 11-21.

Since the cross-sectional area of the inlet pipe is fixed, $V_{1}$ will vary with the quantity of air flowing, i.e., with the load on the engine. Hence, for a constant impeller speed ( $\dot{U}_{1}=a$ constant), $\beta_{1}$ will decrease with $V_{1}$, and the change in direction of the air at entry will increase. When $\beta_{1}$ reaches some minimum value depending upon the design, the motion of the air will change from a streamline to a turbulent flow, and a condition analogous to burbling over an airfoil at high angles of attack will result. When an airfoil is increased in angle of attack beyond the stall point, the lift drops off rapidly, and the equivalent effect in centrifugal superchargers is an abrupt decrease in the compression ratio. For an airfoil, as the angle of attack decreases below the stall angle, the lift decreases gradually


Frg. 11-21.-Impeller with curved entering edges shaped to reduce entering-impact and turbulence losses without sacrifice in strength. and the equivalent effect in a centrifugal supercharger is a gradual decrease in compression ratio with increase in the quantity of air flowing.

This analogy with airfoils would indicate the desirability of an impeller with blades having an entering edge that could be adjusted in curvature as the quantity of air flowing was varied. An automatic mechanism (comparable to the automatic pitchvarying mechanism in propellers) would be ideal, but complexity and cost might more than offset the gain in performance. Pos-

[^18]sibly the best compromise is detachable curved entering edges that can be interchanged for different desired performance ratings. Suitably slotted entering edges (like leading-edge wing slots) might also merit investigation.

By assuming that the entering edges of the impeller blades are suitably shaped to minimize entering impact losses and turbulence, a relation among $R_{p}, D_{2}$, and $N$ can be obtained by combining Eqs. (11-6) and (11-15). Thus, per pound of air flowing

$$
\frac{C \pi^{2} D_{2}^{2} N^{2}}{g}=\frac{J C_{p} T_{1}}{e_{a}}\left(R_{p}^{\frac{K-1}{K}}-1\right)
$$

or

$$
\begin{equation*}
N=\sqrt{\frac{g J C_{p} T_{1}}{C \pi^{2} D_{2}^{2} e_{a}}\left(R_{p}^{\frac{K-1}{K}}-1\right)} \tag{11-18}
\end{equation*}
$$

where $T_{1}=T_{E}$.
It should be borne in mind when planning a supercharger design that air-flow characteristics are adversely altered as the moving air approaches the velocity of sound, and since $V_{2} \approx U_{2}$, it is advisable to keep the impeller-tip speed below 1,200 to 1,500 f.p.s.* Thus to attain compression ratios greater than about 2.5 to 3 or to maintain sea-level pressures to critical altitudes greater than about 20,000 to $25,000 \mathrm{ft}$., two or more stages of compression should be used.

Example 2.-For the engine in Example 1, determine the impeller speed, tip speed, and drive-gear ratio if the impeller diameter is $7 \frac{1}{2}$ in.

Solution.-For Eq. (11-18), $g=32.2, J=778, C_{p} \approx 0.24$,

$$
T_{1}=41.2+460=501.2
$$

$$
C \approx 0.85, D_{2}=7.5 / 12=0.625, e_{a}=0.7, R_{p}=1.688, K=1.4
$$

$$
\begin{aligned}
N & =\sqrt{\frac{32.2 \times 778 \times 0.24 \times 501.2}{0.85 \times \pi^{2} \times 0.625^{2} \times 0.7}\left(1.688^{0.286}-1\right)}=461 \text { r.p.s. } \\
\text { r.p.m. } & =461 \times 60=27,660
\end{aligned}
$$

Tip speed $=\pi \times 0.625 \times 461=905$ f.p.s.
Drive-gear ratio $=\frac{27,660}{2,300} \approx 12: 1$
11-7. Impeller Details.-To avoid restricting the flow into the impeller, the area of passageway into the impeller should be

[^19]approximately equal to the area of the inlet pipe. The area of the inlet pipe may be found from
\[

$$
\begin{equation*}
\frac{Q}{V_{0}}=A_{0}=\pi R_{0}^{2} \tag{11-19}
\end{equation*}
$$

\]

where $Q=$ quantity of charge, c.f.s.
$V_{0}=$ mean velocity in inlet pipe, f.p.s.
$A_{0}=$ area of inlet pipe.
$R_{0}=$ radius of inlet pipe.
The entry area normal to the direction of flow (Fig. 11-22) is the lateral area of the frustrum of a right circular cone in which $S$ is the slant height, $R_{h}$ is the radius of one base, and $R_{h}+S \cos \gamma$ is the radius of the other base. Then
$A_{1}=\pi S\left(2 R_{h}+S \cos \gamma\right)-S n_{b} t: \pi R_{0}^{2}$ or
$R_{0}^{2}=S^{2} \cos \gamma+2 R_{h} S$

$$
\begin{equation*}
-\frac{S n_{b} t}{\pi} \tag{11-20}
\end{equation*}
$$

where $\gamma=$ angle of approach to the impeller,

$$
\begin{aligned}
n_{b} & =\text { number of blades } \\
t & =\text { thickness of the blades }
\end{aligned}
$$

also

$$
S \cos \gamma=R_{1}-R_{h}
$$

Hence

$$
\begin{equation*}
R_{1}=R_{h}+S \cos \gamma \tag{11-21}
\end{equation*}
$$



Fig. 11-22.-Diagram for relating impeller dimensions.

Example 3.-For the engine in Examples 1 and 2, determine the inlet diameter of the impeller if the angle of approach is 15 deg ., the impeller hub diameter is 1.5 in., there are 14 impeller blades having an entering-edge thickness of 0.0625 in., and the mean velocity in the inlet pipe is 150 f.p.s.

Solution.-At 5,000 ft., the specific volume of entering charge is approximately
Specific vólume $=\frac{V}{W}=\frac{R T}{P}=\frac{53.3 \times 501.2}{24.9^{*} \times 0.491 \times 144}=15.2 \mathrm{cu} . \mathrm{ft}$. per lb. Then

$$
A_{0} \quad \pi R_{0}^{2}=\frac{Q}{r}-\frac{15.2 \times 59.5}{150 \times 60} \approx 0.1 \text { sq. ft. }
$$

[^20]$$
R_{0}=\sqrt{\frac{0.1 \times 144}{\pi}}=2.14 \mathrm{in} .
$$

Assume that the diameter of the inlet pipe $\left(=2 \times R_{0}\right)$ is 4.25 in . Then, from Eq. (11-20),

$$
4.57=0.9659 S^{2}+1.5 S-\frac{14 \times 0.0625}{\pi} S
$$

from which $S=1.656$ in. Substituting this value in Eq. (11-21)

$$
R_{1}=0.75+1.656 \times 0.9659=2.35 \mathrm{in}
$$

Hence, the diameter of the impeller at the inlet is

$$
D_{1}=2 R_{1}=4.7 \mathrm{in}
$$

To minimize turbulence, the air passing through the impeller should be turned gradually into the plane of rotation. This indicates the desirability of a large radius of curvature $R$, Fig. 11-22. In this figure,

$$
\begin{align*}
R_{2} & =F+R \cos \gamma+R_{h} \\
R & =\frac{R_{2}-F-R_{h}}{\cos \gamma} \tag{11-22}
\end{align*}
$$

also

$$
R=L_{1}+R \sin \gamma
$$

or

$$
\begin{equation*}
L_{1}=R(1-\sin \gamma) \tag{11-23}
\end{equation*}
$$

Hub curvature $R$ will be a maximum when $F=0$, but this may give a hub length $L_{1}$ to the impeller that is greater than desirable, i.e., the weight of the impeller may be excessive. Hence a compromise between turbulence [ $=f(R)$ ] and impeller weight may be in order.

Example 4.-For the engine in the preceding three examples, assume $F=1 \mathrm{in}$. and determine the hub length and curvature.

Solution.-For Eq. (11-22), $R_{2}=D_{2} / 2=3.75$ in., $R_{h}=0.75$ in., and $\gamma=15 \mathrm{deg}$. Then

$$
R=\frac{3.75-1-0.75}{0.9659}=2.075 \mathrm{in}
$$

and from Eq. (11-23),

$$
L_{1}=2.075(1-0.2588)=1.539 \mathrm{in} .
$$

The over-all hub length will be increased by the thickness of the back side of the impeller disk, but some weight may be saved by dishing in the back end of the hub.

Assuming a constant area of passage, the width of the blades $W_{b}$ normal to the moving air in the impeller may be found as follows:

In the passages where the air is being turned into the plane of the impeller, the cross-sectional area of passages is the lateral area of a frustrum of a right circular cone minus the area occupied by the blades. Thus, in Fig. 11-22,

$$
\begin{align*}
A & =\pi W_{b}\left(R_{x}+R_{y}\right)-n_{b} t W_{b}  \tag{11-2t}\\
R_{x} & =R_{2}-F-R \sin \alpha  \tag{11-25}\\
\dot{R}_{y} & =R_{x}+W_{b} \sin \alpha \tag{11-26}
\end{align*}
$$

and in the straight radial passage

$$
\begin{equation*}
A=2 \pi R_{x} W_{b}-n_{b} t W_{b} \tag{11-27}
\end{equation*}
$$

Example 5.-For the engine in the preceding four examples, determine the width of the blades for constant area of passage.

Solution. $-A\left(=A_{0}\right)=14.4$ sq. in., $n_{b}=14, t=0.1 \mathrm{in} ., R_{2}=3.75 \mathrm{in}$., $F=1$ in., $R=2.075 \mathrm{in}$. For $\alpha=0$

$$
\begin{aligned}
R_{x} & =3.75-1-0=2.75\left(=R_{y}\right) \\
14.4 & =\pi W_{b}(2.75+2.75)-14 \times 0.1 \times W_{b} \\
W_{b} & =0.905 \mathrm{in} .\left(=L_{a}\right)
\end{aligned}
$$

For $\alpha=10$ deg., $\sin \alpha=0.1736$, and

$$
\begin{aligned}
R_{x} & =3.75-1-2.075 \times 0.1736=2.39 \mathrm{in} . \\
R_{y} & =2.39+0.1736 W_{b} \\
14.4 & =\pi W_{b}\left(2.39+2.39+0.1736 W_{b}\right)-14 \times 0.1 \times W_{b} \\
W_{b} & =1.05 \mathrm{in} . \\
R_{y} & =2.39+1.05 \times 0.1736=2.572 \mathrm{in} .
\end{aligned}
$$

Similarly,
For $\alpha=20 \mathrm{deg} ., \quad R_{x}=2.041 \mathrm{in} ., \quad R_{y}=2.434 \mathrm{in} ., \quad \Pi_{b}=1.15 \mathrm{in}$.
For $\alpha=30$ deg., $\quad R_{x}=1.7125 \mathrm{in} ., \quad R_{y}=2.345 \mathrm{in} ., \quad W_{b}=1.265 \mathrm{in}$.
For $\alpha=40 \mathrm{deg} ., \quad R_{x}=1.417 \mathrm{in} ., \quad R_{y}=2.316 \mathrm{in} ., \quad W_{b}=1.4 \mathrm{in}$.
For $\alpha=50$ deg., $\quad R_{x}=1.16 \mathrm{in} ., \quad R_{y}=2.32 \mathrm{in} ., \quad W_{b}=1.5125 \mathrm{in}$.
For $\alpha=60$ deg., $\quad R_{x}=0.952$ in., $\quad R_{y}=2.337$ in., $\quad W_{b}=1.5975 \mathrm{in}$.
For $\alpha=90-\gamma=75 \mathrm{deg}$. and $t=0.0625 \mathrm{in}$., $W_{b}=1.644 \approx 1.656:: S$, thus checking the previous relations involving $R_{1}$.

In the straight radial portion of the impeller, the blade width varies inversely as the radius [Eq. (11-27)]. Hence the tip width may be calculated directly as

$$
L_{2}=\frac{14.4}{2 \pi \times 3.75-14 \times 0.1}=0.65 \mathrm{in}
$$

If it is assumed the energy imparted to the air in the impeller is all retained by the air, the work done by the impeller will be divided between increasing the kinetic energy and the enthalpy of the air. Thus

$$
W_{2}=\left(\frac{V_{2}^{2}}{2 g}-\frac{V_{1}^{2}}{2 g}\right)+J C_{p}\left(T_{2}-T_{1}\right)
$$

or

$$
T_{2}-T_{1}=\frac{W_{2}-\left[\left(V_{2}^{2} / 2 g\right)-\left(V_{1}^{2} / 2 g\right)\right]}{J C_{p}}
$$

But from Fig. 11-18,

$$
V_{2}^{2}=V_{R 2}^{2}+\left(V_{2} \cos \alpha_{2}\right)^{2}=V_{R 2}^{2}+C^{2} U_{2}^{2} \approx V_{1}^{2}+C^{2} U_{2}^{2}
$$

And from Eq. (11-15), .

$$
W_{2}=C \frac{U_{2}^{2}}{g}
$$

Hence, the temperature rise in the impeller is

$$
\begin{equation*}
T_{2}-T_{1}=\frac{2 C U_{2}^{2}-C^{2} U_{2}^{2}}{2 g J C_{p}} \tag{11-28}
\end{equation*}
$$

and the corresponding temperature ratio is

$$
\begin{equation*}
\frac{T_{2}}{T_{1}}=\frac{2 C U_{2}^{2}-C^{2} U_{2}^{2}}{2 g J C_{p} T_{1}}+1 \tag{11-29}
\end{equation*}
$$

By applying the temperature-volume relation

$$
\frac{T_{2}}{T_{1}}=\left(\frac{v_{1}}{v_{2}}\right)^{K-1}
$$

in Eq. (11-29), the change in the specific volume of the air passing through the impeller can be expressed as

$$
\begin{equation*}
\frac{v_{1}}{v_{2}}=\left(\frac{2 C U_{2}^{2}-C^{2} U_{2}^{2}}{2 g J C_{p} T_{1}}+1\right)^{1 /(K-1)} \tag{11-30}
\end{equation*}
$$

Example 6.-Determine the effect of change in specific volume of the charge on the tip width $L_{2}$ of the impeller in Example 5.
Solution.-The specific volume of the air entering the impeller is 15.2 cu. ft. per lb . (Example 3), $C \approx 0.85$, $U_{2}=905$ f.p.s., $T_{1}=501.2^{\circ}$ F. abs. From Eq. (11-30),

$$
\begin{aligned}
& \frac{v_{1}}{v_{2}}=\left(\frac{2 \times 0.85 \times 905^{2}-0.85^{2} \times 905^{2}}{2 \times 32.2 \times 778 \times 0.24 \times 501.2}+1\right)^{1 /(1.4-1)}=1.1329^{2.5}=1.366 \\
& v_{2} \quad \frac{15.2}{1.362}=11.112 \mathrm{cu} . \mathrm{ft} . \text { per lb. }
\end{aligned}
$$

The volume per second is

$$
Q_{2} \quad \frac{59.5}{60} \times 11.112=11.02 \text { c.f.s. }
$$

For $V_{R 2}=V_{1}=150$ f.p.s.

$$
\frac{11.02}{150} \times 144=10.6 \text { sq. in. }
$$

From Eq. (11-27), the tip width is

$$
2 \pi \times 3.75-\frac{10.6}{14 \times 0.1} \quad 0.48 \mathrm{in} .
$$

This value for tip width is based on assumed adiabatic flow through the impeller. Actually, impeller losses will place the tip width somewhere between 0.65 and 0.48 , say at about 0.55 in., but experimental data are necessary to determine the best value for $L_{2}$.

11-8. Diffusers.-Diffusers are designed to convert the kinetic energy of the air leaving the impeller into pressure energy, and they may be made either with or without guide vanes. Generally for in-line and.V-engines, the air or mixture is led off from the diffuser housing through one or two pipes, and this makes possible the use of a long spiral diffuser of gradually increasing cross section (Fig. .11-23). In radial engines, usual, though not universal, practice is to provide a diffuser with vanes which guide the air into a collector ring to which individual pipes leading to each cylinder are attached, usually at an angle (Fig. 11-20). The long spiral diffuser permits a more gradual conversion of kinetic energy, and this would indicate less turbulence and perhaps slightly greater efficiency, but the arrangement of cylinders and space limitations make the application difficult in radial engines.

If not restricted radially, air leaving the impeller will form a free vortex. If the axial width of the diffuser is held constant, say at impeller tip width $L_{2}$, the area in a radial direction will vary directly as the radius; hence the radial component of velocity $V_{R}$ will vary inversely as the radius. For constant angular momentum $M V R=$ constant. . The tangential component $V_{T}$ ( $=V \cos \alpha$ ) will also vary inversely with the radius. Thus the
resultant velocity will decrease from impeller-tip velocity $V_{2}$ inversely as the radius, and the air will follow a logarithmic spiral path, i.e., $\alpha=\alpha_{2}=$ constant. With increasing density,


Frg. 11-23.-Impeller and spiral völute type of diffuser for a Mercedes-Benz inverted V-12 engine. (From S.A.E. Jour., Vol. 49, No. 4, October, 1941.)
however, the radial component of velocity will vary inversely as the product of the radius and density, i.e.,

$$
Q=\frac{W}{d}=A_{R} v_{R}=2 \pi R L_{2} v_{R}
$$

or

$$
\begin{equation*}
v_{R}=\frac{W}{2 \pi R L_{2} d}=\frac{W v}{2 \pi R L_{2}} \tag{11-31}
\end{equation*}
$$

where $W=$ air flow, lb. per sec.

$$
v=\text { specific volume, cu. ft. per lb. }
$$

The tangential component will not be affected by change in the density since the mass $M$ is unaffected. Hence, the air will deviate from a logarithmic spiral path. However, by using the mean density $d_{m}$ or mean specific volume $v_{m}$ in the diffuser, $\alpha$ will remain constant and the mean path of the air can be approximately represented by

$$
\begin{equation*}
R=R_{2} e^{\theta \tan \alpha_{2}} \tag{11-32}
\end{equation*}
$$

where $e=2.718+$.
$\theta=$ angle between $R_{2}$ and $R$ expressed in radians.

Exampie 7.-For the supercharger in the preceding examples, determine the absolute velocity and the approximate mean path that the air would follow in the diffuser, if it was not restricted by guide vanes.

Solution.-For the mean specific volume, experimental data on diffuser entering and leaving pressures and temperatures are needed, but if unavailable, an approximation may be made as follows:

From Example 1, the manifold pressure is $42 \mathrm{in} . \mathrm{Hg}$ abs., $R_{p}=1.688$, $T_{1}=501.2$, the adiabatic horsepower $=27.45$,

$$
W=59.5 \mathrm{lb} . \text { charge per minute }
$$

and for an assumed adiabatic temperature efficiency of $e_{a}=0.7$,

$$
\text { Fluid hp. }=\frac{27.45}{0.7}=39.3
$$

Hence an equivalent polytropic exponent based on Eq. (11-7b) is,

$$
1.688^{(n-1) / 1}=\frac{39.3 \times 33,000}{59.5 \times 778 \times 0.24 \times 501.2}+1=1.232
$$

from which $n=1.669$ and $\begin{array}{cc}n-1 & 0.4\end{array}$
From Eq. (11-8), the manifold temperature is

$$
T_{\operatorname{man} .}=501.2 \times 1.688^{0.4}=619^{\circ} \mathrm{F} . \text { abs }
$$

and the specific volume in the manifold is

$$
v_{\operatorname{man} .} \quad R T \quad \frac{53.3 \times 619}{42 \times 0.491 \times 144}=11.1 \mathrm{cu} . \mathrm{ft} . \text { per } \mathrm{lb} .
$$

For adiabatic conditions, the specific volume leaving the impeller (Example 6) was $v_{2}=11.112$, but for $n=1.669, v_{2}=15.2 / 1.1329^{1.495}=12.6$. These two values for $v_{2}$ probably bracket the actual value since most sources consider the impeller to be more efficient than the diffuser. Hence it seems reasonable to assume $v_{2} \approx 12$, and, for the diffuser,

$$
12+11.1 \quad 11.5 \mathrm{cu} . \mathrm{ft} . \text { per } \mathrm{lb}
$$

From Eq. (11-31), the radial component of velocity at the impeller tip is

$$
v_{R 2} \quad \frac{59.5 \times 11.5 \times 144}{60 \times 2 \pi \times 3.75 \times 0.55}=127 \text { f.p.s. }
$$

The tangential component is

$$
V_{T 2}=C U_{2} \approx 0.85 \times 905=769 \text { f.p.s. }
$$

and

$$
\begin{aligned}
& \alpha_{2}=\arctan 127 / 769=\arctan 0.1652=9^{\circ} 22^{\prime} \\
& V_{2}=\frac{769}{\cos 9^{\circ} 22^{\prime}} \quad 780 \mathrm{f} . \mathrm{p} . \mathrm{s} .
\end{aligned}
$$

From Eq. (11-32), for $\theta=30^{\circ}=\frac{\pi}{6}=0.525$ radian

$$
R=3.75 \times 2.718^{0.525 \times 0.1652}=4.09 \mathrm{in} .
$$

For constant angular momentum, for $\theta=30^{\circ}$

$$
V_{T}=V_{T 2} \times \frac{R_{2}}{R} \times 769 \times \frac{3.75}{4.09}=705 \text { f.p.s. }
$$

and the absolute velocity of the air is

$$
V=\frac{V_{T}}{\cos \alpha_{2}}=\frac{705}{0.9867}=715 \text { f.p.s. }
$$

Similarly for

| $=60$ | 90 | 120 | 566 deg. |
| :---: | :---: | :---: | :---: |
| $R=4.45$ | 4.85 | 5.3 | 19.25 in. |
| $V=665$ | 601 | 551 | 150 f.p.s. |

These calculations show that to slow the air down to initial velocity $V_{0}=V=150$ f.p.s. in a free vortex, the diffuser would have to be abnormally large in diameter and the diffuser housing would have to be quite long. Wall friction and turbulence tend to reduce both $R$ and $\theta$, and if, in addition, the axial width is increased by passing the air to a spiral volute chamber of uniformly increasing circular or oval cross section, the vaneless diffuser can be used with in-line or V-engine superchargers.

Example 8.-By assuming that the radial-engine supercharger in the previous examples is to be adapted to a V-engine of equivalent size and performance, determine the diameter of the outlet from the diffuser.

Solution.-From Example 7, the specific volume at the diffuser outlet is $v_{\text {man. }}=11.1 \mathrm{cu} . \mathrm{ft}$. per lb.; hence, if a mean outlet• velocity equal to the inlet velocity ( $V=V_{0}=150$ f.p.s.) is assumed, the diameter of the outlet is

$$
\frac{\pi}{4} D^{2}=\frac{11.1 \times 59.5}{150 \times 60}
$$

or

$$
D=0.3055 \mathrm{ft} .=3.665 \mathrm{in} .
$$

For vaned diffusers, the passageways through the diffuser may be likened to the exit cone of a wind tunnel wherein energy losses are due to ${ }^{7}$ wall friction, angular divergence of the cone, and kinetic energy losses as the air leaves the exit cone. Applied to diffusers, these losses are somewhat conflicting in that excessive length of the passageway will increase skin friction and the bulk of the diffuser housing, a short length with a large apex angle
will increase divergence losses, and a short length with a small apex angle will increase exit losses. In addition, with diffusers, any abrupt change of direction of the air entering or leaving will be accompanied by impact losses. Hence, usual practice is to allow the air to form a free vortex from tip radius $R_{2}$ outward $1 / 2$ to 1 in. to the diffuser-vane entry radius $R_{3}$ and then set the entering edges of the vanes parallel to the path of the entering air, i.e., tangent to the logarithmic spiral at radius $R_{3}$. Since


Fig. 11-24.-Percentage losses in exit cones of various forms. (From NACA Tech. Rept. 73.)
$V_{R}$ varies with the quantity of flow, fixed vanes can be set correctly for one condition of operation only.

Diffuser vanes may be straight or curved toward the natural free path and of uniform thickness or they may be wedge shaped (Fig. 11-20). Straight vanes give the greatest deviation from the natural path, whereas curved vanes (usually arcs of circles) allow a more gradual conversion of kinetic energy, i.e., the effective length of the passageway is increased and this would indicate a reduction in the losses (Fig. 11-24). However, with a limited number of vanes of constant thickness, it is difficult to attain a low enough angle of divergence or vertex angle (Fig. 11-24) to avoid excessive turbulence in the passageway. By
gradually increasing the thickness of the vanes from radius $R_{3}$ to radius $R_{4}$, the angle of divergence can be kept low, and this would indicate an increased efficiency, but the increased losses resulting from the higher exit velocity from the diffuser passageway might largely offset the gain. Apparently, experimental methods are necessary to determine the best proportions.

Example 9.-By assuming circular-are vanes of uniform thickness, lay out diffuser proportions for the radial-engine supercharger in the preceding examples.


Fig. 11-25.-Layout for a diffuser.
Solution.-Referring to Fig. 11-25, assume a free vortex space of

$$
R_{3}-R_{2}=0.75 \mathrm{in} .
$$

From Example 7, $\alpha_{2}=9^{\circ} 22^{\prime}$. From Eq. (11-32), $\theta_{F V}=63$ deg. and dotted curve $Q P M$ is the free path of the air without guide vanes. Lay off line $P N$ normal to the free path of the air at $P$. Angle $O P N=\alpha_{2}$. Assume an angle of "wrap"' of the vane $\theta_{w}=60 \mathrm{deg}$. and an outer radius

$$
R_{4}=1.6 \times R_{3}=1.6 \times 4.5=7.2 \mathrm{in} .
$$

Construct a perpendicular bisector to a line connecting $P$ and $S$. The intersection of this bisector with $P N$ is at $N$ which is the center of are PS. Arc $P S$, the desired vane shape, is parallel to the entering air at $P$ and delivers the air to the diffuser collector ring along the line ST. Assume 15 vanes. Then angle $P O P^{\prime}=36 \% / 15=24$ deg., and vane $P^{\prime} S^{\prime}$ is laid off as before. A larger number of vanes will decrease the angle of divergence
but increase the skin friction; hence the optimum number appears to be a matter of experiment. Vane thickness may be made about $1 / 8 \mathrm{in}$. with sharp entering edges.

Air leaving the diffuser passages is usually allowed to enter a collector ring tangentially (i.e., the ring is slightly offset axially) where it may be assumed to slow down to initial velocity, $V_{0}$. The volume of the collector ring may be determined by considering it as a circular torus wherein the parts are related by

$$
\begin{equation*}
V_{C T}=2 \pi^{2} R_{5} R_{C \eta}^{2} \tag{11-33}
\end{equation*}
$$

where $V_{c T}=$ volume of the torus ring.

$$
R_{5}=\text { radius to center of the torus ring }=R_{4}+R_{c r}
$$

$R_{C T}=$ radius of the ring.
The diameter of the diffuser collector ring $\left(=2 R_{C T}\right)$ may be made four to six times the axial width of the diffuser. .

Air entering tangentially into the collector ring from the diffuser passageways will move in a helical path approximately along the line ST, Fig. 11-25. Hence, to minimize impact losses at entry to the offtake pipes leading from the collector ring to the intake valves, these pipes should join the collector ring at an angle such that their center lines at entry are approximately in a direction corresponding to line ST. Turns in the offtake pipes should be of large radius, and the diameter may be made such as to maintain the velocity approximately equal to the initial velocity $V_{0}$. To accomplish this last, however, it should be borne in mind that the offtake pipes lead to individual cylinders which take in their charge during a part of the cycle only, i.e., the flow is intermittent.

Example 10.-For the radial engine in the preceding examples, determine a suitable diameter of connecting pipe between the diffuser collector ring and the intake-valve port if the intake valve open time is 240 deg . of crankshaft travel per cycle.

Solution.-The flow for the engine is $\frac{59.5 \times 11.1}{60}=11$ c.f.s.; hence the equivalent rate of flow to each cylinder is ${ }^{1} 1 / 9=1.221$ c.f.s., but for a four-stroke-cycle engine, this amount of charge flows into the cylinder in

$$
240 / 720=\text { one-third of the time. }
$$

Therefore the equivalent continuous flow is $1.221 \times 3=3.663$ c.f.s. Then for a mean velocity of 150 f.p.s., the offtake pipe diameter is

$$
D_{O P}=12 \sqrt{\frac{4 \times 3.663}{\times 150}}: 2.12 \mathrm{in}
$$

11-9. Supercharger Drives.-For critical altitudes up to $20,000 \mathrm{ft}$. or a little more, gear-driven centrifugal superchargers have been most favored. The gearing is usually of the spur type and in two steps, although a variety of possibilities exist.


Fig. 11-26.-Principle of the exhaust turbine. (A) Diagrammatic arrangement of nozzle and blading. (B) Pressure and velocity variation in the nozzle and blading. (C) Velocity diagram of gases passing through the turbine.

At the speeds involved, the gears must be quite accurately made and care must be exercised to ensure precise balance and freedom from critical vibration. ${ }^{9,10}$

At any given speed, the problem of transmitting the necessary horsepower to the impeller is not difficult, but under conditions
of rapid engine acceleration, supercharger drive-gear stresses may become excessively large, and to avoid failure, slip clutches, springs, fluid couplings, etc., are often used. When a constantspeed propeller is used, however, the problem of protecting the supercharger drive gearing against sudden acceleration loads is greatly reduced. Impeller speed and horsepower requirements have been considered in Pars. 11-5 and 11-6. Detail design of the drive gearing is generally similar to that indicated for reduction gearing in Chap. 8.

For very high altitude operation, exhaust-turbine supercharger drives have many advantages. The exhaust turbine is quite similar to a single-stage impulse steam turbine in so far as the general arrangement is concerned. Thus, in Fig. 11-26, the combustion gases at exhaust pressure $P_{1}$ and temperature $T_{1}$ enter the nozzle. At the mouth or outlet of the nozzle, the gases have expanded to a lower pressure $P_{2}$ and have increased in velocity to $V_{2}$. In passing through the turbine wheel, the velocity drops to $V_{3}$ and some of the kinetic energy given up is utilized in producing a torque on the turbine wheel.

Referring to Fig. 11-26, for the turbine nozzle, from the basic relation for adiabatic flow of gases and for an assumed negligible entering velocity, i.e., $V_{1}=0$

$$
\begin{equation*}
\frac{V_{2}^{2}}{2 g}=778\left[C_{p}\left(T_{1}-T_{2}\right)\right] \tag{11-34}
\end{equation*}
$$

or

$$
\begin{equation*}
V_{2}=223.8 \sqrt{C_{p}\left(T_{1}-T_{2}\right)} \tag{11-35}
\end{equation*}
$$

where $V_{2}=$ velocity of exhaust gas leaving the nozzle, f.p.s.
$C_{p}=$ specific heat at constant pressure for the exhaust gases, B.t.u./(lb.)(deg. F.).
$T_{1}=$ temperature of gases in the exhaust manifold, deg. F. $T_{2}=$ temperature of exhaust gases leaving the nozzle.
But 1

$$
\frac{T_{2}}{T_{1}}=\left(\frac{P_{2}}{P_{1}}\right)^{(\kappa-1) / K}
$$

Hence

$$
\begin{equation*}
V_{t}=223.8 \sqrt{C_{p} T_{1}\left[1-\left(\frac{P_{2}}{P_{1}}\right)^{(K-1) / K}\right]} \tag{11-36}
\end{equation*}
$$

where $P_{1}=$ pressure in the exhaust manifold, lb. per sq. in. abs. $P_{2}=$ pressure of the gases leaving the nozzle, lb. per sq. in. abs.

$$
K=C_{p} / C_{v}
$$

$C_{v}=$ specific heat at constant volume for the exhaust gases, B.t.u./(lb.)(deg. F.).
For maximum absorption of kinetic energy by the turbine blades

$$
\begin{equation*}
\frac{V_{2} \cos \alpha}{2}=V_{B}=\pi D N \tag{11-37}
\end{equation*}
$$

where $\alpha=$ the angle between the center line of the nozzle and the plane of the turbine blades.
$V_{B}=$ mean velocity of the blades, f.p.s.
$D=$ mean diameter of the turbine wheel, ft .
$N=$ r.p.s. of the turbine wheel [ $=$ r.p.s. of the impeller, Eq. (11-18)].
The efficiency of the turbine blades may be expressed in terms of the kinetic energy change, thus
$e_{B}=\frac{\left(W_{G} V_{2}^{2} / 2 g\right)-\left(W_{G} V_{3}^{2} / 2 g\right)}{W_{G} V_{2}^{2} / 2 g}=1-\left(\frac{V_{3}}{V_{2}}\right)^{2}=1-\sin ^{2} \alpha$
where $W_{G}=$ flow of exhaust gas through the turbine, lb. per sec.
$V_{3}=$ velocity of the gases leaving the turbine.
The theoretical horsepower imparted to the turbine blades is proportional to the change in kinetic energy, thus
$\mathrm{hp} .=\frac{W_{G}\left(V_{2}^{2}-V_{3}^{2}\right)}{2 g \times 550}=\frac{W_{G} V_{2}^{2}\left(1-\sin ^{2} \alpha\right)}{2 g \times 550}=\frac{W_{G} V_{2}^{2}}{1,100 g} \times e_{B}$

11-10. Accessories.-Accessories such as carburetors, fuel pumps, magnetos, starters, generators, tachometers, and various kinds of pressure and vacuum pumps are usually purchased from specialty manufacturers and assembled on the engine. Hence the engine designer is at liberty to select rather than design such parts. However, to ensure proper fitting and operation, he should be generally familiar with these accessories, and he must have mounting pad and drive data.

The design of mountings and drives would appear at first thought to be merely a matter of routine layout, but accessories have become so numerous in recent years that the problem of crowding them all into the available space is no longer a simple one. In fact, in many recent large installations, the space between the rear end of the crankcase and the fire wall has been literally jammed with a maze of fittings, pipes, wiring, etc., to the point where installation, inspection, and maintenance is most difficult. A trend toward relieving this condition is observable in some very large airplanes'where space permits the use of auxiliary power plants, but in small and medium-sized planes, the main engine is still. required to support and drive practically all the accessories. Some parts, which might be classed as primary accessories, are essential to engine operation, and in any type of airplane, these should logically be mounted close by, if not actually on, the engine.

11-11. Carburetors and Fuel Pumps.-A purely rational approach to the design of a suitable size of carburetor for an engine is complicated by a large number of variables such as the intermittent character of the flow, the Venturi characteristics, and the fuel-flow characteristics at various conditions of operation. For a preliminary selection, however, the following two formulas are recommended by the Bendix-Stromberg Carburetor Company.

For one carburetor barrel feeding three or fewer cylinders,

$$
\begin{equation*}
V_{A}=\frac{D_{C} \times N_{R}}{133,000}+A_{1} \tag{11-40}
\end{equation*}
$$

and for one carburetor barrel feeding four or more cylinders,

$$
\begin{equation*}
V_{A}=\cdot \underset{480,000}{D_{C} \times n_{C} \times N_{R}+A_{I}} \tag{11-41}
\end{equation*}
$$

where $V_{A}=$ Venturi area, sq. in.
$D_{C}=$ displacement per cylinder, cu. in.
$n_{C}=$ number of cylinders.
$N_{R}=$ engine speed, r.p.m.
$A_{D N}=$ discharge nozzle area, sq. in.
Example.-Select a suitable carburetor and mounting flange for a 4.625by 4.5 -in., nine-cylinder radial engine rated $210 \mathrm{~b} . \mathrm{hp}$. at $\dot{2}, 000 \mathrm{r} . \mathrm{p} . \mathrm{m}$.

Solution.-From Eq. (11-41), the net Venturi area is

$$
V_{A}-A_{D N}=\frac{4.625^{2} \times 0.785 \times 4.5 \times 9 \times 2,000}{480,000}=2.82 \text { sq. in. }
$$

From Table A1-24, a model Na-R7A single-barrel carburetor having a barrel diameter of $2^{11 / 16} \mathrm{in}$. should be suitable, but for engines actually to be built, the carburetor manufacturer should be consulted for confirmation of the selection. From Table A1-25, a No. 7, $21 / 2-\mathrm{in}$. nominal diameter, single-barrel S.A.E. Standard carburetor flange is indicated.

Fuel may be supplied to the carburetor by gravity flow from the fuel tank or by means of a fuel pump. Fuel pumps are usually of the positive-displacement vane type with a by-pass relief valve which may be set to maintain the desired carburetor fuel supply pressure.

Fuel pumps are usually built to fit S.A.E. Standard fuel pump mounting pads (Table A1-27), the square-type pad being favored. Drive shafts designed to transmit 0.1 to 0.5 hp . (depending on the size of pump) will be adequate.

Fuel-pump capacity should be sufficient to supply at least 1 lb . of fuel per b.hp. per hour at maximum power output. Thus for an engine rated $750 \mathrm{~b} . \mathrm{hp}$. at $2,700 \mathrm{r} . \mathrm{p} . \mathrm{m}$. and using a fuel of 0.7 specific gravity, the fuel-pump capacity should not be less than

$$
\frac{750 \times 1.0}{8.33 \times 0.7}=129 \text { gal. per } \mathrm{hr}
$$

To attain this flow, a Pesco R-400 series pump (Table A1-26) would have to turn at not less than 1,600 r.p.m., i.e., the ratio of pump shaft to crankshaft r.p.m. would have to be at least $1,600 / 2,700 \approx 0.6$. However, a somewhat higher ratio, say the normally used value of 0.875 , would merely by-pass more excess fuel and allow for greater flexibility, in the control of vapor lock, but Pesco pump shaft speeds in excess of 2,500 r.p.m. are not recommended.

11-12. Magnetos, Starters, and Generators.-Aircraft-engine ignition systems may be either of the magneto or batterygenerator type; magneto ignition is by far the most common. Government requirements for engines over 100 hp . dictate the use of two separate ignition systems. In the case of magneto ignition, this means two separate units, or the equivalent, i.e., a double magneto.

Magnetos ordinarily have two, four, or eight poles, i.e, they are capable of producing two, four, or eight sparks per revolution. Thus, for a two-pole magneto on a five-cylinder, four-stroke-cycle engine, the magneto shaft should turn at 1.25 times crankshaft speed, and for a four-pole magneto on a sevencylinder, four-stroke-cycle engine, the magneto shaft should turn at 0.875 times crankshaft speed. Tables A1-28 and A1-29 give magneto selection and mounting-pad data suitable for preliminary design, but for engines actually to be built, the magneto manufacturer should be consulted for confirmation of the selection.

The simplest method of starting an aircraft engine is by swinging the propeller. This method, though somewhat dangerous, is feasible on small, low starting torque engines, but in the larger engines, starters are very desirable and in many cases necessary.

Starters may be classed as hand-turning gear, hand inertia, hand and electric inertia, direct-cranking electric, air, and combustion types. Each type has advantages and disadvantages such as cost, convenience, and continuous availability, and selection should depend on engine size, type of energy available, type and application of the airplane, etc.

Fortunately, however, S.A.E. Standard starter motor mountings are generally used by starter manufacturers so that considerable leeway is available to the engine user. Table A1-30 lists a variety of available starters together with data on S.A.E. mounting-flange number, weight, maximum engine horsepower that the starter will handle, and voltage requirements. Table A1-31 gives data on standard S.A.E. starter motor mountings.

Engine-driven generators are usually built to fit standard S.A.E. mounting pads, and a sizable range of types and capacities can be had for a given mounting. Table A1-32 gives some generator selection and mounting-pad data.

11-13. Tachometers and Miscellaneous Accessories.-To facilitate the checking of operating conditions, practically all aircraft engines are arranged to permit the observation of crankshaft r.p.m. This involves a tachometer-drive connection in which the drive shaft generally turns at one-half crankshaft speed, presumably because early engines were of the in-line or $V$ type, and a convenient point of attachment for the tachometer
drive was the end of the camshaft. Table A1-33 gives S.A.E. Standard tachometer-drive data.

In addition to the accessories more or less commonly found on all aircraft engines, additional drives for hydraulic pumps, vacuum pumps, propeller governors, etc., frequently are needed. For the most of these miscellaneous accessories, the S.A.E. has endeavored to standardize mounting pads and flanges. Hence, the designer confronted with the problem of selecting and mounting these accessories usually will find standard mounting data in the S.A.E. "Handbook." For data on these special accessories, the designer is referred to the current literature of the accessory manufacturers.

11-14. Accessory-drive Details.-In view of the number of accessories usually required, some ingenuity on the part of the designer is necessary to obtain a simple and effective arrangement. Power for driving must come either directly or indirectly from the crankshaft, and to keep the arrangement as simple as possible, a main accessory shaft usually is splined to the rear end of the crankshaft. Drive shafts for each accessory are then geared for desired speed ratios to the main accessory shaft. Such drives can be very skillfully arranged or badly cluttered, depending upon the ingenuity of the designer. For the student, a probable best approach is to study the arrangements used in current successful engines even to the extent of sketching such arrangements as most nearly conform to the needs for his engine. This will enable him to visualize the problem more clearly and to draw on previous experience.

## Suggested Design Procedure

1. Select materials and sketch in the main crankcase section on the assembly drawings or on superimposed tracing paper. Check the arrangement for weak points such as fabrication difficulties, sharp reentrant corners in highly stressed parts, unnecessarily indirect stress paths, interference of parts, assembly difficulties, etc.
2. Make detail drawings of each part of the crankcase.
3. Design and make detail drawings of the oil pump and connecting parts.
4. If a supercharger is to be built into the engine, sketch a general layout of the proposed arrangement.
5. If a supercharger is to be used, determine speed and power requirements.
6. If a supercharger is to be used, determine detail dimensions for the impeller, and make detail drawings.
7. If a supercharger is to be used, determine detail dimensions for the diffuser and make detail drawings.
8. If a supercharger is to be used, determine detail dimensions of the drive gearing and make detail drawings.
9. List all accessories that are to be included or provided for, and make sketches approximately to scale showing the proposed arrangement for attaching and operating. Study of arrangements used in current successful engines will be very helpful in planning the accessory grouping. "Mockups" may even be necessary as aids to visualizing the desired arrangement.
10. With the accessory grouping planned to ensure proper and effective functioning of each unit, determine necessary detail dimensions, and make detail drawings of drives, mounting pads, etc., properly arranged in relation to adjacent parts.
11. Lay out the accessory section of the crankcase, and check for rigidity, ease of fabrication, assembly difficulties, structural weaknesses, etc.
12. Make detail drawings of the accessory section of the crankcase.
13. Design and make detail drawings of all remaining miscellaneous parts.
14. Transfer all remaining detail parts to complete the assembly drawings of the engine.
15. When items 1 to 14 have been completed and put in proper form, submit for checking and approval.

## Problems

1. A $53 / 16$ - by $53 / 16$-in., 14 -cylinder, 6.75 -compression-ratio engine is rated $750 \mathrm{~b} . \mathrm{hp}$. at 2,550 r.p.m. at $9,500 \mathrm{ft}$. altitude $\left(P_{\mathrm{atm}}=20.98 \mathrm{in} . \mathrm{Hg}\right.$ abs., $t_{\mathrm{atm}}=25.1^{\circ} \mathrm{F}$.). The fuel rate is 0.58 lb . per b.hp. hr., and the air:fuel ratio is $12.3: 1$ by weight. Assuming an over-all adiabatic efficiency of 65 per cent, estimate the horsepower required to drive the supercharger.
2. For the engine in Problem 1, the impeller-crankshaft speed ratio is 11:1. Determine the impeller diameter, tip speed, and r.p.m.
3. For the engine in Problems 1 and 2, determine the inlet diameter of the impeller if the angle of approach is 10 deg., the impeller-hub diameter is 1.5 in ., there are 16 impeller blades having an entering edge thickness of 0.05 in., and the mean velocity in the inlet pipe is 150 f.p.s.
4. For the engine in the preceding three problems, assume $F=1.2 \mathrm{in}$. (see Fig. 11-22), and determine the hub length and curvature.
5. For the engine in the preceding four problems, determine the width of the impeller blades for a constant area of passage.

6: Determine the effect of change in specific volume of the charge on the tip width $L_{2}$ of the impeller in Problem 5.
7. For the supercharger in the preceding problems, determine the absolute velocity and the approximate mean path that the air would follow in the diffuser if it was not restricted by guide vanes.
8. Assuming the radial engine supercharger in the preceding problems is to be adapted to a V-engine of equivalent size and performance, determine the diameter of the outlet from the diffuser.
9. Assuming circular-arc vanes of uniform thickness, determine and lay out diffuser proportions for the radial-engine supercharger in the preceding problems.
10. For the radial-engine supercharger in the preceding problems, determine suitable dimensions for the diffuser collector ring.
11. For the radial engine in the preceding problems, determine a suitable diameter of connecting pipe between the diffuser-collector ring and the intake-valve port if the intake-valve open time is 250 deg . of crankshaft travel per cycle.
12. To increase the rated altitude of the engine in Problem 1 to 25,000 ft. $\left(P_{\mathrm{atm}}=11.1 \mathrm{in} . \mathrm{Hg}\right.$ abs., $t_{\mathrm{atm}}=-30.15^{\circ} \mathrm{F}$.), it is planned to use an exhaust-turbine supercharger ahead of the gear-driven supercharger. Exhaust manifold temperature $=1340^{\circ} \mathrm{F}$.,

$$
\text { exhaust manifold pressure }=30 \mathrm{in} . \mathrm{Hg} \text { abs., }
$$

turbine-wheel mean diameter $=9$ in.,
angle of nozzle to plane of blades $=20 \mathrm{deg}$.,
specific heats of exhaust gas, $C_{p}=0.24, . C_{v}=0.17$. Adiabatic temperature efficiency of the air impeller driven by the turbine $=70$ per cent.
a. Find the turbine speed in r.p.m.
$b$. Find the diameter of the air impeller necessary to compress the air from $25,000 \mathrm{ft}$. to the equivalent of $9,500 \mathrm{ft}$.
c. Find the fluid horsepower necessary for the air impeller.
d. What proportion of the exhaust gases must pass through the turbine if the over-all turbine efficiency is 50 per cent?

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## APPENDIX 1

Table A1-1.-American Aircraft Engines
(From Automotive Ind., Vol. 82, No. 5, Mar. 1, 1940)


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Table A1-1.-American Aircraft Engines.-(Continued)











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Table A1-1.-American Aircraft Engines.-(Continued)



Symbolis and Abbreviations

$\qquad$ $m 75$ per cent power allowable. ${ }^{n} 7.14$ and 10.00:1 blower Liq-Liquid. Mil-Military. Pend-A. T. C. pending. W-Water, two-speed supercharger. - Unit consists of two sixRate with controllable propeller at $2,000 \mathrm{ft}$. ${ }^{i}$ Dual type. $\qquad$
 General
a Based on maximum horse-
power.
© Optional,
c 87 octane rating for take-
off.
d Applies to motor with
0.5625 propeller-gear ratio.
e Gear-drive engines also
available at same rating.
Table A1－1．－American Aircraft Eingines．－（Continued）

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|  |  | प7P！${ }^{\text {a }}$ | $\vdots \vdots \vdots \vdots \vdots \vdots \vdots$ |  |
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| ৪ | 888 |  |  |  |

[^21]Symbols and Abbreviations

| Starter Make <br> Au－Auto－Lite． <br> Eel－Eclipse． <br> Opt－Optional． | PE－Propeller swing or elec－ tric motor． <br> PS－Propeller swing． |
| :---: | :---: |
| Method of Starting | Eugine Manufacturers |
| A－DE－Air or direct crank－ ing electric． | ${ }^{1}$ Akron Aircraft Inc． <br> ${ }^{2}$ Monocoupe Corp． |
| DE－Direct cranking elec－ tric． | ${ }^{3}$ Lenape Aircraft Motors， Inc． |
| EI－Electric inertia． | ${ }^{4}$ Aviation Mfg．Corp． |
| EM－Electric motor． | ${ }^{5}$ Sky Motors． |
| HC－Hand crank． | ${ }^{6}$ Aircooled Motor ${ }^{\text {C Corp．}}$ |

Table A1-2.-Foreign Airplane-engine Data (From Automotive Ind., Feb. 27, 1937)

British

| Rolls-Royce, Kestrel X, XI, XII. . . . . . . . . . . . . . . . . . . . . . . . . | V60 | Liq | 12 | $5.00 \times 5.50$ | 1,296.0 | 7.00 | 127 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Rolls-Royce, Kestrel XIV, XV, XVI. | V60 | Liq | 12 | $5.00 \times 5.50$ | 1,296.0 | 6.00 | 127 |
| Rolls-Royce, Kestrel IV, V, VI (V.P.).. | V60 | Liq | 12 | $5.00 \times 5.50$ | 1,296.0 | 6.00 | 119 |
| Rolls-Royce, Kestrel VII, VIII, IX (V.P.). | V60 | Liq | 12 | $5.00 \times 5.50$ | 1,296.0 | 6.00 | 134 |
| Rolls-Royce, Kestrel XIV, XV, XVI (V.P.)..... | V60 | Liq | 12 | $5.00 \times 5.50$ | 1,296.0 | 6.00 | 127 |
| Czechoslovakia |  |  |  |  |  |  |  |
| Walter, Atom.. | H | Air | 2 | $3.35 \times 3.78$ | 67.1 | 5.20 | 113 |
| Walter, Mikron. | I | Air | 4 | $3.35 \times 3.78$ | 133.0 | 5.20 | 117 |
| Walter, Minor. | I | Air | 4 | $4.14 \times 4.53$ | 244.0 | 5.30 | 122 |
| Walter, Junior. | I | Air | 4 | $4.53 \times 5.51$ | 354.8 | 5.20 | 117 |
| Walter, Major-4. | I | Air | 4 | $4.65 \times 5.51$ | 373.6 | 5.20 | 121 |
| Walter, Major-6. | $\stackrel{\text { I }}{ }$ | Air | ${ }^{6}$ | $4.65 \times 5.51$ | 561.2 | 5. 20 | 128 |
| Walter, Sagitta I-RC. | V60 | Air | 12 | $4.65 \times 5.51$ | 1,120.6 | 5.50 | 118 |
| Walter, Sagitta II-RC. | V60 | Air | 12 | $4.65 \times 5.51$ | 1,120.6 | 5.50 | 118 |
| Walter, Gemma I... | Rad | Air | 9 | $4.13 \times 4.72$ | 570.4 | 5.30 | 117 |
| Walter, Scolar. | Rad | Air | 9 | $4.13 \times 3.94$ | 475.8 | 5.40 | 121 |
| Walter, Bora II. | Rad | Air | 9 | $4.13 \times 4.72$ | 570.4 | 6.30 | 133 |
| Walter, Bora II-R. | Rad | Air | 9 | $4.13 \times 4.72$ | 570.4 | 6.30 | 133 |
| Walter, Castor II. | Rad | Air | 7 | $5.32 \times 6.69$ | 1,038.8 | 6.00 | 111 |
| Walter, Pollux II. | Rad | Air | 9 | $5.32 \times 6.69$ | 1,335.9 | 6.00 | 112 |
| Walter, Pollux II-R....... | Rad | Air | 9 | $5.32 \times 6.69$ | 1,335.9 | 6.00 | 103 |
| Walter, Super Castor I-RC. | Rad | Air | 9 | $5.32 \times 5.75$ | 1,146.8 | 5.50 | 119 |
| Walter, Super Castor II-RC. | Rad | Air | 9 | $5.32 \times 5.75$ | 1,146.8 | 5.50 | 110 |
| French |  |  |  |  |  |  |  |
| Farman, 7EAr. | Rad | Air | 7 | $4.53 \times 5.32$ | 600.22 | 5.20 | 73 |
| Farman, 7ED.. | Rad | Air | 7 | $4.53 \times 5.32$ | 600.22 | 5.20 | 82 |
| Farman, 9EBr. | Rad | Air | 9 | $4.53 \times 5.32$ | 768.33 | 5.20 | 83 |
| Farman, 12WIrs | WI | Liq | 12 | $5.32 \times 5.12$ | 1,305.72 | 6.40 | 111 |
| Farman, 12WKrs. | WI | Liq | 12 | $5.32 \times 5.12$ | 1,365.72 | 6.40 | 115 |

Table A1-2.-Foreign Airplane-engine Data.-(Continued)

| Make and model <br> (Data cortinued on pp. 334 and 335) | Cylinder data |  |  |  |  | Ratings |  |  |  |  |  |  |  | Propeller drive | Weight, lb. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Blower ratio | $\left.\begin{array}{\|c\|} \text { Cylin- } \\ \text { der } \\ \text { mate- } \\ \text { rial } \end{array} \right\rvert\,$ | Valves per cylinder |  |  | Maximum except take-off |  |  | Take-off |  | Cruising |  | $\begin{gathered} \text { Oc- } \\ \text { tane } \\ \text { rating } \end{gathered}$ |  |  |  |
|  |  |  | $\begin{gathered} \text { In- } \\ \text { take } \end{gathered}$ | $\begin{array}{\|c\|} \text { Ex- } \\ \text { haust } \end{array}$ | $\begin{array}{\|c\|} \hline \text { Ar- } \\ \text { range-- } \\ \text { ment } \end{array}$ | Hp. | R.p.m. | At sea level or altitude | Hp. | R.p.m. | Hp. | R.p.m. |  |  | $\left\lvert\, \begin{gathered} \text { or } \\ \text { starter } \end{gathered}\right.$ | $\begin{aligned} & \text { ing } \\ & \text { hp. } \end{aligned}$ |


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Table A1－2．－Foreign Airplane－engine Data．－（Continued）

| Make and model | Carburetors |  | Fuel pump sup－ plied | Igaition system |  |  | Starting |  | Installation dimensions over－all，in． |  |  | Height above engine bed，in． | Center－ to－center engine bearers， in． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| pp． 332 and 333） | Num－ ber | Make |  | Make | Current | Num－ ber | Make | Method | Length | Height | Width |  |  |

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Table A1-2.-Foreign Airplane-engine Data.-(Continued)

| Make and model | Cylinder data |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Arrangement | Cooling | Number of cylinders | Bore, stroke, in. | Piston displacement, cu. in. | Compression ratio | B.m.e.p. at cruising hp. |
| French |  |  |  |  |  |  |  |
| Farman, 12 Crs... | V60-1 | Liq | 12 | $3.94 \times 4.72$ | 690.41 | 7.40 | 103 |
| Gnome-Rhone, Mistral Major 14No. | Rad | Air | 14 | $5.75 \times 6.50$ | 2,358.80 | 6.10 | 139* |
| Gnome-Rhone, Mistral Major 18L. | Rad | Air | 18 | $5.75 \times 7.09$ | 3,308.64 | 6.10 | $145 *$ |
| Gnome-Rhone, Mistral Major 14M. | Rad | Air | 14 | $4.80 \times 4.57$ | 1,157.78 | 6.50 | 148* |
| Hispano Suiza, 12Y21.... | V60 | Liq | 12 | $5.91 \times 6.69$ | 2,196.0 | 7.00 | 133* |
| Hispano Suiza, 12Xirs-1. | V60 | Liq | 12 | $5.12 \times 6.69$ | 1,647.0 | 5.80 | 158* |
| Hispano Suiza, 14AA-04. | Rad | Air | 14 | $6.13 \times 6.69$ | 2,759.6 | 6.20 | 151* |
| Hispano Suiza, 14AB-02. | Rad | Air | 14 | $5.32 \times 5.12$ | 1,589.0 | 6.20 | 141* |
| Renault, 4PGI...... | I | Air |  | $4.72 \times 5.51$ | 386.1 | 5.30 | 103 |
| Renault, 4PEI. | I | Air | 4 | $4.72 \times 5.51$ | 386.1 | 5.70 | 107 |
| Renault, 6Q01. | I | Air | 6 | $4.72 \times 5.51$ | 579.5 | 6.40 | 111 |
| Renault, 6Q03. | I | Air | 6 | $4.72 \times 5.51$ | 579.5 | 6.50 | 116 |
| Renault, 12R01. | V60 | Air | 12 | $4.72 \times 5.51$ | 1,159.0 | 6.40 | 111 |
| Renault, 14T... | Rad | Air* | 14 | $6.06 \times 6.93$ | 2,806.0 | 6.40 | 122 |
| Salmson, 9AdR-60cv. | Rad | Air |  | $2.76 \times 3.39$ | 181.8 | 5.60 | 101* |
| Salmson, 9AeRS-75cv. | Rad | Air | 9 | $2.76 \times 3.39$ | 181.8 | 5.60 | 126* |
| Salmson, 9ND-175cv. | Rad | Air | 9 | $3.94 \times 5.51$ | 603.9 | 5.30 | 125* |
| Salmson, 9Aba-280cv. | Rad | Air | 9 | $4.92 \times 6.69$ | 1,142.5 | 5.30 | 105* |
| Salmson, $9 \mathrm{Na}-350 \mathrm{cv}$. | Rad | Air | 0 | $5.51 \times 6.30$ | 1,350.5 | 5.30 | 117* |
| Salmson, $9 \mathrm{NaS}-350-630 \mathrm{cv}$ | Rad | Air | 9 | $5.51 \times 6.30$ | 1,350.5 | 5.30 | 112* |
| Salmson, 18AbS-570-965cv. | Rad | Air | 18 | $4.92 \times 7.09$ | 2,426.6 | 5.30 | 89* |
| Salmson, 6TE-170cv.. | I | Air | 6 | $4.53 \times 5.04$ | 486.2 | 5.50 | 136* |
| Salmson, 6TES-250cv. | I | Air | 6 | $4.53 \times 5.04$ | 486.2 | 5.50 | 163* |


| Argus, As10C. | V90 | Air | 8 | $4.72 \times 5.51$ | 772.7 | 5.90 | 109 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Brandenburg, Sh14A-4. | Rad | Air | 7 | $4.25 \times 4.72$ | 469.7 | 6.00 | 106 |
| Brandenburg, SAM322H2. | Rad | Air | 9 | $6.06 \times 6.30$ | 1,636.0 | 6.40 | 126 |
| Hirth, 60R-2. | I | Air | 4 | $4.01 \times 4.33$ | 220.0 | 5.80 | 106 |
| Hirth, 504A-1. | I | Air | 4 | $4.13 \times 4.53$ | 244.0 | 6.00 | 117 |
| Mercedes-Benz, Diesel OF2. | V60 | Liq | 12 | $6.50 \times 8.27$ | 3,295.2 | 15.00 | 100 |
| Junkers, Jumo L5G. | I | Liq | 6 | $6.30 \times 7.48$ | 1,398.1 | 5.50 |  |
| Junkers, Jumo 205C. | I | Liq : | 6 | $4.13 \times$ (c) | 1,013.8 | 17.00 | 100 |
| Junkers, Jumo 205D. | I | Liq | 6 | $4.13 \times$ (c) | 1,013.8 | 17.00 | 105 |
| Italian |  |  |  |  |  |  |  |
| Fiat, A24R. | V60 | Liq | 12 | $5.51 \times 6.89$ | 2,002.0 | 5.70 | 115 |
| Fiat. A30RA | V60 | Liq | 12 | $5.31 \times 5.51$ | 1,713.6 | 8.00 | 77 |
| Fiat, A54. | Rad | Air | '7 | $4.13 \times 4.72$ | 493.5 | 5.50 | 84 |
| Fiat, A70.. | Rad | Air | 7 | $4.53 \times 4.53$ | 510.0 | 5.75 | 120 |
| Fiat, A74RC. | ${ }_{¢}$ Rad | Air | 14 | $4.53 \times 4.53$ | 1,900.3 | 6.50 | 145* |
| Fiat, A80RC. | Rad | Air | 18 | $5.51 \times 0.50$ | 2,788.9 | 6.50 | 135* |
| Isotta Fraschini, 750R. | W | Liq | 18 | $5.12 \times 6.69$ | 4,073.1 | 5.70 | 70 |
| Isotta Fraschini, 750RC. | W | Liq | 18 | $5.12 \times 0.69$ | 4,073.1 | 5.70 | 70 |
| Isotta Fraschini, XIR. | V | Liq | 12 | $5.75 \times 6.30$ | 1,991.0 | 6.70 | 103 |
| Isotta Fraschini, XIRC40 | V | Liq | 12 | $5.75 \times 6.30$ | 1,991.0 | 6.40 | 105 |
| Isotta Fraschin, Caccia. | V | Liq | 12 | $4.92 \times 5.12$ | 1,257.2 | 5.70 | 119 |
| Isotta Fraschini, Astro 7C-21. | Rad | Air | 7 | $6.06 \times 6.30$ | 1,272.2 | 5.95 | 110 |

Table A1-2.-Foreign Airplane-engine Data.-(Continued)



| German |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Argus. | 2.34 | 2 | Sum | Yes | Bos | Mag | 2 | Own | HA | 43.51 | 28.27 | 34.64 | 9.29 | 18.74 |
| Bradenburg. | 2.32 | 1 | Sum | Yes | Bos | Mag | 2 | Own | CA | 38.39 | 36.85 | ..... | ..... | 18.81 |
| Brandenburg. .... | 2.08 | 1 | Sum | Yes | Bos | Mag | 2 | Bos | HC | 50.59 | 52.13 | ..... | ..... | 22.05 |
| Hirth. . | 3.24 | 1 | Sum | Opt | Bos | M \& B | e | Own | HC | 33.70 | 27.10 | 15.40 | 11.80 | 6.50 |
| Hirth. | 2.87 | 1 | Pal | Opt | Bos | M \& B | e | Own | HC | 37.70 | 28.60 | 19.90 | 8.45 | 11.00 . |
| Mercedes-Benz... | 2.87 |  |  | Yes |  |  | . | DG | .... | 74.02 | 42.32 | 38.58 | 25.20 | 29.92 |
| Junkers. | 2.01 | 1 | Sum | Yes | Bos | Mag | 2 | Own | CA | 70.86 | 47.84 | 25.59 | ..... | 34.10 |
| Junkers. | 2.24 |  |  | Yes |  |  | . | Own | CA | 76.50 | 52.17 | 21.54 | $\ldots .$. | 22.85 |
| Junkers. | 1.94 |  |  | Yes |  |  |  | Own | CA | 76.50 | 52.17 | 21.54 | ..... | 22.85 |
| Junkers. |  |  |  |  |  | $\ldots$ |  |  |  |  |  |  |  |  |
| Italian |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Fiat. | 2.31 | 2 | Own | Yes | Mar | Mag | 2 | Own | CA | 69.69 | 41.93 | 28.93 | 25.39 |  |
| Fiat. | 2.55 | 3 | Own | Yes | Mar | Mag | 2 | Own | CA | 68.94 | 30.81 | 25.71 | 21.81 |  |
| Fiat | 3.31 | 1 | Str | Yes | Mar | Mag | 2 | Own | CA | 21.30 | 36.81 | 25.71 | 21.81 |  |
| Fiat | 2.37 | 1 | Str | Yes | Mar | Mag | 2 | Mar | CA | 20.71 | 36.61 | 25.71 | 21.81 |  |
| Fiat | 1.48* | 1 | Str | Yes | Mar | Mag | 2 | Own | CA | 41.14 | 47.05 | 25.71 | 21.81 |  |
| Fiat. | 1.60* | 1 | Own | Yes | Mar | Mag | 2 | Own | CA | 45.47 | 52.56 | 25.71 | 21.81 |  |
| Isotta Fraschini.. | 2.81 | 6 | Own | Yes | Mar | Mag | 2 | Own | CA | 85.04 | 41.92 | 40.55 |  |  |
| Isotta Fraschini. . | 2.92 | 0 | Own | Yes | Mar | Mag | 2 | Own | CA | 86.37 | 47.44 | 40.55 |  |  |
| Isotta Fraschini. . | 2.86 | 4 | Own | Yes | Mar | Mag | 2 | Own | CA | 75.16 | 40.16 | 32.40 |  |  |
| Isotta Fraschini. . | 2.64 | 4 | Own | Yes | Mar | Mag | 2 | Own | CA | 83.88 | 42.84 | 32.84 |  |  |
| Isotta Fraschini. . | 1.75* | 4 | Zen | Yes | Mar | Mag | 2 | Own | CA | 69.92 | 31.89 | 29.13 |  |  |
| Isotta Fraschini. . | 2.20 | 1 | Own | Yes | Mar | Mag | 2 | Own | CA | 19.84 | 47.25 |  |  |  |

For footnotes to table see 1. 342 .

Symbols and Abbreviations For Table A1-2

General
*-Based on maximum horsepower.
(c) $-2 \times 6.30$ (two cycle).

HO-Heavy oil.
Opt-Optional.
SL-Sea level.
Cylinder Arrangement
Hor-Horizontal.
H4-Four banks of four cylinders each in H formation.
H6-Four banks of six cylinders each in H formation.
I-In line.
Rad-Radial.
V-V.
V60-V type, 60 deg.
V60-I-V type, 60 deg., inverted.
V90-V type, 90 deg.
W-Three banks of cylinders.
WI-Three banks of cylinders -inverted.

Cooling
Liq-Liquid.
Cylinder Material
1-Aluminum with cast-iron liner.
2-Aluminum with steel liner.
3-Cast iron.
7-Steel with aluminum heads.
8-Steel.
10-Cast-iron with steel sleeves.

Valve Arrangement
F-F-head.
I-In head with push rods and rocker arms.
OH -Overhead camshaft.
L-i head-valve at side.

Propeller Drive
D-Direct.
G-Geared.

Carburetor Make
Ama-Amal.
Bro-Bronzania.
Cla-Claudel-Hobson.
Pal-Pallas.
Str-Stromberg.
Zen-Zenith.
Ignition and Starting Systems, Make

Bos-Bosch.
BW-British Thompson Houston or Watford.
BTH—British Thompson Houston.
Duc-Ducellier.
DG-Druckluft \& Gluhkerzen.
Mar-Marell.
RB-Robert Bosch.
Rot-Rotax.
Scin-Scintilla.
Starting Method
CA-Compressed air.

Car-Cartridge.
EM-Electric motor.
GD-Gas distributor and handturning gear.
HA-Hand crank.
HC-Hand crank from machine.
HE-Hand crank, or electric motor.

In-Inertia.
PS-Propeller swing.
Current Sources
Bat-Battery.
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Table A1-3.-American Stock, Marine, and Commergial Vehicle Engines.-(Continued)

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Table A1－3．－American Stock，Marine，and Commercial Vehicle Engines．－（Continued）

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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)


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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)




[^22]Table A1-3.-American Stock, Marine, and Commerctal Vehicle Engines.-(Continued)




Table A1－3．－American Stock，Marine，and Commercial Vehicle Engines．－（Conlinued）

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Table A1－3．－American Stock，Marine，and Commerctal Vehicle Engines．－（Continued）

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Table Al－3．－American Stock，Marine，and Commercial Vehicle Engines．－（Continued）

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Table A1－3．－American Stock，Marine，and Commercial Vehicle Engines．－（Continued）

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Table A1－3．－American Stock，Marine，and Commercial Vehicle Engines．－（Continued）

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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)



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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)



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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)




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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)


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Table A1-3.-American Stock, Marine, and Commercial Vehicle Engines.-(Continued)




Table A1-3.-American Stock, Marine, and Commerctal Vehicle Engines.-(Continued)

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Table A1－3．－American Stock，Marine，and Commerctal Vehicle Engines．－（Continued）

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## Table A1-4.-Rotating and Reciprocating Weights in Aircraft Engines

(From Angle, "Engine Dynamics and Crankshaft Design," and S.A.E. Jour., Vol. 29, Nos. 4 and 5, October, November, 1931)

| Engine | Type |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Liberty- | 6-cyl. vertical | 5.00 | 7.00 | 19.63 | 137.4 | 5.80 | 3:70 | 0.295 | 0.069 |
| Rausie-E-6 | $6-\mathrm{cyl}$. vertical | 5.00 | 6.00 | 19.63 | 117.8 | 5.99 | 3.73 | 0.305 | 0.074 |
| Hall-Scott, L-6. | 6 -cyl. vertical | 5.00 | 7.00 | 19.63 | 137.4 | 5.95 | 3.13 | 0.303 | 0.066 |
| Isotta-Fraschini | 6-cyl. vertical | 5.51 | 7.08 | 23.86 | 169.0 | 7.20 | 3.80 | 0.302 | 0.065 |
| Benz-200. | 6 -cyl. vertical | 5.51 | 7.48 | 23.86 | 178.4 | 6.40 | 4.40 | 0.268 | 0.061 |
| B.hp.-200 | 6-cyl. vertical | 5.71 | 7.48 | 25.62 | 191.3 | 6.50 | 3.80 | 0.254 | 0.054 |
| Mercedes-200. | $6-\mathrm{cyl}$. vertical | 5.51 | 6.30 | 23.86 | 150.3 | 9.40 | 3.30 | 0.395 | 0.085 |
| Aeromarine, U-8 | 8-cyl. V | 4.50 | 6.50 | 14.18 | 32.2 | 3.60 | 2.60 | 0.266 | 0.067 |
| Wright-E. | 8-cyl. V | 4.72 | 5.11 | 17.53 | 89.9 | 4.60 | 2.30 | 0.262 | 0.077 |
| Wright-H. | 8-cyl. V | 5.51 | 5.90 | 23.82 | 140.8 | 7.20 | 3.10 | 0.302 | 0.073 |
| Packard-744 | 8-cyl. V | 4.75 | 5.25 | 17.72 | 93.0 | 5.00 | 2.35 | 0.282 | 0.079 |
| Curtiss-K12 | 12-cyl. V | 4.50 | 6.00 | 15.92 | 95.4 | 3.35 | 1.70 | 0.210 | 0.053 |
| Liberty-12. | 12-cyl. V | 5.00 | 7.00 | 19.63 | 137.4 | 6.20 | 3.15 | 0.315 | 0.068 |
| Rolls-Royce "Eagle" | 12-cyl. V | 4.50 | 6.50 | 15.90 | 103.4 | 3.75 | 1.92 | 0.236 | 0.055 |
| Packard-1237. | 12-cyl. V | 5.00 | 5.25 | 19.63 | 103.1 | 5.83 | 2.56 | 0.297 | 0.081 |
| Packard-2025. | 12-cyl. V | 5.75 | 6.50 | 26.00 | 168.8 | 8.06 | 4.01 | 0.310 | 0.072 |
| Duesenberg-H. | 16-cyl. V | 6.00 | 7.50 | 28.27 | 212.1 | 6.29 | 3.47 | 0.219 | 0.046 |
| Napier-"Lion". | 12-cyl. W | 5.50 | 5.125 | 23.76 | 121.7 | 5.50 | 2.13 | 0.321 | 0.063 |
| Eng. Div. W-1-A | 18-cyl. W | 5.50 | 6.50 | 23.76 | 154.4 | 7.40 | 3.74 | 0.312 | 0.072 |
| Lawrence-L. | 3-cyl. radial | 4.25 | 5.25 | 14.20 | 74.5 | 3.05 | 1.50 | 0.215 | 0.061 |
| A.B.C. "Wasp". | 7-cyl. radial | 4.53 | 5.91 | 16.12 | 95.2 | 2.30 | 1.41 | 0.143 | 0.039 |
| Lawrence R-1 | 9-cyl. radial | 4.25 | 5.25 | 14.18 | 74.5 | 3.05 | 2.83 | 0.215 | 0.079 |
| ABC "Dragon Fly" | 9 -cyl. radial | 5.50 | 6.50 | 23.76 | 154.4 | 4.20 | 2.59 | 0.177 | 0.044 |
| Curtiss V-1570 | 12-cyl. V | 5.125 | 6.25 | 20.6 | 129 | 4.11* | 2.68 | 0.200 | 0.053 |
| (Conqueror). |  |  |  |  |  | $3.9 \dagger$ | 2.68 | 0.189 | 0.051 |
| Wright R 1750 | 9 -cyl. radial | 6.00 | 6.875 | 28.25 | 169.8 | 7.45* | 2.80 | 0.264 | 0.061 |
| (Cyclone) |  |  |  |  |  | $6.74+$ | 2.80 | 0.237 | 0.057 |

[^27]Table A1－5．－Crankpin Data

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|  | 㙳 |  |

Table A1-6.-Crankshaft Main Bearing Data for In-line and V-engines

| Engine | Type | Bore and stroke, in. | Hp. and r.p.m. | Crankshaft bearing | $\begin{gathered} \text { Diam- } \\ \text { eter, } \\ \text { in. } \end{gathered}$ |  | $L / D$ | $\begin{aligned} & \text { Pro- } \\ & \text { jected } \\ & \text { area, } \\ & \text { sq. in. } \end{aligned}$ | Rub- <br> bing <br> veloc- <br> ity, <br> f.p.s. | $\begin{gathered} \text { Bearing } \\ \text { pressure } \\ \text { ib. per sq.in. } \end{gathered}$ |  | Rubbing factor | $V / P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  | Max. | Mean |  |  |
| Liberty $6 \ldots \ldots \ldots \ldots$ | 6-cyl. vertical | $5 \times 7$ | 240 at 1,800 | Center | 2.625 | 1.625 | d. $6: 9$ | 4.27 | 20.6 | $\overline{1,219}$ | 957 | $\overline{19,750}$ | $\overline{0.02155}$ |
|  |  |  |  | Intermediate | l 2.625 | ${ }_{1}^{1.625}$ | 0.6:? | ${ }_{4}^{4.27}$ | 20.6 | ${ }_{691}^{984}$ | 548 | 11,300 | 0.0376 0.0391 |
| Chevrolet(1938). Master | 6-cyl. vertical | $3.5 \times 3.75$ | 85 at 3,200 | No. 1 | 2.6875 | 1.1875 | $\overline{0.111}$ | $\overline{3.185}$ | 37.6 |  |  |  | 0 |
|  |  |  |  | No. 2 | 2.719 | 1.1875 | 0. $1: 36$ | 3.22 | 38.0 |  |  |  |  |
|  |  |  |  | No. 3 | 2.75 | 1.4375 | 0.8! | 3.95 | 38.4 |  |  |  |  |
|  |  |  |  | No. 4 | 2.781 | 1.625 | 0.ix: | 4.52 | 38.9 |  |  |  |  |
| $\overline{\text { Nash Ambassador Six }}$(1938). | 6-cyl. vertical | $3.375 \times 4.375$ | $\overline{105 ~ a t ~ 3,400 ~}$ | No. 1 | 2.485 | 1.25 | 0.:30 | 3.11 | 36.9 |  |  |  |  |
|  |  |  |  | No. ${ }^{2}$ | 2.485 | 0.9375 | - | 2.33 | 36 |  |  |  |  |
|  |  |  |  | No. 4 | 2.485 | 1.875 | 0:\%\% | 4.66 | 36.9 |  |  |  |  |
|  |  |  |  | No. 5 | 2.485 | 0.9375 | 0.337 | 2.33 | 36.9 |  |  |  |  |
|  |  |  |  | No. 6 | 2.485 | 0.9375 | 0.:377 | 2.33 | 36.9 |  |  |  |  |
|  |  |  |  | No. 7 | 2.485 | 1.625 | 0. 4 , | 4.04 | 36.9 |  |  |  |  |
| Hispano 300........ | 8-cyl. V | $5.51 \times 5.9$ | 325 at 1,800 |  | $2.52$ | 1.893 | 0.7\%; | 4.765 | 19.8 | 1, 315 | 989 | 19, 120 | $\overline{0.0200}$ |
|  |  |  |  | Intermediate End | $\left\lvert\, \begin{aligned} & 2.52 \\ & 2.52 \end{aligned}\right.$ | 1.893 4.255 | 0.7.) | \|4.765 <br> 10 <br> 715 | 19.8 | 1,2693 | 512 | 10, 111 | 0.0386 0.0765 |
| Wright H-2......... | 8-cyl. V | $5.51 \times 5.9$ | 406 at 2,000 | Center | 2.52 |  | 0.7; | - 4.785 |  | - | 259 | 5 | 0.0765 |
|  |  |  |  |  | 2.52 | 1.893 | 0.7\%, | 4.765 |  |  |  | 12, | 0.0204 0.0378 |
|  |  |  |  | End | 2.52 | 4.255 | 1.6i? | 10.715 | 22.0 | ${ }^{1,430}$ | 291 | 12, |  |
| $\overline{\text { Cadillac V-8(1938)... }}$ | $8-\mathrm{cyl}, \mathrm{V}$ | $3.5 \times 4.5$ | 135 at 3,400 | No. 1 | 2.5 | 1.0625 | 0.42: | 2.66 | 37.05 |  |  |  |  |
|  |  |  |  | No. 2 | 2.5 | 1.1562 | 0. $16:$ | 2.39 | ${ }^{37.05}$ |  |  |  |  |
|  |  |  |  | No. 3 | 2.5 | 1.969 | 0.7xio | 4.91 | 37.05 |  |  |  |  |
| $\overline{\text { Curtiss D-12........ }}$ | 12-cyl. V | $4.5 \times 6$ | 425 at 2,000 | Center | 3.0 | 1.781 | 0.599, | 5.34 | 26.18 | 964 | 734 | 19,200 | 0.0357 |
|  |  |  |  | Intermediate | 3.0 | 1.531 | 0.il | 4.563 | 26.18 | 1,040 | 561 | 14,680 | 0.0465 |
|  |  |  |  | End | 3.0 | 1.531 | O.i.i | 4.563 | 26.18 | 608 | 178 | 12,500 | 0.0547 |
| $\overline{\text { Liberty } 12 \ldots \ldots \ldots \ldots .}$ | 12-cyl. V | $5 \times 7$ | 420 at 1,700 | Center | 2.625 | 1.625 | 0.6i: ${ }^{\text {a }}$ | 4.27 | 19.45 | 1,580 | 1,165 | 22,650 | 0.0167 |
|  |  |  |  | Intermediate | ${ }_{2}^{2.625}$ | 1.625 | 0.619 | 4.27 | 19.45 | 1,150 |  | 14,000 | 0.0270 |
|  |  |  |  | End | 2.625 | 1.625 | 0.619 | 4.27 | 19.45 | '845 | 623 | 12,100 | 0.0312 |
| Packard 2500....... | 12-cyl. V | $6.375 \times 6.5$ | 800 at 2,000 | Propeller end | 3.5 3.5 3 | ${ }_{1}^{2.25}$ | 0.a 6 | 7.875 | 30.55 | 728 | 555 | 16,950 | 0.0550 |
|  |  |  |  | Center | 3.5 3.5 | $\stackrel{1}{2.5}$ | 0 | 8.75 | 30.55 30.55 | 1,785 | 982 | 30,000 | 0.03 |
|  |  |  |  | Rear end | 3.5 | 1.437 | 0.:1 | ${ }_{5} 5.031$ | 30.55 | 1,139 | 868 | 26.517 | 0.0336 |
| Curtiss $\mathrm{V}-1570 \ldots \ldots$. | 12-cyl. V | $5.125 \times 6.25$ | $\ldots \ldots .$. | Center | 3.5 | 1.594 | 0.15\% | 5.39 | -36.7 |  |  |  |  |
|  |  |  |  | Intermediate | 3.5 | 1.344 | 0.381 | 4.52 | 36.7 |  |  | 34.700 | 0.0387 |
|  |  |  |  | Ead | 13.5 | 1.344 | 0.isi | 4.52 | 36.7 | 1, 112 |  |  |  |

Table A1-7.-Relative Crankpin-bearing Loads with Various
Arrangements of 6- by $6.875-\mathrm{In}$. Cylinders (From S.A.E. Jour., Vol. 29, No. 5, November, 1931)

| Cylinders <br> per crankpin | Arrangement | Dis-placement, cu.in. | Weight per crankpin |  | Bearing <br> load, lb. |  | Force per cu . in. of piston displacement, Ib. |  | Required bearing area based on mean load, \% |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Rotating, lb. | Recip-rocating, lb. | Max. | Mean |  |  |  |
|  |  |  |  |  |  |  | Max. | Mean |  |
| 1 |  | 195 | 6.00 | 6.82 | 7,880 | 3,740 | 40.4 | 19.2 | 100 |
| 2 | 60- or $45-\mathrm{deg}$. V | 390 | 8.00 | 13.64 | 8,140 | 5,730 | 20.9 | 14.7 | 153 |
| 3 | $40-\mathrm{deg}$. W | 585 | 10.00 | 20.46 | 10,100 | 6,790 | 17.3 | 11.6 | 181 |
| 3 | $60-\mathrm{deg}$. W | - 585 | 10.00 | 20.46 | 13,050 | 8,020 | 22.3 | 13.7 | 214 |
| 3 | $80-\mathrm{deg}$. W | 585 | 10.00 | 20.46 | 9,960 | 7,630 | 17.0 | 13.0 | 204 |
| 3 | Radial | 585 | 10.00 | 20.46 | 10,230 | 6,860 | 17.5 | 11.7 | 183 |
| 5 | Radial | 975 | 14.00 | 34.10 | 11, 880 | 8,920 | 12.2 | 9.2 | 238 |
| 7 | Radial | 1365 | 18.00 | 47.74 | 13,740 | 11,520 | 10.1 | 8.5 | 308 |
| 9 | Radial | 1755 | 22.00 | 61.38 | 16,320 | 14,080 | 9.3 | 8.0 | 376 |

Table A1-8.-Field of Usefulness for Various Bearing Metals (From S.A.E. Jour., Vol. 45, No. 6, December, 1939)

| Description of bearing metal | Max. permissible unit pressure, lb. per sq. in. | Min. permissible $Z n / P_{\max }$ | $\begin{gathered} \text { Maximum } \\ P_{\max } V \end{gathered}$ | Oil reservoir temperature, deg. F. | Minimum crankshaft hardness | Affected by corrosion |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tin-base babbitt:  <br> Copper............ $3.50 \%$ <br> Antimony........ $7.50 \%$ <br> Tin.............. 89.00 <br> Lead (max.)...... $0.25 \%$ | 1,000 | 20 <br> Stand | $35,000$ <br> quality | $235$ <br> earings | Not important | No |
| Tin-base babbitt: <br> Same composition as above | 1,500 | $15$ <br> Alpha pr | $42,500 .$ <br> cess quality | 235 bearings | Not important | No |
| High-lead babbitt:  <br> Tin.................. $5-7 \%$ <br> Antimony........ $9-11 \%$ <br> Lead............. $82-86 \%$ <br> Copper (max.).... $0.25 \%$ | 1,800 | 10 | 40,000 | 225 | Not important | No |
| Cadmium-silver:  <br> Silver.................75\% $0.50 \%$ <br> Copper........... $0.50 \%$ <br> Cadmium........ $98.75 \%$ | Over 1,800 and up to 3,850 | 3.75 | $\begin{gathered} 90,000 \text { and } \\ \text { upwards } \end{gathered}$ | 260 | 250 Brinell | Not likely if temperature is maintained as specified and proper |
| Copper-lead:  <br> Copper........... $60 \%$ <br> Lead............ $40 \%$ | Over 1.800 | 3.75 | 90,000 and upwards | 260 | 300 Brinell |  |

Table A1-9.-Principal Dimensions (in Inches) of Six Different Aircraft-engine Crankshafts
(From S.A.E. Jour., Vol. 28, No. 4, April, 1931)


| $\begin{aligned} & \text { Dimen- } \\ & \text { sion } \end{aligned}$ | Crankshaft number |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 |
| A | 3.3125 | 4.125 | 3.5 | 3.75 | 4.125 | 4.25 |
| B | 3.3125 | 4.125 | 3.5 | 3.75 | 4.125 | 4.25 |
| C | 6 | 3 | 5.5 | 5.75 | 7.75 | 5.75 |
| D | 2.5625 | 3 | 2.875 | 2.875 | 3.25 | 3.875 |
| E | 1.375 | 1.9375 | 1.625 | 1.625 | 1.75 | 3.125 |
| $F$ | 2 | 2.25 | 2.5 | 2.5 | 2.75 | 3.25 |
| G | 1 | 1.4375 | 0.75 | 0.75 | 1 | 2.5625 |
| H | 2.75 | 3.25 | 3.125 | 3.125 | 3.125 | 3.5625 |
| J | 3.75 | 3.75 | 3.375 | 3.75 | 4.25 | 3.9375 |
| K | 1.3125 | 1.4375 | 1.1875 | 1.3125 | 1.375 | 1.6875 |
| L | 1.3125 | 1.125 | 1.25 | 1.375 | 1.25 | 1.3125 |
| $\mathrm{M}\left\{\begin{array}{l}1 \\ 2\end{array}\right.$ | 2.625 | 3.5 , $\}$ | 3.75 |  |  |  |
| ${ }^{\text {m }}$ 2 | 2.375 | 3.1255 | 3.75 | 3.75 | 3.875 | $\{4.125$ |
| T | 2.75 | 2.75 | 2.4375 | 2.875 | 3.1875 | 3.4375 |

1. Front.
2. Rear.

Table A1-10.-Radial-engine Bearing Reactions for Maximum Radial Gas Load on Crankpin (1) at Rated Power and
(2) at Rated Power Combined with Inertia Load at Rated Speed (Average Values Only)
(From S.A.E. Jour., Vol. 28, No. 4, April, 1931)


| Crankshaft number | Crank- <br> pin <br> load, <br> lb. | $R_{1}$ |  | $R_{2}$ |  | $R_{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | lb . | \% | lb . | \% | lb . | \% |
| 1 | 8,440 | 3,380 | 40 | 6,000 | 71 | 930 | 11 |
| 2 | 10,400 | 3,740 | 36 | 9,100 | 87.5 | 2,440 | 23.5 |
| 3 | 11,200 | 4,260 | 38 | 8,680 | 77.5 | 1,740 | 15.5 |
| 4 | 13,800 | 5,240 | 38 | 10,800 | 78 | 2,200 | 16 |
| 5 | 15,650 | 6,260 | 40 | 11,100 | 71 | 1,720 | 11 |
| 6 | 15,000 | 5,920 | 39.5 | 11,600 | 77 | 2,480 | 16.5 |
| Average (1).... Variation, \% of mean value Average (2).... |  |  | 38.6 |  | 77 |  | 15.6 |
|  |  |  | $\left\{\begin{array}{r}+3.6 \\ -6.7\end{array}\right.$ |  | $\left\{\begin{array}{r}+13.6 \\ -7.8\end{array}\right.$ |  | $\left\{\begin{array}{l}+51 \\ -29\end{array}\right.$ |
|  |  |  | 40.6 |  | 72.6 |  | 12.9 |

Table A1-11.-Characteristics and Dimensions of Curtiss V-1570 Conqueror Engine
(From S.A.E. Jour., Vol. 29, No. 4, October, 1931)Number of cylinders12
Arrangement of cylinders Two banks at $60-\mathrm{deg}$. V
Method of numbering cylinders 6, 5, 4, 3, 2, 1-Right
Propeller end 6, 5, 4, 3, 2, 1—Left
Firing order, crankshaft rotation clockwise facing rear ofengine.................. 1L, 6R, 5L, 2R, 3L, 4R, 6L, 1R, 2L, 5R, 4L, 3R
Bore, in ..... 5.125
Stroke of master-rod cylinder ( $2 R$ ), in ..... 6.250
Stroke of articulated-rod cylinder, in ..... 6.430
Piston area, sq. in ..... 20.63
Total piston displacement, cu. in ..... 1,569.5
Brake horsepower ..... 630
Speed, r.p.m ..... 2,400
Compression-ratio, average ..... 5.80: 1
Mechanical efficiency, \% ..... 89.4
Brake mean effective pressure, lb. per sq. in ..... 132.4
Indicated mean effective pressure, lb. per sq. in ..... 148.1
Master connecting-rod length, center to center ( $L$ ), in: ..... 10.0
Master connecting rod to crank ratio ( $L / R$ ), in ..... 3.20
Articulated-rod length, in ..... 7.594
Link-pin radius ( $R_{1}$ ), in ..... 2.406
Angle between link-pin radius and master-rod center line ( $\alpha_{1}$ ), deg. min ..... 66-30Master rods are assembled in the left cylinder bankValve timing:
Inlet valve opens, deg. before top dead center .....  5
Inlet valve closes, deg. after bottom dead center. ..... 55
Exhaust valve opens, deg. before bottom dead center ..... 60
Exhaust valve closes, deg. before top dead center ..... 0
Valve-tappet clearance, intake and exhaust, in $0.014-0.016$
Magneto timing:
Left magneto advance, deg ..... 33
Right magneto advance, deg ..... 38
Reciprocating and rotating weights:
Reciprocating weight per cylinder of master rod, lb ..... 4.11
Piston, complete with rings and pin, lb ..... 2.97
Upper end of master connecting rod, lb ..... 1.14
Reciprocating weight per cylinder of articulated rod, lb ..... 3.90
Upper end of articulated connecting rod, lb ..... 0.93
Rotating weight of crankpin, lb ..... 5.36
Lower end of master connecting rod, lb ..... 4.53
Lower end of articulated connecting rod, lb ..... 0.83
Crankpin bearing:
Diameter, in ..... 2.500
Length, total, in ..... 1.500
Table A1-11.-Characteristics and Dimensions of Curtiss V-1570 Conqueror Engine.-(Continued)
Length, effective, in ..... 1.391
Effective projected bearing area, minus oil groove, sq. in ..... 3.28
Crankshaft end and intermediate bearings:
Diameter, in ..... 3.500
Length, total, in ..... 1.500
Length, effective, in ..... 1.344
Effective projected bearing area, sq. in ..... 4.52
Crankshaft center bearing:
Diameter, in ..... 3.500
Length, total, in ..... 1.750
Length, effective, in ..... 1.594
Effective projected bearing area, sq. in ..... 5.39
Crankshaft:
Diameter of journal, in ..... 3.500
Bore through journal, in ..... 2.750
Diameter of crankpin, in ..... 2.500
Length of crankpin, in ..... 1.920
Bore through crankpin, in ..... 1.250
Crankpin fillets, in ..... 0.250
Journal fillets, in ..... 0.187
Width of crank cheek at top of journal, in ..... 3.790
Thickness of crank cheek, in ..... 0.987
Distance between end and intermediate crankpin centers, in. ..... 5.750
Distance between center crankpin centers, in ..... 6.000
Table A1-12.-Engine Characteristics and Dimensions of Wright R-1750 Cyclone Engine(From S.A.E. Jour., Vol. 29, No. 4, October, 1931)
Number of cylinders ..... 9
Arrangement of cylinders ..... Radial
Numbering of cylinders 1-9 consecutively, clockwise facing rearof engine, No. 1 vertical and on top
Firing order $1,3,5,7,9,2,4,6,8$
Crankshaft rotation Clockwise facing rear of engine
Bore, in ..... 6.000
Stroke of master-rod cylinder ( $2 R$ ), in ..... 6.875
Piston area ( $A p$ ), sq. in ..... 28.27
Total piston displacement, cu. in ..... 1,750
Brake horsepower ..... 525
Speed, r.p.m ..... 1,900
Compression ratio ..... 5.0:1
Mechanical efficiency, assumed, \% ..... 90
Brake mean effective pressure, lb. per sq. in ..... 125.0
Indicated mean effective pressure, lb. per sq. in ..... 139.0
Master connecting-rod length, center to center ( $L$ ), in ..... 13.750
Master connecting-rod to crank ratio ( $L / R$ ) ..... 4.000
Articulated or link-rod length, in ..... 11.046
Master rod is assembled in cylinder 7
Table A1-12.-Engine Characteristlics and Dimensions of Wright R-1750 Cxclone Engine.-(Continued)
Valve timing:
Inlet valve opens, deg. before top dead center ..... 25
Inlet valve closes, deg. after bottom dead center ..... 60
Exhaust valve opens, deg. before bottom dead center ..... 80
Exhaust valve closes, deg. after top dead center ..... 25
Valve tappet clearance, in ..... 0.050
Spark advance, deg. before top dead center ..... 30
Supercharger:
Type Geared centrifugal
Impeller speed 8 times crankshaft
Reciprocating and rotating weights:
Reciprocating weight per cylinder of master rod, lb ..... 7.45
Piston, complete with rings and pin, lb ..... 5.34
Upper end of master connecting rod, lb ..... 2.11
Reciprocating weight per cylinder of link rod, lb ..... 6.74
Upper end of link connecting rod, 1 lb ..... 1.40
Rotating weight at crankpin ( $W_{c}$ ), lb ..... 25.22
Lower end of master connecting rod, lb ..... 15.62
Lower end of link connecting rod, lb ..... 1.20
Crankpin-bearing dimensions:
Diameter, in ..... 3.250
Length, total, in ..... 3.906
Length, effective, in ..... 3.562
Effective projected bearing area, sq. in ..... 11.58
Front main bearing:
Construction Steel sheet lined with high-load bronze
Diameter, in ..... 4.375
Effective length, in ..... 1.687
Effective projected bearing area, sq. in ..... 7.38
Rear main bearing:
Type Commercial Hoffman R-190-LL or SK KF light series roller bearing No. 8216-C
Inner diameter, in ..... 3.5433
Mm ..... 90
Outside diameter, in ..... 62,992
Mm ..... 160
Width, in ..... 1. 181
Mm ..... 30
Front thrust bearing:
Type..... Commercial Standard S.A.E. light series ball bearing No ..... 218
Inner diameter, in ..... 3.3433
Mm ..... 90
Oitside diameter, in ..... 6.2992
Mm ..... 160
Width, in ..... 1.181
Mm ..... 30

Table A1-13.-Rilation of Crutsing to Take-off Horsepower and R.P.M. for Eleven American Aircraft Engines

| Cruising <br> hp. | Take- <br> off <br> hp. | Cruis- <br> ing <br> r.p.m. | Take- <br> off <br> r.p.m. | Cruising hp. <br> Take-off hp. | Cruising r.p.m. |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 40 | 2,300 | 2,575 | 75 | Take-off r.p.m. |
|  | 225 | 2,000 | 2,175 | 78 | 89.5 |
| 175 | 250 | 2,000 | 2,200 | 76 | 92 |
| 160 | 200 | 1,750 | 2,000 | 80 | 91 |
| 200 | 252 | 1,900 | 2,050 | 79.5 | 87.5 |
| 75 | 100 | 1,650 | 1,810 | 75 | 92.8 |
| 94 | 125 | 1,725 | 1,925 | 75 | 91 |
| 120 | 160 | 1,775 | 1,975 | 75 | 89.5 |
| 120 | 160 | 1,650 | 1,850 | 75 | 90 |
| 160 | 210 | 1,700 | 1,900 | 76 | 89 |
| 110 | 160 | 2,050 | 2,260 | 69 | 89.5 |

Table A1-14.-Aircraft-engine Piston Data
(See page 396 for values)


A-Diameter
${ }^{B}$ - Length (not including crown).
$C$ - Crown or cup?
$D$-Thickness of bottom flange.
$E$-Distance from bottom of skirt to bottorn of lowest groove.
$F$-Width of top land.
$G_{A}$ (etc.)-Width and depth of lower ring grooves ( $G_{1}$-upper)
$G_{L}$-Groove containing holes for lubricant.
$H$-Diameter of wrist-pin hole.
$I$-Length of wrist-pin hole.
$J$-Height of bottom flange.
$\underset{L}{K}$ —Thickness of boss, botton
$M$-Thickness of skirt above bottom flange.
$N$-Thickness of wall at upper ring
grooves.
$o$ - Thickness of head (to bottom of ribs on ribbed pistons).
$P$-Spacing of ribs.
$Q$-Depth of ribs.
$R$-Width of lands between grooves.
$S$-Wall thickness under boss.
$T$-Beveled 60 deg. to crown (about $1 / 4 \mathrm{in}$. wide).
$U$-Type of lubrication holes.
$V$-Full floating piston pin.
$W$ 二Web support for pin bosses.
$X$-Number of rings per groove.
Table A1-14.-Aircraft-engine Piston Data.-(Conlinued)

| Item | Piston numbers* |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 |
| Material. | $\mathrm{Al}$ | S.A.E. 321 | Al | Y-alloy | Lynite | Lynite | S.A.E. 321 | A] |
| Weight............. | 3 lb .5 .5 oz . | $4 \mathrm{lb} .12 .4 \mathrm{oz}$ | Alloy 4 lb .14 .4 oz . | 4 lb .2 .4 oz . | 3 lb .8 .75 oz . | Lymite | 1 lb .13 .5 oz. | 2.25 lb . |
| Volume, cu. in........ | 33.6 | - 49.35 | 48.28 | 41.35 | 33.68 | 0.105.... | 19.04 |  |
| Density, lb. per cu, in. $A$................. | 0.102 5.59 | 0.97 6.1 | ${ }_{6}^{0.1} 1$ | 0.1 5.95 | 0.105 4.97 | 0.105 4.98 | 0.097 4.5 |  |
| $B$ | 3.92 | 4.0 | 3.92 | 5.95 3.95 | 5.1 | 4.98 4.3 | 4.5 3.2 | 4.6 3.47 |
| C. | -0.8 | 0 | +0.64 | 0 | +0.4 | 0 | 0 | 3.47 |
| D | 0.1 | 0.4 | 0.35 | 0.45 | 0.15 | 0.4 | 0.4 | 0.125 |
| E | 0.88 | 0.19 | 0.22 | 0.1 |  | 0.3 | 0.15 |  |
|  | $\stackrel{0.35}{0.3}$ | 0.47 | 0.22 | 0.25 | 0.4 | 0.3 | 0.2 | 0.35 |
| $G_{1}$ | $0.13 \times 0.22$ | $0.13 \times 0.22$ | $0.2 \times 0.2$ | $0.2 \times 0.2$ | $0.25 \times 0.19$ | $0.25 \times 0.19$ | $0.125 \times 0.16$ | $0.15 \times 0.20$ |
| G | $0.13 \times 0.22$ | $0.13 \times 0.22$ | $0.2 \times 0.2$ | $0.2 \times 0.2$ | $0.25 \times 0.19$ | $0.25 \times 0.19$ | $0.125 \times 0.16$ | $0.15 \times 0.20$ |
| $\mathrm{C}_{3}$ | $0.2 \times 0.22$ $0.2 \times 0.22$ | $0.13 \times 0.22$ |  | $0.2 \times 0.2$ | $0.25 \times 0.19$ | $0.25 \times 0.19$ | $0.125 \times 0.16$ | $0.15 \times 0.20$ |
| $C_{L}$ | $G_{G_{4}, G_{A}}$ | $\cdots \dddot{G}_{3}, \square_{A} \cdots$ | $G_{2}, G_{A}$ | $\cdots{ }_{G_{3}}$ | $G_{3}$ | None | $G_{A}$ | $0.15 \times{ }_{G_{4}}^{\times 0.20}$ |
| $G_{A}$ | $0.2 \times 0.22$ | $0.13 \times 0.22$ | $0.125 \times 0.2$ | $0.2 \times 0.2$ | C.... | $0.25 \times 0.2$ | $0.125 \times 0.16$ |  |
| H | 1.25 | 1.5 | 1.5 | 1.5 | 1.25 | 1.25 | $1.2 \times 0.16$ | 1.10 |
| $\underline{I}$ | 1.5 | 1.7 | 1.9 | 1.85 | 1.05 | 1.13 | 1.0 | 1.40 |
|  |  | 0.5 | 0.35 | 0.4 | 0. | 0.65 | 0.35 | 0.18 . |
|  | 0.35 | 0.4 | 0.25 | 0.20 | 0.25 | 0.25 | 0.15 | 0.1875 |
| A | Ribbed ${ }^{\text {a }}$ | $0.15 \cdots$ | 0.1 | $0.12 \times$ | Tapered | 0.25 | 0.1 .1 | ${ }_{0}^{0.1875}$ |
|  | 0.5 | 0.5 | 0.4 | 0.4 | 0.7-0.4 | 0.8-0.6 | 0.5 | 0.50 |
| ${ }_{P}^{O}(P, H, R) \dagger$ | $0.25(H)$ | $1.0(R)$ | $1.0(H)$ | 1.15 (H) | $0.4(P)$ | 0.45 (1 R) | $0.85(1 R)$ | 0.32 (R) |
| $P$ | $0.8 \times 0.86$ | 0.4 | $0.6 \times 0.7$ | $0.6 \times 0.7$ |  | 0.6(1) | 0.85 | 0.375 |
| $\stackrel{Q}{R}$ | $0.375-0.5$ | 0.4-0.5 | 0.7 | 0.85 |  |  | 0.6 | 0.30 |
| $R_{1}$ <br> $R_{2}$ | 0.1 | 0.15 | 0.17 | 0.125 | 0.125 | 0.125 | 0.08 | 0.125 |
| $R 2$ $R_{2}$ | 0.10 | 0.15 |  | 0.125 | 0.125 | 0.125 | 0.10 | 0.125 |
| $\stackrel{R}{R}$ | 0.10 0.4 | $0.4{ }^{\text {a }}$ | 0.35 | 0.15 | 0.2 | 0.25 | 0. 125 | 0.125 |
| $T$ |  | Yes |  |  | 0.125 Rad |  | 0.125 | 0.125 0.125 |
| U | ${ }^{3}$ | 2,3 | 1.5 |  | ${ }_{3.4}$ | None | 3 | 0.12 |
| V | Yes | Yes | Yes | Yes | No | No | Yes | Yes |
| d | $W_{1}$ | $W_{1}$ | $W_{1}$ | $W_{1}$ |  | $W_{2}$ | $W_{1}$ | $W_{1}$ |
|  | 1 | ${ }_{0}^{1} 0.02$ | $2\left(G_{A} 1\right)$ 0.015 | ${ }_{0}^{2} 03$ | 1 | 1 | 1.0 | 1 |

* 1. Skirt cut away 0.6 in. at bosses. Well ribbed between bosses. 2 and 3 . Valve indentations in crown. 4. Crown domed. 5. Skirt inset at pin
bosses to center of boss. Pins are driven in and retainers fitted. Weights do not.
$\dagger P, H, R$ refers to type of crown (underside), $P$-plain, $H$-honeycombed, $R$-ribbed.

Table A1-15.-Aircraft-engine Piston-pin and Piston-ring Data

| Item | Piston-pin numbers* |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
|  | 2 |  |  | 4 |
| $A$ |  | 5 | 7 |  |
| $C$ | 6.1 | 5.9 |  |  |
| $D$ | 5.5 | 5.5 | 4.25 | 4.1 |
| $E$ | 0.18 | 0.12 |  |  |
| $F$ | 1.5 | 1.5 | 1.25 | 1.2 |
| $G$ | 1.1 | 1.23 | 0.82 | 0.95 |
| $H$ | 1.12 | 1.25 | 0.82 | 1.0 |
| $J$ | 1.1 | 1.1 | $\cdots \cdots$ | 0.7 |
|  | 0.9 | 0.95 |  |  |

* Piston-pin numbers correspond to piston numbers in Table A1-14. All dimensions are in inches.

| Item | Piston-ring numbers* |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 2 | 3 | 3 | 4 | 4 | 5 | 7 | 7 | 9 | 10 |
| A. | 6.25 | 6.25 | 6.3 | 6.15 | 6.15 | 5.12 | 4.62 | 4.7 | 5.18 | 4.125 |
| $B$. | 0.125 | 0.10 | 0.10 | 0.10 | 0.10 | 0.25 | 0.125 | 0.12 | 0.25 | 0.29 |
| $C$. | 0.18 | 0.20 | 0.20 | 0.18 | 0.18 | 0:18 | 0.15 | 0.15 | 0.15 | 0.13 |
| D. | 0.60 | 0.70 | 0.75 | 0.56 | 0.65 | 0.45 | 0.45 | 0.68 | 0.65 | 0.36 |
| Section. | $b$ | $b$ | $e$ | $b$ | e | d | $b$ | $c$ | $a$ | $a$ |
| Function $\dagger$ | $c$ | $c$ | $s$ | $c$ | $s$ | c | $c$ | $s$ | $c$ | c |
| Weight, oz. | 1.7 | 1.4 | 1.4 | 1.3 | 1.2 | 2.6 | 1.0 | 0.8 | 2.4 | 2.0 |

* Piston-ring numbers correspond to piston numbers in Table A1-14.
$\dagger c=$ compression ring. $s=$ scraper or oil ring.
All dimensions are in inches.
Dimensions $A$ and $D$ are for ring free.


Piston or wrist pins


Table A1-16A.-Piston-ring and Groove Widths (From S.A.E. "Handbook")

| Nom. ring width | All ring widths, in. |  |  | Ring-groove widths, in. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | All diam. max. | Under 6 in. diam. | 6-8 in. diam. | Oil-ring grooves |  |  |  | Top compression ring grooves only |  |  |  |
|  |  |  |  | $\begin{gathered} 2-411 / 16 \text { in. } \\ \text { diam. } \end{gathered}$ |  | $\begin{gathered} \text { 43/4-8 in. } \\ \text { diam. } \end{gathered}$ |  | $\begin{gathered} 2-411 / 16 \mathrm{in} . \\ \text { diam. } \end{gathered}$ |  | $43 / 4-8 \mathrm{in} .$ <br> diam. |  |
|  |  | Min. | Min. | Max. | Min. | Max. | Min. | Max. | Min. | Max. | Min. |
| 3/32 | 0.0935 | 0.0930 | 0.0925 | 0.0955 | 0.0945 | 0.0960 | 0.0950 | 0.0960 | 0.0950 | 0.0965 | 0.0955 |
| 1/8 | 0.1240 | 0.1235 | 0.1230 | 0.1260 | 0.1250 | 0.1265 | 0.1255 | 0.1265 | 0.1255 | 0.1270 | 0.1260 |
| 5/32 | 0.1550 | 0.1545 | 0.1540 | 0.1570 | 0.1560 | 0.1575 | 0.1565 | 0.1575 | 0.1565 | 0.1580 | 0.1570 |
| $3 / 16$ | 0.1865 | 0.1855 | 0.1855 | 0.1885 | 0.1875 | 0.1890 | 0.1880 | 0.1890 | 0.1880 | 0.1895 | 0.1885 |
| $1 / 4$ | 0.2490 | 0.2485 | 0.2480 | 0.2510 | 0.2500 | 0.2515 | 0.2505 | 0.2515 | 0.2505 | 0.2520 | 0.2510 |

The piston-ring grooves provide for a minimum side clearance of 0.001 in . for cylinders under $43 / 4 \mathrm{in}$. diameter and 0.0015 in . for cylinders of $43 / 4$ to 8 in . diameter. The greater clearance for the top compression ring is recommended only in order to give improved ring performance.

Table A1-16B.-Ring Widthis for Cylinder Diameters

| Cylinder <br> diameter, in. | Ring width, in. |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Compres- <br> sion rings | Oil rings |  |  |  |  |
|  | $1 / 8$ | $1 / 8$ | $5 / 32$ | $3 / 16$ |  |  |
| $41 / 2-57 / 16$ | $5 / 32$ | $\cdots$ | $5 / 32$ | $3 / 16$ | $1 / 4$ |  |
| $51 / 2-67 / 16$ | $3 / 16$ | $\cdots$ | $\cdots$ | $3 / 16$ | $1 / 4$ |  |
| $61 / 2-8$ |  |  |  |  |  |  |

Note: Oil-ring widths or combinations of widths shall be selected from the widths specified between the diameters listed.

The accompanying specifications for piston rings and grooves have in general been used for some time and have been adopted as a standard primarily for the types of internal-combustion engines commonly used in automobiles, motorboats, etc. For pistons used in aircraft engines and engines not of the conventional automobile type, it may be necessary to deviate from the rings and grooves recommended in order to secure most satisfactory performance, but such modifications should not be made by changing the piston-ring width or radial thickness.

Table A1-16C.-Piston-ring Radial Wall Thickness and Groove Diameters

| Cylinder diameter, in. | Ring radial wall thickness, in max | Ring groove bottom diameter, in., max. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | Cast-iron pistons |  | Aluminum pistons |  |
|  |  | Compression rings | Oil rings | Compression rings | Oil rings |
| $\begin{aligned} & 31 / 2 \\ & 39.6 \\ & 356 \\ & 31516 \\ & 33 / 4 \end{aligned}$ | 0.150 0.150 0.155 0.155 0.160 | 3.166 3.228 3.288 3.280 3.342 3.395 | 3.126 3.188 3.240 3.302 3.355 3.35 | 3.159 3.221 3.273 3.273 3.335 3.387 | 3.119 3.181 3.233 3.295 3.347 3.3 |
| $\begin{aligned} & 31316 \\ & 37 / 8 \\ & 31816 \\ & 416 \\ & 4316 \end{aligned}$ | 0.160 0.165 0.165 0.165 0.165 | 3.457 3. 509 3.571 3.571 3.634 3.696 | 3.417 3.469 3.531 3.594 3.656 | 3.449 3.501 3.563 3.563 3.626 3.688 | $\begin{aligned} & 3.409 \\ & 3.461 \\ & 3.523 \\ & 3.586 \\ & 3.648 \end{aligned}$ |
| $\begin{aligned} & 41 / 8 \\ & 43 / 8 \\ & 438 \\ & 4836 \\ & 438 \end{aligned}$ | 0.165 0.165 0.170 0.170 0.175 | 3.758 3.820 3.873 3.935 3.987 | $\begin{gathered} 3.718 \\ 3.780 \\ 3 \\ 3833 \\ 3.895 \\ 3.947 \end{gathered}$ | $\begin{aligned} & 3.750 \\ & 3.812 \\ & 3 \\ & 3.864 \\ & 3.926 \\ & 3.978 \end{aligned}$ | 3.710 3 3.772 3.824 3.886 3.938 |
| $\begin{aligned} & 4716 \\ & 4 y 5 \\ & 4516 \\ & 458 \\ & 41 / 16 \end{aligned}$ | 0.175 0.180 0.180 0.180 0.180 | 4.049 4.102 4.164 4.226 4.288 | 4.009 4.062 4.124 4.186 4.248 | 4.040 4.093 4.155 4.217 4.279 | 4.000 4.053 4.115 4.177 4.239 |
| $\begin{aligned} & 431 / 1 \\ & 4716 \\ & 418 \\ & \hline 1518 \end{aligned}$ | 0.185 0.185 0.190 0.190 0.195 | 4.341 4.403 4.455 4.517 4.570 | 4.301 4.363 4.415 4.477 4.530 | 4.331 4.393 4.445 4.507 4.560 | 4.291 4.353 4.405 4.467 4.520 |
| $\begin{aligned} & 5316 \\ & 515 \\ & 538 \\ & 51.16 \\ & 55 / 16 \end{aligned}$ | 0.195 0.195 0.195 0.200 0.200 | 4.632 4.694 4.756 4.809 4.871 | 4.592 4.654 4.716 4.769 4.831 | 4.622 4.684 4.746 4.798 4.860 | 4.582 4.644 4.706 4.758 4.820 |
| $\begin{aligned} & 538 \\ & 5716 \\ & 53 / 6 \\ & 5916 \\ & 558 \end{aligned}$ | 0.205 0.205 0.210 0.210 0.215 | 4.923 4.985 5.038 5.100 5.152 | 4.883 4.945 4.998 5.960 5.060 5.112 | 4.912 4.974 5.027 5.089 5.089 5.141 | 4.872 4.934 4.987 4.989 5.049 5.101 |
| $\begin{aligned} & 511 / 16 \\ & 53, \\ & 513 \\ & 57 / 26 \\ & 513 / 16 \end{aligned}$ | 0.215 0.220 0.220 0.225 0.225 | 5.214 5. 267 5.329 5.381 5.483 |  | 5.203 5.203 5.355 5.317 5.369 5.431 | 5.163 5.215 5.277 5.329 5.391 |
| $\begin{aligned} & 6 \\ & 611 / 6 \\ & 613 \\ & 63 / 3 \\ & 61 / 4 \end{aligned}$ | 0.230 0.230 0.235 0.235 0.240 | 5.496 5.558 5.610 5.672 5.725 | 5.456 5.518 5.570 5.632 5.685 | 5.484 .5 .546 .5 .598 5.660 5.712 | 5.444 5.506 5.558 5.620 5.672 |
| $\begin{aligned} & 65 / 6 \\ & 635 \\ & 65 / 16 \end{aligned}$ | $\begin{aligned} & 0.240 \\ & 0.245 \\ & 0.245 \end{aligned}$ | $\begin{aligned} & 5.787 \\ & 5.839 \\ & 5.901 \end{aligned}$ | $\begin{aligned} & 5.747 \\ & 5.799 \\ & 5.861 \end{aligned}$ | 5.774 5.826 5.888 | $\begin{aligned} & 5.734 \\ & 5.786 \\ & 5.848 \end{aligned}$ |

Table A1-16D.-Ring Joints and Drain Holes
(The following data were adopted as recommended practice only.)
Ring-joint Clearance.-Rings having maximum radial wall thickness as recommended should have a free joint opening of approximately $D / 6.75$ to permit assembling them without overstressing individual castings having a mean tensile strength of about $28,000 \mathrm{lb}$. per sq. in., as piston-ring joint clearance must be determined from the minimum cylinder diameter. It is recommended that joint clearance for rings be as follows:

## Ring-joint Clearances

## Cylinder Diameter, In.

$2-415 / 16$ 5-8. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 0.010-0.020

Number of Oil-ring Groove Drain Holes

## Cylinder Diameter, In.


29/16-215/1610
$3-37 / 16$ ..... 12
$31 / 2 \quad-3^{15} / 16$ ..... 14
$4 \quad-41 / 2$ ..... 12
49/16-57/6 ..... 14
$51 / 2 \quad-5^{15} / 16$ ..... 16
$6-65 / 8$ ..... 14
$6^{11 / 16}-7^{15} / 16$ ..... 16
8. ..... 17Size of Oil-ring Groove Drain Hole
Drill Hole
Nominal Ring Width, In. Diameter', In.
1/8. ..... $3 / 32$
5/32 ..... 1/8
3/16 ..... $5 / 32$
$1 / 4$. ..... $7 / 32$

Table A1-17.-S.A.E. Standard Dimensions for Connecting-rod

## Bolts

(From S.A.E. "Hàndbook")

|  |  |  |  |  |  |  | $y_{0}$ | = Drill fors cotter | size <br> A.E. <br> pin |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Diameter | A | $B$ | $C$ | D | Threads per inch NF-3 | $E^{*}$ | $F$ | $\begin{array}{c\|c} G \\ \text { No. } \end{array}$ | $H$ length minus | $R$ |
| 5/16 |  | $3 / 16$ | $3 / 16$ | $\left\|\begin{array}{l} 0.3125 \\ 0.3105 \end{array}\right\|$ | 24 | $1 / 2$ | 3/16 | 48 | 3/32 | 0.01-1/32 |
| 3/8 |  | 5/8 | 7/32 | 0.3750 0.3730 | 24 | 5/8 | 7/32 | 36 | 964 |  |
| 716 |  | 11/16 | 1/4 | 0.4375 <br> 0.4355 | 20 | 11/16 | 1/4 | 36 | 9/64 |  |
| 1/2 |  | $3 / 4$. | 9/32 | $\begin{aligned} & 0.5000 \\ & 0.4975 \end{aligned}$ | 20 | $3 / 4$ | 9/32 | 36 | 9/64 | 1/64-3/64 |
| 9/16 |  | 7/8 | $5 / 16$ | $\left\|\begin{array}{l} 0.5625 \\ 0.5600 \end{array}\right\|$ | 18 | 7/8 | 5/16 | 28 | 316 |  |
| 5/8 |  | 1 | 38 | $\left.\begin{aligned} & 0.6250 \\ & 0.6220 \end{aligned} \right\rvert\,$ | 18 | 1 | 3/8 | 28 | 316 |  |
| $3 / 4$ |  | 11/8 | 7/16 | $\left\|\begin{array}{l} 0.7500 \\ 0.7470 \end{array}\right\|$ | 16 | 11/8 | 7/16 | 28 | 316 | 1/32-1/16 |
| 7/8 |  | 13/8. | 1/2 | $\begin{aligned} & 0.8750 \\ & 0.8715 \end{aligned}$ | 14 | 11/4 | 12 | 28 | $3 / 16$ |  |
| 1 |  | 11/2 | 916 | $\begin{aligned} & 1.0000 \\ & 0.9965 \end{aligned}$ | 14 | 11/2 | 5/8 | 28 | 3116 |  |

* Minimum length of usable threads.

Recommended practice for material is S.A.E. steel 2330 or 3130.
Head-treatment should give a Brinell test of 223 to 285.
From the report of the Engine Division, adopted by the Society, August, 1920.
Revised by Gasoline Engine Division, January, 1941.


| Item | Link-rod number |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | 1 | 2 | 3 | 4 |
| A. | 11.05 | 10.20 | 9.00 |  |
| $B$. | 1.35 | 1.55 | 0.85 |  |
| $C$. | 1.05 | 0.875 | 1.00 |  |
| D. | 1.98 | 2.00 | 1.55 |  |
| E. | 1.48 | 1.35 | 1.55 |  |
| $F$. | 1.90 | 1.70 | 1.50 |  |
| $G$. | 1.50 | 1.45 |  |  |
| H | 0.14 | 0.12 | 0.10 |  |
| $J$. | 0.125 | 0.125 | 0.125 |  |
| $K$ | 9.30 | 7.55 |  |  |
| $L$. | 1.65 | 1.53 | 1.25 |  |
| $M$. | 1.50 | 1.37 | 1.10 |  |
| $N$. | 1.23 | 1.23 | 1.15 |  |
| 0 . | 1.07 | 1.07 | 0.90 |  |
| $P$. | 0.531 | 0.675 | 0.32 |  |
| $Q$ | 0.531 | 0.675 | 0.32 |  |
| $R$. | Fillet | 1.25 | 1.00 |  |
| $S$. | 0.625 | 1.50 | 1.00 |  |
| $T$. | 0.1875 | 0.125 | 0.25 |  |
| $U$. | 0.25 | 0.125 | 0.25 |  |
| $V$. | 0.125 | 0.125 | 0.50 |  |
| Weight, including bushing, lb | 2.75 | 2.1875 |  |  |
| Weight piston-pin end, lb . | 1.438 | 1.1875 |  |  |
| Weight link-pin end, lb . | 1.312 | 1.00 |  |  |
| Number. oil holes. | 1 | 2 |  |  |

All dimensions in inches.

Table A1-19.-Propeller Hubs and Shaft Ends, Aircraft, Spline Type
S.A.E. Recommended Practice
(From S.A.E. "Handbook")


Shaft Ends
Propeller Shaft Ends


Diameters $A, K$, and $X$ shall be concentric with each other within 0.0003 in. reading before splining operation.

American Standard 12 pitch threads.

Table A1-20.-Shaft End, Taper Type
(From S.A.E. "Handbook")


Taper Shaft End

| S.A.E. shaft No. | Taper |  |  | Key |  |  |  | Locking holes |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $L$ | D | $d$ | K | $W$ +0.0000 -0.0005 | $T$ +0.000 -0.007 | $S$ +0.010 -0.000 | $G$ | H | $\begin{gathered} \text { Num- } \\ \text { ber } \end{gathered}$ |
| 00 | 3 | 1.250 | 0.950 | 15/8 | 0.2495 | 0.250 | 0.154 | 3/16 | 5/32 | 1 |
| 0 | 35/8 | 1.875 | 1.512 | 21/4 | 0.3750 | 0.278 | 0.154 |  | $7 / 32$ | 4 |
| 1 | 55/32 | 2 :050 | 1.535 | 3 | 0.3750 | 0.278 | 0.154 | 15/32 | 13/64 | 5 |
| 2 | 7 | 2.362 | 1.662 | 5716 | 0.4730 | 0.237 | 0.143 |  |  |  |

The taper (included angle) should vary from absolute uniformity by being 0.000 to 0.001 in . larger at large end.

Taper Shaft End Threads

| S.A.E. <br> shaft <br> No. | Internal thread (optional) |  |  | External thread |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $B$ | $I$ | Pitch diam., min. | $A^{*}$ | $E$ | Pitch diam., min. |
| 00 | None | None | None | 1 | $3 / 4^{\prime \prime}-16$ | 0.7094 |
| 0 | 5/8 | $7 / 8^{\prime \prime}-18$ | 0.8390 | 13/16 | 13/8' ${ }^{\prime \prime}$-18 | 1.3390 |
| 1 | 7/8 | 15/16 ${ }^{\prime \prime}$-24 | 0.9104 | 1116 | 11/2' ${ }^{\prime \prime}$-18 | 1.4640 |
| 2 | 1116 | $1^{\prime \prime} \quad-14$ | 0.9536 | 11/4 | 1916 ${ }^{\prime \prime}$-12 | 1.5084 |

Thread Form, American (National) Standard.

* Number 00 shaft end is designed for use of standard S.A.E. 3/4-in. castle nut. All other sizes require special nuts.


# Table A1-21.-Splines for Soft Broached Holes in <br> Fittings <br> S.A.E. Standard <br> (From S.A.E. "Handbook") 

The accompanying splines have become established as basic standard for a great many applications in the automotive, machine-tool, and other industries, since they were adopted originally by the Society in 1914.

The dimensions, given in inches, apply only to soft broached holes. The shaft dimensions depend upon the shape and material of the parts, their heat-treatment, methods of machining, etc., to give the required fit. The method and amount of "breaking" sharp corners and edges also depend upon the conditions and requirements of each application.

The tolerances allowed are for good construction and may be readily maintained by usual broaching methods. The tolerances selected for the large and small diameters will depend upon whether the fit between the mating parts, as finally made, is on the large or the small diameter. The other diameter, being designed for clearance, may have a wider manufacturing tolerance. If the final fit between the parts is only on the sides of the spline, wider tolerances may be permitted on both the large and small diameters.

The formula for theoretical torque capacity (pressure on sides of spline) in inch-pounds per inch of bearing length and at $1,000 \mathrm{lb}$. pressure per square inch, is given in footnotes following the table for each type of spline.


Formulas for $W, h$, and $d$, in terms of Large Diameter, $D$

| No. of splines | $\dot{W}$, for all fits | $\begin{gathered} A \\ \text { permanent fit } \end{gathered}$ |  | $\begin{gathered} B \\ \text { to slide not } \\ \text { under load } \end{gathered}$ |  | $\begin{gathered} C \\ \text { to slide } \\ \text { under load } \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $h$ | $d$ | $h$ | $d$ | $h$ | $d$ |
| 4 | $0.241 D^{*}$ | 0.075 D | 0.850 D | $0.125 D$ | 0.730 D |  |  |
| 6 | 0.250 D | 0.050 D | 0.900 D | $0.075 D$ | 0.850 D | 0.100 D | 0.800 D |
| 10 | 0.156 D | 0.045 D | 0.910 D | 0.070 D | 0.860 D | $0.095 D$ | 0.810 D |
| 16 | 0.098 D | 0.045 D | 0.910 D | 0.070 D | 0.860 D | 0.095 D | 0.810 D |

[^28]
## Table A1-22.-Ball-bearing Selection ${ }^{1,2}$

All standard ball bearings are made to internationally agreed upon dimensions for bore, outer diameter, and width and in three series, i.e., light, medium, and heavy. The American edition of these standards is published in the S.A.E. "Handbook." Detailed dimensions may vary with different manufacturers, but over-all S.A.E. standard dimensions are adhered to. Hence, the following data may be used to select the size of bearing needed. Final approval of the selection should be obtained from the manufacturer of the bearing.

In the following subdivisions of this table, the first digit in the bearing number refers to the type of New Departure bearings, the second identifies the series, and the third and fourth, taken together, are the bearing bore number, which is such that, multiplied by 5 , it gives the bore diameter in millimeters, except for the small bores $0,1,2$, and 3. In the S.A.E. "Handbook," the serial and bore number is used as the bearing identifying number for single-row radial bearings. For example, in bearing 1309, the number 1 indicates that the bearing is a New Departure single-row radial fillingnotch type; 3 indicates that the bearing is of medium series; 09 indicates that the bore number is 9 , and as $9 \times 5=45$, it also indicates that the bore diameter is 45 mm .; 309 is the S.A.E. number for this bearing.

The following methods of selection are adapted from recommended practice in the New Departure "Handbook," 12th edition. It is assumed that the loads and speeds are known.

Let $L=$ calculated radial load on bearing, lb .
$T=$ calculated thrust load on bearing, lb.
$\dot{n}=$ r.p.m. of shaft through bearing ( $=$ r.p.m. of inner ring of bearing).
$F=$ radial equivalent conversion factor (Table A1-22A).
$Z=$ life modifier (Table A1-22B).
$M=$ the speed correction for rotating outer ring ( $M=1.46$ for the light, 1.61 for the medium, and 1.74 for the heavy series bearings in this table).
$K=$ shock-load correction factor (Table A1-22C).
$C=$ radial or equivalent radial capacity, lb .
For bearings under radial load,

$$
C=L \times Z \times K
$$

For bearings under thrust and radial load,

$$
C=L \times F \times Z \times K
$$

For bearings under pure thrust,

$$
C=T \times F \times Z \times K
$$

For a rotating inner ring (the usual case), locate the value of $C$ found by the preceding methods in the proper speed ( $n$ ) column of Table A1-22E or

[^29]A1-21G as applies (for filling-notch bearings); or Table A1-22I or. A1-22K as applied (for nonfilling-notch bearings). Then read across to the lefthand column of the table for the corresponding New Departure (or S.A.E.) bearing number. Enter this bearing number in Table A1-22D, A1-22F, $\mathrm{A} 1-22 \mathrm{H}$, or A1-22J as applies, and read the over-all bearing dimensions as indicated. An alternate last step is to enter the last three digits (S.A.E. bearing number) in the S.A.E. "Handbook" bearing tables and read the bearing dimensions therein.

If the outer ring of the bearing is rotating, multiply the speed $n$ by the speed correction factor $M$ and use the product to locate $C$ in the load tables.

Table A1-22A.-Combined Load Factors $F$, for Conversion to Radial Equivalent
(From New Departure "Handbook")

| $T / L$ | Single-row fillingnotch N.D. type 1000 | Single-row nonfillingnotch N.D. type 3000 |
| :---: | :---: | :---: |
| 0.05 | 0.99 | 0.99 |
| 0.10 | 1.00 | 0.99 |
| 0.15 | 1.02 | 0.99 |
| 0.20 | 1.04 | 1.00 |
| 0.25 | 1.06 | 1.00 |
| 0.30 | 1.10 | 1.01 |
| 0.35 | 1.14 | 1.02 |
| 0.40 | 1.19 | 1.04 |
| 0.45 | 1.24 | 1.06 |
| 0.50 | 1.30 | 1.09 |
| 0.60 | $\ldots$ | 1.14 |
| 0.70 | .... | 1.21 |
| 0.80 | ... | 1.28 |
| 0.90 | . . . | 1.35 |
| 1.00 | .... | 1.44 |
| 1.25 | - . . . | 1.66 |
| 1.50 | . . . | 1.90 |
| 1.75 | . . . | 2.17 |
| 2.00 | .... | 2.45 |
| 3.00 | . . . | 3.62 |
| 4.00 | .... | 4.65 |
| 5.00 | . . $\cdot$ | 5.63 |
| 7.50 |  | 8.07 |
| 10.00 |  | 10.57 |
| Pure thrust | , | 1.00 |

# Table A1-22B.-Radial Load Life Modifiers, Z; for Giving Desired Bearing Life <br> (Based on data from New Departure "Handbook") 



Table A1-22C.-Shock-load Factors
(From Norman, Ault, and Zarobsky, "Fundamentals of Machine Design")
Type of Service $K$ for Ball

|  | Bearing |
| :---: | :---: |
| Uniform steady load. | . 1.00 |
| Light shock load. | 1.50 |
| Moderate shock load | 2.00 |
| Heavy shock load. | 2.50 |
| Extreme and indeterm |  |

Table A1-22D.-Single-row Radial Bearings Type 1000
(Filling-notch type)
(From New Departure "Handbook")
Principal Dimensions
Provide maximum single-row capacity for radial loads. May be used for combined loads when chosen in accordance with factors $F$ (Table A1-22A).


| N.D. bearing No. | $\begin{gathered} \text { Bore } \\ B \end{gathered}$ |  | $\begin{gathered} \text { Diameter } \\ D \end{gathered}$ |  | Width W |  | Balls |  | $\underset{r^{*}}{\text { Radius }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mm . | In. | Mm. | In. | Mm. | In. | Diam. | No. |  |
| 1304 | 20 | 0.7874 | 52 | 2.0472 | 15 | 0.5906 | $13 / 32$ | 9 | 0.04 |
| 1404 | . |  | 72 | 2.8346 | 19 | 0.7480 | \%'6 | 8 |  |
| 1305 | 25 | 0.9843 | 62 | 2.4409 | 17 | 0. 6693 | 13/32 | 11 | 0.04 |
| 1405 | . |  | 80 | 3.1496 | 21 | 0.8268 | 5 | 8 | 0.06 |
| 1206 | . |  | 62 | 2.4409 | 16 | 0.6299 | 352 | $\cdots$ | 0.04 |
| 1306 | 30 | 1.1811 | 72 | 2.8346 | 19 | 0.7480 | 15/32 | 11 | 0.04 |
| 1406 | . |  | 90 | 3.5433 | 22 | 0.9055 | 1116 | 9 | 0.06 |
| 1207 | . | ...... | 72 | 2.8346 | 17 | 0.6693 | 316 | 12 | 0.04 |
| 1307 | 35 | 1.3780 | 80 | 3.1496 | 21 | 0.8268 | 1732 | 11 | 0.06 |
| 1407 | . . |  | 100 | 3.9370 | 25 | 0.9043 | 34 | 9 | 0.06 |
| 1208 | $\ldots$ |  | 80 | 3.1496 | 18 | 0.7087 | 15/32 | 13 | 0.04 |
| 1308 | 40 | 1.5748 | 90 | 3.5433 | 23 | 0.9055 | 1932 | 11 | 0.06 |
| 1408 | . . |  | 110 | 4.3307 | 27 | 1.0630 | 1316 | 9 | 0.08 |
| 1209 | $\cdots$ |  | 85 | 3.3465 | 19 | 0.7480 | 15.32 | 14 | 0.04 |
| 1309 | 45 | 1.7717 | 100 | 3.9370 | 25 | 0.9843 | 21/32 | 12 | 0.06 |
| 1409 | . . |  | 120 | 4.7244 | 29 | 1.1417 | $3{ }^{3}$ | 10 | 0.08 |
| 1210 | . |  | 90 | 3.5433 | 20 | 0.7874 | 15/32 | 15 | 0.04 |
| 1310 | 50 | 1.9685 | 110 | 4.3307 | 27 | 1.0630 | 23/32 | 12 | 0.08 |
| 1410 |  |  | 130 | 5.1181 | 31 | 1.2205 | 15ís | 10 | 0.08 |
| 1211 |  |  | 100 | 3.9370 | 21 | 0.8268 | 17/32 | 15 | 0.06 |
| 1311 | 55 | 2.1654 | 120 | 4.7244 | 29 | 1.1417 | 25/32 | 12 | 0.08 |
| 1411 |  |  | 140 | 5.5118 | 33 | 1.2992 | 1 | 10 | 0.08 |
| 1212 |  |  | 110 | 4.3307 | 22 | 0.8661 | 19/32 | 15 | 0.06 |
| 1312 | 60 | 2.3632 | 130 | 5.1181 | 31 | 1.2205 | 27,32 | 12 | 0.08 |
| 1412 |  |  | 150 | 5.9055 | 35 | 1.3780 | 17, 6 | 10 | 0.08 |

[^30]Table A1-22E.-Single-Row Radial Bearings Type 1000 (Filling-notch type)
(From New Departure "Handbook")
Radial Load Ratings
The bearing capacities listed on this page are basic radial load ratings in pounds, with rotating inner ring. From these ratings, bearings of the proper size for the service desired can readily. be selected by use of data given in Table A1-22D.

| N.D. | R.p.m. (n) |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ing <br> No. | 200 | 300 | 400 | 500 | 600 | 800 | 1,000 | 1,500 | 2,000 | 3,000 | 5,000 |
| 1304 | 1,565 | 1,365 | 1,240 | 1,150 | 1,085 | 982 | 915 | 800 | 726 | 635 | 535 |
| 1404 | 2,160 | 1,885 | 1,720 | 1,595 | 1,500 | 1,370 | 1,265 | 1, 105 | 1,005 | 875 | 0 |
| 1305 | 1,990 | 1,735 | 1,575 | 1,465 | 1,380 | 1,260 | 1,160 | 1,015 | 923 | 805 | 680 |
| 1405 | 2,580 | 2,250 | 2,050 | 1,900 | 1,790 | 1,625 | 1,510 | 1,315 | 1,195 | 1,045 | 883 |
| $1206{ }^{\circ}$ | 1,735 | 1,365 | 1,420 | 1,315 | 1,240 | 1,125 | 1,045 | 917 | 829 | 727 | 811 |
| 1306 | 2,490 | 2,170 | 1,970 | 1,825 | 1,720 | 1,570 | 1,450 | 1,270 | 1,150 | 1,005 | 886 |
| 1406 | 3,435 | 2,990 | 2,720 | 2,525 | 2,375 | 2,145 | 2,000 | 1,750 | 1,590 | 1,390 | 1,175 |
| 1207 | 2,530 | 2,210 | 2,005 | 1,865 | 1,755 | 1,595 | 1,480 | 1,290 | 1,175 | 1,025 | 865 |
| 1307 | 2,855 | 2,100 | 2,265 | 2,100 | 1,980 | 1,800 | 1,670 | 1,455 | 1,325 | 1,155 | 982 |
| 1407 | 3,980 | 3,475 | 3,160 | 2,935 | 2,760 | 2,520 | 2,330 | 2,030 | 1,845 | 1,610 | 1,355 |
| 1208 | 2,990 | 2,610 | 2,375 | 2,205 | 2,075 | 1,885 | 1,750 | 1,530 | 1,390 | i, 210 | 1,020 |
| 1308 | 3,560 | 3,110 | 2,830 | 2,625 | 2,470 | 2,245 | 2,080 | 1,820 | 1,650 | 1,440 | 1,205 |
| 1408 | 4,550 | 3,970 | 3,605 | 3,350 | 3,150 | 2,870 | 2,660 | 2,320 | 2,110 | 1,840 | 1, 560 |
| 1209 | 3,235 | 2,825 | 2,570 | 2,385 | 2,245 | 2,010 | 1,890 | 1,650 | 1,500 | 1,310 | 1,100 |
| 1309 | 4,400 | 3,835 | 3,480 | 3,240 | 3,045 | 2,770 | 2,570 | 2,245 | 2,040 | 1,780 | 1,500 |
| 1409 | 5,535 | 4,825 | 4,390 | 4,075 | 3,830 | 3,470 | 3,230 | 2,820 | 2,560 | 2,240 |  |
| 1210 | 3,495 | 3,055 | 2,775 | 2,580 | 2,430 | 2,195 | 2,040 | 1,785 | 1,620 | 1,415 |  |
| 1310 | 5, 065 | 4,410 | 4,020 | 3,820 | 3,510 | 3, 190 | 2,960 | 2,580 | 2,345 | 2,050 |  |
| 1410 | 6,190 | 5,400 | 4,900 | 4,550 | 4,290 | 3, 900 | 3,615 | 3,155 | 2,870 | 2,505 |  |
| 1211 | 4,120 | 3,650 | 3,310 | 3,075 | 2,895 | 2,625 | 2,440 | 2,135 | 1,940 | 1,695 |  |
| 1311 | 5,750 | 5,010 | 4,560 | 4,245 | 3,990 | 3,605 | 3,360 | 2,935 | 2,665 | 2,325 |  |
| 1411 | 6,870 | 6,000 | 5,450 | 5,060 | 4,770 | 4,320 | 4,015 | 3,510 | 3,190 | 2,785 |  |
| 1212 | 4,900 | 4,300 | 3,900 | 3,615 | 3,400 | 3,100 | 2,865 | 2,615 | 2,280 | 1,995 |  |
| 1312 | 6,490 | 5,655 | 5,145 | 4,780 | 4,495 | 4,100 | 3,790 | 3,310 | 3,010 | 2,620 |  |
| 1412 | 7,575 | 6,600 | 6,010 | 5,585 | 5,250 | 4,780 | 4,430 | 3,870 | 3,510 | 3,065 |  |

Table Al-22F.-Single-row Radial Bearings Type 1000 (Filling-notch type)
(From New Departure "Handbook")
Principal Dimensions
Provide maximum single-row capacity for radial loads. May be used for combined loads when chosen in accordance with factors $F$ (Table A1-22A).

| N.D. bearing No. | $\underset{B}{\text { Bore }}$ |  | $\begin{gathered} \text { Diameter } \\ D \end{gathered}$ |  | Width W |  | Balls |  | $\underset{r^{*}}{\text { Radius }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mm. | In. | Mm . | In. | Mm . | In. | Diam. | No. |  |
| 1213 | $\cdots$ |  | 120 | 4.7244 | 23 | 0.9055 | 21/32 | 15 | 0.06 |
| 1313 | 65 | 2.5591 | 140 | 5.5118 | 33 | 1.2992 | 29\%2 | 12 | 0.08 |
| 1413 | ... |  | 160 | 6.2992 | 37 | 1.4567 | 13/8 | 10 | 0.08 |
| 1214 | $\cdots$ | ...... | 125 | 4.9213 | 24 | 0.9449 | 23/32 | 15 | 0.06 |
| 1314 | 70 | 2.7559 | 150 | 5.9055 | 35 | 1.3780 | 31/32 | 12 | 0.08 |
| 1414 | $\ldots$ |  | 180 | 7.0866 | 42 | 1.6535 | 11/4 | 10 | 0.10 |
| 1215 | . | ..... | 130 | 5.1181 | 25 | 0.9843 . | 21/32 | 16 | 0.06 |
| 1315 | 75 | 2.9528 | 160 | 6.2992 | 37 | 1.4567 | 1 | 13 | 0.08 |
| 1415 | . . | . . . . . | 190 | 7.4803 | 45 | 1.7717 | 18/8 | 10 | 0.10 |
| 1216 | . | ...... | 140 | 5.5118 | 26 | 1.0236 | $11 / 16$ | 17 | 0.08 |
| 1316 | 80 | 3.1496 | 170 | 0.6929 | 39 | 1.5354 . | 1316 | 13 | 0.08 |
| 1416 | . . |  | 200 | 7.8740 | 48 | 1.8898 | 1716 | 10 | 0.10 |
| 1217 | $\cdots$ | ...... | 150 | 5.9055 | 28 | 1.1024 | 25/32 | 16 | 0.08 |
| 1317 | 85 | 3.3465 | 180 | 7.0866 | 41 | 1.6142 | 118 | 13 | 0.10 |
| 1417 | ... | ...... | 210 | 8.2677 | 52 | 2.0472 | 1122 | 10 | 0.12 |
| 1218 | ... | ...... | 160 | 6.2992 | 30 | 1.1811 | 23/32 | 15 | 0.08 |
| 1318 | 90 | 3.5433 | 190 | 7.4803 | 43 | 1.6929 | 1316 | 13 | 0.10 |
| 1418 | . . | ...... | 225 | 8.8583 | 54 | 2.1260 | 15\% | 10 | 0.12 |
| 1219 |  |  | 170 | 6.6929 | 32 | 1.2598 | 2932 | 15 | 0.08 |
| 1319 | 95 | 3.7402 | 200 | 7.8740 | 45 | 1.7717 | 1\%4 | 13 | 0.10 |
| 1220 | . . |  | 180 | $7.0866^{\circ}$ | 34 | 1.3386 | 31/32 | 15 | 0.08 |
| 1320 | 100 | 3.9370 | 215 | 8.4646 | 47 | 1.8504 | 13/8 | 12 | 0.10 |
| 1221 | . . |  | 190 | 7.4803 | 36 | 1.4173 | 1 | 16 | 0.08 |
| 1321 | 105 | 4.1339 | 225 | 8.8583 | 49 | 1.9291 | 17/18 | 12 | 0.10 |
| 1222 |  |  | 200 | 7.8740 | 38 | 1.4961 | 11/6 | 16 | 0.08 |
| 1322 | 110 | 4.3307 | 240 | 9.4488 | 50 | 1.9685 | 1\%2 | 12 | 0.10 |

[^31]Table A1-22G.-Single-row Radial Bharings Type 1000 (Filling-notch type)
(From New Departure "Handbook")
Radial Load Ratings
The bearing capacities listed on this page are basic radial load ratings in pounds, with rotating inner ring. From these ratings, bearings of the proper size for the service desired can readily be selected by use of data given in Table A1-22F.

|  | R.p.m. (n) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ing <br> No. | 200 | 300 | 400 | 500 | 600 | 800 | 1,000 | 1,500 | 2,000 | 3,000 |
| 1213 | 5,675 | 4,975 | 4,500 | 4,180 | 3,940 | 3,585 | 3,315 | 2,910 | 2,640 | 2,300 |
| 1313 | 7,210 | 6,300 | 5,730 | 5,310 | 5,000 | 4,510 | 4,215 | 3,680 | 3,350 | 2,915 |
| 1413 | 8,295 | 7,245 | 6,580 | 6,110 | 5,750 | 5,200 | 4,850 | 4,235 | 3,850 | 3,360 |
| 1214 | 5,770 | 5,060 | 4,575 | 4,250 | 4,005 | 3,645 | 3,375 | 2,955 | 2,680 | 2,335 |
| 1314 | 8,000 | 6,980 | 6,350 | 5,895 | 5,550 | 5,025 | 4,675 | 4,080 | 3,710 | 3,240 |
| 1414 | 9,720 | 8,490 | 7,800 | 7,160 | 6,740 | 6,050 | 5,685 | 4,965 | 4,510 | 3,940 |
| 1215 | 6,100 | 5,360 | 4,850 | 4,500 | 4,240 | 3,860 | 3,580 | 3,145 | 2,845 | 2,485 |
| 1315 | 9,010 | 7,860 | 7,150 | 6,640 | 6,250 | 5,680 | 5,260 | 4,600 | 4,180 | 3,650 |
| 1415 | 11,010 | 9,600 | 8,740 | 8,100 | 7,625 | 6,930 | 6,430 | 5,625 | 5,110 |  |
| 1216 | 6,900 | 6,025 | 5,490 | 5,090 | 4,790 | 4,360 | 4,040 | 3,525 | 3,200 | 2,800 |
| 1316 | 9,890 | 8,635 | 7,845 | 7,290 | 6,875 | 6,220 | 5,780 | 5,050 | 4,590 |  |
| 1416 | 11,880 | 10,350 | 9,420 | 8,750 | 8,235 | 7,500 | 6,945 | 6,060 | 5,510 |  |
| 1217 | 7,850 | 6,880 | 6,220 | 5,780 | 5,440 | 4,940 | 4,585 | 4,020 | 3,645 |  |
| 1317 | 10,750 | 9,395 | 8,530 | 7,925 | 7,465 | 6,780 | 6,290 | 5,495 | 4,990 |  |
| 1417 | 12,700 | 11,090 | 10,050 | 9,350 | 8,800 | 8,010 | 7,420 | 6,475 | 5,890 |  |
| 1218 | 8,400 | 7,370 | 6,680 | 6,190 | 5,820 | 5,300 | 4,920 | 4,310 | 3,900 |  |
| 1318 | 11,690 | 10,200 | 9,275 | 8,605 | 8,110 | 7,380 | 6,835 | 5,970 | 5,415 |  |
| 1418 | 14,200 | 12,400 | 11,280 | 10,460 | 9,850 | 8,960 | 8,300 | 7,250 | 6,590 |  |
| 1219 | .9,300 | 8,150 | 7,400 | 6,850 | 6,450 | 5,880 | 5,440 | 4,770 | 4,320 |  |
| 1319 | 12,600 | 11,000 | 10,000 | 9,300 | 8,745 | 7,970 | 7,360 | 6,440 | 5,850 |  |
| 1220 | 10,225 | 8,975 | 8,150 | 7,540 | 7,110 | 6,480 | 5,990 | 5,250 | 4,750 |  |
| 1320 | 13,550 | 11,830 | 10,750 | 10,000 | 9,410 | 8,550 | 7,930 | 6,930 | 6,295 |  |
| 1221 | 11,330 | 9,900 | 9,000 | 8,350 | 7,860 | 7,130 | 6,630 | 5,785 | 5,260 |  |
| 1321 | 14,510 | 12,680 | 11,510 | 10,700 | 10,080 | 9, 170 | 8,495 | 7,425 | 6,735 |  |
| 1222 | 12,320 | 10,780 | 9,790 | 9,100 | 8,550 | 7,750 | 7,210 | 6,300 | 5,715 |  |
| 1322 | 15,400 | 13,600 | 12,250 | 11,480 | 10,700 | 9,780 | 9,105 | 7,870 | 7,160 |  |

Table A1-22H.-Single-row Radial Bearings Type 3000
(No filling-notch type)
(From New Departure "Handbook")
Principal Dimensions
For radial or combined loads from either direction where thrust is to be resisted by a single bearing and is not great enough to require use of angular contact type. For capacities under thrust or combined loads, use factors $F$ (Table A1-22A).

| N.D. bearing No. | $\begin{gathered} \text { Bore } \\ B \end{gathered}$ |  | $\begin{gathered} \text { Diameter } \\ D \end{gathered}$ |  | Width W |  | Balls |  | $\underset{r^{*}}{\text { Radius }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mm. | In. | Mm. | In. | Mm . | In. | Diam. | No. |  |
| 3200 | . |  | 30 | 1.1811 | 9 | $0.35 \pm 3$ | 73์2 | 7 | 0.025 |
| 3300 | 10 | 0.3937 | 35 | 1.3780 | 11 | 0.4331 | 1/4 | 7 |  |
| 3201 | . | ..... | 32 | 1.2598 | 10 | 0.3937 | 0.210 | 8 | 0.025 |
| 3301 | 12 | 0.4724 | 37 | 1.4567 | 12 | 0.4724 | \% $\% 2$ | 7 | 0.04 |
| 3202 | $\ldots$ |  | 35 | 1.3780 | 11 | 0.4331 | 0.210 | 9 | 0.025 |
| 3302 | 15 | 0.5906 | 42 | 1.6536 | 13 | 0.5118 | 516 | 7 | 0.04 |
| 3203 | . | ...... | 40 | 1.5748 | 12 | 0.4724 | 9/32 | 8 |  |
| 3303 | 17 | 0.6693 | 47 | 1.8504 | 14 | 0.5512 | ${ }^{13} 32$ | 7 | 0.04 |
| 3204 | . |  | 47 | 1.8504 | 14 | 0.5512 | 516 | 8 |  |
| 3304 | 20 | 0.7874 | 52 | 2.0472 | 15 | 0.5906 | 33/32 | 7 | 0.04 |
| 3205 | . |  | 52 | 2.0472 | 15 | 0.5906 | 516 | 9 |  |
| 3305 | 25 | 0.9843 | 62 | 2.4409 | 17 | 0.6693 | 1332 | 8 | 0.04 |
| 3206 | . | ...... | 62 | 2.4409 | 16 | 0.6299 | 36 | 9 |  |
| 3306 | 30 | 1.1811 | 72 | 2.8346 | 19 | 0.7480 | 15.52 | 8 | 0.04 |
| 3207 | . |  | 72 | 2.8346 | 17 | 0.6693 | $7{ }^{76}$ | 9 | 0.04 |
| 3307 | 35 | 1.3780 | 80 | 3.1496 | 21 | 0.8268 | 1732 | 8 | 0.06 |
| 3208 | . |  | 80 | 3.1496 | 18 | 0.7087 | 15.32 | 9 | 0.04 |
| 3308 | 40 | 1.5748 | 90 | 3.5433 | 23 | 0.9055 | 1932 | 8 | 0.06 |
| 3209 | . | . . . . . | 85 | 3.3465 | 19 | 0.7480 | $15 \% 2$ | 10 | 0.04 |
| 3309 | 45 | 1.7717 | 100 | 3.9370 | 25 | 0.9843 | $21 / 32$ | 8 | 0.06 |
| 3210 |  |  | 90 | 3.5433 | 20 | 0.7874 | 15.38 | 11 | 0.04 |
| 3310 | 50 | 1.9685 | 110 | 4.3307 | 27 | 1.0630 | $23 \% 2$ | 8. | 0.08 |
| 3211 |  |  | 100 | 3.0370 | 21 | 0.8268 | 17.32 | 11 | 0.06 |
| 3311 | 55 | 2.1654 | 120 | 4.7244 | 29 | 1.1417 | 2532 | 8 | 0.08 |

[^32] will clear.

Table A1-22I.-Single-row Radial Bearings Type 3000 (No filling-notch type)
(From New Departure "Handbook")

## Radial Load Ratings

The bearing capacities listed on this page are basic radial load ratings in pounds, with rotating inner ring. From these ratings, bearings of the proper size for the service desired can readily be selected by use of data given in Table A1-22H.

|  | R.p.m. |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ing <br> No. | 200 | 300 | 400 | 500 | 600 | 800 | 1,000 | 1,500 | 2,000 | 3,000 | 5,000 |
| 3200 | 419 | 364 | 332 | 307 | 290 | 264 | 244 | 213 | 194 | 169 | 140 |
| 3300 | 481 | 419 | 381 | 356 | 333 | 305 | 281 | 245 | 223 | 195 | 163 |
| 3201 | 515 | 450 | 410 | 380 | 357 | 319 | 301 | 263 | 239 | 209 | 162 |
| 3301 | 603 | 523 | 479 | 441 | 419 | 379 | 352 | 307 |  | 244 | . 209 |
| 3202 | 610 | 533 | 485 | 450 | 424 | 388 | 357 | 312 | 284 | 248 | 200 |
| 3302 | 712 | 620 | 564 | 521 | 493 | 448 | 415 | 362 | 330 | 288 | 242 |
| 3203 | 788 | 689 | 625 | 581 | 546 | 494 | 460 | 402 | 365 | 319 | 270 |
| 3303 | 832 | 729 | 660 | 612 | 578 | 523 | 486 | 425 | 386 | 337 | 284 |
| 3204 | 944 | 827 | 749 | 690 | 655 | 595 | 552 | 482 | 438 | 381 | 321 |
| 3304 | 1,160 1 | 1,010 | 917 | 851 | 802 | 726 | 677 | 593 | 537 | 470 | 398 |
| 3205 | 1,120 | 976 | 889 | 825 | 775 | 700 | 655 | 571 | 520 | 454 | 383 |
| 3305 | 1,560 1 | 1,360 | 1,235 | 1,140 | 1,080 | 988 | 910 | 795 | 724 | 631 | 534 |
| 3206 | 1,475 1 | 1,290 | 1,175 | 1,085 | 1,025 | 930 | 865 | 758 | 683 | 600 | 503 |
| 3306 | 1,9.55 1 | 1,700 | 1,545 | 1,430 | 1,350 | 1,230 | 1,140 | 996 | 902 | 788 | 695 |
| 3207 | 2,090 1 | 1,825 | 1,655 | 1,540 | 1,450 | 1,315 | 1,220 | 1,065 | 970 | 845 | 714 |
| 3307 | 2,240 | 1,950 | 1,775 | 1,650 | 1,550 | 1,410 | 1,310 | 1,140 | 1,040 | 905 | 770 |
| 3208 | 2,340 | 2,040 | 1,860 | 1,725 | 1,620 | 1,475 | 1,370 | 200 | 090 | 947 | 798 |
| 3308 | 2,790 | 2,440 | 2,220 | 2,060 | 1,935 | 1,760 | 1,630 | 1,430 | 1,295 | 1,130 | 945 |
| 3209 | 2,580 2 | 2,260 | 2,045 | 1,900 | 1,790 | 1,600 | 1,510 | 1,315 | 00 | 5 | 877 |
| 3309 | 3,260 2 | 2,840 | 2,580 | 2,400 | 2,255 | 2,055 | 1,905 | 1,660 | 1,510 | 1,320 | 1,110 |
| 3210 | 2,640 | 2,455 | 2,240 | 2,100 | 1,980 | 1,780 | 1,660 | 1,450 | 1,320 | 1,150 |  |
| 3310 | 3,7553 | 3,270 | 2,980 | 2,830 | 2,600 | 2,360 | 2,195 | 1,910 | 1,735 | 1,520 |  |
| 3211 | 3,390 | 2,985 | 2,700 | 2,500 | 2,355 | 2,140 | 1,980 | 1,735 | 1,580 | 1,380 |  |
| 3311 | 4,2553 | 3,715 | 3,385 | 3,1402 | 2,960 | 2,675 | 2,490 | 2,175 | 1,975 | 1,725 |  |

## Table A1-22J.-Single-row Radial Bearings Type 3000 (No filling-notch type) <br> (From New Departure "Handbook") <br> Principal Dimensions

For radial or combined loads from either direction where thrust is to be resisted by a single bearing and is not great enough to require use of angular contact type. For capacities under thrust or combined loads, use factors $F$ (Table A1-22A).


| N.D. bearing No. | $\begin{gathered} \text { Bore } \\ B \end{gathered}$ |  | $\begin{gathered} \text { Diameter } \\ D \end{gathered}$ |  | Width W |  | Balls |  | $\underset{r^{*}}{\text { Radius }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Mm. | In. | Mm . | In. | Mm. | In. | Diam. | No. |  |
| 3212 | 60 | 2.3622 | 110 | 4.3307 | 22 | 0.8661 | 19/32 | 10 | 0.06 |
| 3312 | . . | $\cdots$ | 130 | 5.1181 | 31 | 1.2205 | 27/32 | 8 | 0.08 |
| 3213 | ... | ...... | 120 | 4.7244 | 23 | 0.9055 | 21/32 | 10 | 0.06 |
| 3313 | 65 | 2.5591 | 140 | 5.5118 | 33 | 1.2992 | 29/32 | 8 | 0.08 |
| 3214 |  | ...... | 125 | 4.9213 | 24 | 0.9449 | 21/32 | 11 | 0.06 |
| 3314 | 70 | 2.7559 | 150 | 5.9055 | 35 | 1.3780 | ${ }^{1 / 3} 2$ | 8 | 0.08 |
| 3215 | $\cdots$ |  | 130 | 5.1181 | 25 | 0.9843 | 21/32 | 11 | 0.06 |
| 3315 | 75 | 2.9528 | 160 | 6.2992 | 37 | 1.4567 | 1 | 8 | 0.08 |
| 3216 | $\ldots$ |  | 140 | 5.5118 | 26 | 1.0236 | 11/16 | 11 |  |
| 3316 | 80 | 3.1496 | 170 . | 6.6929 | 39 | 1.5354 | 1116 | 8 | 0.08 |
| 3217 | ... |  | 150 | 5.9055 | 28 | 1.1024 | 25/32 | 11 | 0.08 |
| 3317 | 85 | 3.3465 | 180 | 7.0866 | 41 | 1.6142 | 11/8 | 8 | 0.10 |
| 3218 | $\ldots$ |  | 160 | 6.2992 | 30 | 1.1811 | 27/32 | 11 | 0.08 |
| 3318 | 90 | 3.5433 | 190 | 7.4803 | 43 | 1.6929 | 13/16 | 8 | 0.10 |
| 3219 | $\ldots$ |  | 170 | 6.6929 | 32 | 1.2598 | 2932 | 11 | 0.08 |
| 3319 | 95 | 3.7402 | 200 | 7.8740 | 45 | 1.7717 | 11/4 | 8 | 0.10 |
| 3220 |  |  | 180 | 7.0866 | 34 | 1.3386 | 31/32 | 11 | 0.08 |
| 3320 | 100 | 3.9370 | 215 | 8.4646 | 47 | 1.8504 | 13/8 | 8 | 0.10 |
| 3221 |  |  | 190 | 7.4803 | 36 | 1.4173 | 1 | 11 | 0.08 |
| 3321 | 105 | 4.1339 | 225 | 8.8583 | 49 | 1.9291 | 176 | 8 | 0.10 |
| 3222 |  |  | 200 | 7.8740 | 38 | 1.4961 | 1116 | 11 | 0.08 |
| 3322 | 110 | 4.3307 | 240 | 9.4488 | 50 | 1.9685 | 11/2 | 8 | 0.10 |

[^33]Table A1-22K.-Single-row Radial Bearings, Type 3000 (No filling-notch type)
(From New Departure "Handbook")
Radial Load Ratings
The bearing capacities listed on this page are basic radial load ratings in pounds, with rotating inner ring. From these ratings, bearings of the proper size for the service desired can readily be selected by use of data given in Table A1-22J.

| $\begin{aligned} & \text { N.D. } \\ & \text { No. } \end{aligned}$ | R.p.m. (n) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 200 | 300 | 400 | 500 | 600 | 800 | 1,000 | 1,500 | 2,000 | 3,000 |
| 3212 | 3,750 | 3,290 | 2,970 | 2,750 | 2,595 | 2,360 | 2,180 | 1,920 | 1,735 | 1,520 |
| 3312 | 4,805 | 4,200 | 3,815 | 3,540 | 3,330 | 3,040 | 2,810 | 2,455 | 2,230 | 1,940 |
| 3213 | 4,325 | 3,800 | 3,435 | 3,180 | 3,000 | 2,725 | 2,525 | 2,215 | 2,010 | 1,750 |
| 3313 | 5,350 | 4,665 | 4,250 | 3,940 | 3,705 | 3,345 | 3, 130 | 2,730 | 2,485 | 2,160 |
| 3214 | 4,700 | 4,100 | 3,720 | 3,455 | 3,250 | 2,960 | 2,745 | 2,405 | 2, 180 | 1,895 |
| 3314 | 5,930 | 5,170 | 4,705 | 4,365 | 4, 110 | 3,725 | 3, 465 | 3,025 | 2,750 | 2,400 |
| 3215 | 4,770 | 4,165 | 3,780 | 3,510 | 3,300 | 3,005 | 2,790 | 2,445 | 2,210 | 1,920 |
| 3315 | 6,325 | 5,520 | 5,020 | 4,660 | 4,395 | 3,980 | 3,700 | 3,230 | 2,935 | 2,565 |
| 3216 | 5,155 | 4,500 | 4,100 | 3,800 | 3,575 | 3,260 | 3,020 | 2,635 | 2,390 | 2,095 |
| 3316 | 6,945 | 6,055 | 5,505 | 5,110 | 4,825 | 4,365 | 4,055 | 3,550 | 3,220 |  |
| 3217 | 6,100 | 5,340 | 4,845 | 4,500 | 4,235 | 3,845 | 3,560 | 3,135 | 2,835 |  |
| 3317 | 7,550 | 6,600 | 5,990 | 5,560 | 5,250 | 4,750 | 4,410 | 3,860 | 3, 500 |  |
| 3218 | 6,820 | 5,990 | 5,420 | 5,010 | 4,740 | 4,310 | 4,000 | 3,500 | 3,170 |  |
| 3318 | 8,205 | 7,160 | 6,510 | 6,050 | 5,700 | 5,185 | 4,800 | 4,200 | 3,810 |  |
| 3219 | 7,580 | 6,620 | 6,000 | 5,570 | 5,230 | 4,785 | 4,425 | 3,880 | 3,510 |  |
| 3319 | 8,845 | 7,725 | 7,020 | 6,530 | 5,135 | 5,595 | 5,160 | 4,510 | 4, 100 |  |
| 3220 | 8,320 | 7,300 | 6,620 | 6,130 | 5,790 | 5,260 | 4,875 | 4,265 | 3,865 |  |
| 3320 | 10,040 | 8,760 | 7,960 | 7,400 | 6,970 | 6,330 | 5,880 | 5, 140 | 4,660 |  |
| 3221 | 8,780 | 7,700 | 6,990 | 6,480 | 6,100 | 5,530 | 5,150 | 4,480 | 4,080 |  |
| 3321 | 10,750 | 9,390 | 8,535 | 7,930 | 7,460 | 6,790 6 | 6,295 | 5,500 | 4,985 |  |
| 3222 | 9,550 | 8,390 | 7,600 | 7,075 | 6,630 | 6,010 | 5,600 | 4,890 | 4,440 |  |
| 3322 | 11,410 | 10,080 | 9,070 | 8,500 | 7,925 | 7,235 | 6,745 | 5,835 | 5,305 |  |

Table A1-23.-Roller-bearing Selection
For conditions of extreme load or severe shock loads such as occur in the main bearings of radial engines, roller-type bearings are frequently most applicable. For a given size, roller bearings have a greater loadcarrying capacity than ball bearings because they provide "line" contact as against "point" contact. Cylindrical roller bearings have the disadvantage of inability to take appreciable thrust loads. Roller bearings are manufactured in the "metric" and "inch" types; data on the latter are given in Tables A1-22B and A1-22C. Inch-type bearings* as manufactured by the Norma-Hoffmann Bearings Corporation are further classified as "standard," "one-lipped," and "two-lipped" types (see Fig. A). Standard and one-lipped types of roller bearings correspond in general to filling-notch types of ball bearings in that they contain the maximum number of rollers. Two-lipped type roller bearings correspond in general to non-filling-notch types of ball bearings, but they cannot take thrust loads. Standard roller bearings have the advantage over one- and particularly two-lipped types in that endwise movement of the shaft does not bind the rollers in the outer race, but this entails provision of means to hold the


Fig. A.-Types of roller bearings. outer race from slipping out of position. In general, one- and two-lipped types of roller bearings are preferable for radial-engine main bearings because the outer races can be more easily held in place axially.

Radial load ratings for Hoffmann roller bearings are given in Tables A1-23B and A1-23C for the range of bearing sizes most likely to be needed for aircraft-engine main bearings. (Load ratings for standard types are the same as for the one-lipped type. The bearing numbers differ by the deletion of the $L$ in the standard type.) These load ratings are for nonshock conditions and are based on a life of $10,000 \mathrm{hr}$. For aircraft-engine main bearings, the load $C$ for entry in the load tables may be determined from

$$
\begin{equation*}
C=L \times Z \times K \tag{1}
\end{equation*}
$$

where $C=$ equivalent radial capacity, lb .
$L=$ calculated radial load on the bearing, lb.
$Z=$ life factor for a desired bearing life other than $10,000 \mathrm{hr}$. (Fig. B).
$K=$ the shock load factor (Table Al-23A).
To determine the proper size of roller bearing, enter $C$ as determined by Eq. (1) in Table A1-23B or A1-23C (as applies) at the proper r.p.m. and read the major bearing dimensions and the bearing number on the left side of the table.

[^34]

Desired life, hours $\times 10^{-2}$
Desired life hours $\times 10^{-2}$.

Table A1-23A.-Shock-load Factoris for Roller Bearings

Type of Service Factor, $K$
Uniform and steady load. ....... . 1.0
Light shock load. . . . . . . . . . . . . . . . . 1.0
Moderate shock load. . . . . . . . . . . . 1.3
Heavy shock load. . . . . . . . . . . . . . . 1.7
Extreme and indeterminate shock
load.............................. . . 2.0
Fig. $B$.
Table A1-23B.-One-lipped Inch-type Hoffmann Precision
Rollef Bearings
(From engineering data of the Norma-Hoffmann Bearings Corporation)

| Bearing No. | Bearing dimensions, in. |  |  |  | Load in pounds at speed in r.p.m. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | $B$ | $C$ | $H$ | 500 | 1,000 | 1,500 | 2,000 | 3,000 |
| RLS-L Type Light Series |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | * |  |  |
| RLS-15-L | 2 | 4 | 0.8125 | 0.0937 | 2,610 | 2,070 | 1,810 | 1,640 | 1,430 |
| RLS-16-L | 2.250 | 4.500 | 0.875 | 0.0937 | 3,420 | 2,710 | 2,370 | 2,150 | 1,880 |
| RLS-17-L | 2.500 | 5 | 0.9375 | 0.0937 | 4,050 | 3,210 | 2,800 | 2,550 | 2,230 |
| RLS-18-L | 2.750 | 5.250 | 0.9375 | 0.0937 | 4,300 | 3,410 | 2,980 | 2,710 | 2,370 |
| RLS-19-L. | 3. | 5.750 | 1.0625 | 0.0937 | 5,290 | 4.200 | 3,670 | 3,330 |  |
| RLS-19.5-L | 3.250 | 8 | 1.0625 | 0.0937 | $\cdot 5,600$ | 4,440 | 3,880 | 3,530 |  |
| RLS-20-L. | 3.500 | 6.500 | 1. 125 | 0.125 | 6,750 | 5,360 | 4,680 | 4,250 |  |
| RLS-20.5-L | 3.750 | 6.750 | 1.125 | 0.125 | 7,130 | 5,660 | 4,940 | 4,480 |  |
| RLS-21-L | 4 | 7.250 | 1.250 | 0.125 | 7,950 | 6,310 | 5,510 | 5,010 |  |
| RMS-L Type Medium Series |  |  |  |  |  |  |  |  |  |
| RMS-15-L. | 2 | 4.50 | 1.0625 | 0.0937 | 5,390 | 4,280 | 3,740 | 3,400 | 2,970 |
| RMS-16-L. | 2.250 | 5 | 1.250 | 0.125 | 6,000 | 4,760 | 4,160 | 3,780 | 3,300 |
| RMS-17-L. | 2.500 | 5.500 | 1.250 | 0.125 | 7,500 | 5,950 | 5,200 | 4,720 | 4, 130 |
| RMS-18-L | 2.750 | 6.250 | 1.375 | 0.125 | 10,300 | 8,170 | 7,140 | 6,490 |  |
| RMS-19-L |  | 7 | 1.5625 | 0.1562 | 12,620 | 10,010 | 8,740 | 7,940 |  |
| RMS-19.5-L. | 3.250 | 7.500 | 1.5625 | 0.1562 | 13,520 | 10,730 | 9,370 | 8,510 |  |
| RMS-19.75-L | 3.375 | 7.500 | 1.5625 | 0.1562 | 13,520 | 10,730 | 9,370 | 8,510 |  |
| RMS-20-L. | 3.500 | 8.125 | 1.750 | 0.1562 | 15,920 | 12,630 | 11,040 | 10,030 |  |
| RMS-20.5-L | 3.750 | 8.250 | 1.750 | 0.1562 | 15,920 | 12,630 | 11,040 | 10,030 |  |
| RMSS-21-L. | 4 | 8.500 | 1.750 | 0.1562 | 17,060 | 13,540 | 11,820 | 10,740 |  |
| RMSS-21.5-L | 4.500 | 8.750 | 1.750 | 0.1562 | 17,060 | 13,540 | 11,820 | 10,740 |  |

Note: Bearing dimension symbols correspond to figures on p. 417.

Table A1-23C.-Two-lipped Inch-type Hoffmann Precision
Roller Bearings
(From Engineering Data of the Norma-Hoffmann Bearings Corporation)

| Bearing No. | Bearing dimensions, in. |  |  |  | Load in pounds at speed in r.p.m. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | $B$ | C | $H$ | 500 | 1,000 | 1,500 | 2,000 | 3,000 |
| RLS-LL Type Light Series |  |  |  |  |  |  |  |  |  |
| RLS-15-LL. | 2 | 4 | 0.8125 | 0.0937 | 2,300 | 1,830 | 1,600 | 1,450 | 1,270 |
| RLS-16-LL. | 2.250 | 4.500 | 0.875 | 0.0937 | 3,010 | 2,390 | 2,090 | 1,900 | 1,660 |
| RLS-17-LL. | 2.500 | 5 | 0.9375 | 0.0937 | 3,550 | 2,820 | 2,460 | 2,230 | 1,950 |
| RLS-18-LL. | 2.750 | 5.250 | 0.9375 | 0.0937 | 3,790 | 3,010 | 2,630 | 2,390 | 2,090 |
| RLS-19-LL. | 3 | 5.750 | 1.0625 | 0.0937 | 4,670 | 3,700 | 3,230 | 2,940 |  |
| RLS-19.5-LL | 3.250 | 6 | 1.0625 | 0.0937 | 4,980 | 3,950 | 3,450 | 3,130 |  |
| RLS-20-LL. | 3.500 | 6.500 | 1.125 | 0.125 | 5,810 | 4,610 | 4,030 | 3,660 |  |
| RLS-20.5-LL | 3.750 | 6.750 | 1.125 | 0.125 | 6,190 | 4,910 | 4,290 | 3,900 |  |
| RLS-21-LL | 4 | 7.250 | 1.250 | 0.125 | 7,070 | 5,610 | 4,900 | 4,460 |  |
| RMS-LL Type Medium Series |  |  |  |  |  |  |  |  |  |
| RMS-15-LL | 2 | 4.50 | 1.0625 | 0.0937 | 4,770 | 3,790 | 3,310 | 3,000 | 2,620 |
| RMS-16-LL | 2.250 | 5 | 1.250 | 0.125 | 5,500 | 4,370 | 3,810 | 3,460 | 3,030 |
| RMS-17-LL | 2.500 | 5.500 | 1.250 | 0.125 | 6,500 | 5,160 | 4,510 | 4,090 | 3,580 |
| RMS-18-LL. | 2.750 | 6.25 | 1.375 | 0.125 | 8,580 | 6,810 | 5,950 | 5,410 |  |
| RMS-19-LL | 3 | 7 | 1.5625 | 0.1562 | 10,810 | 8,580 | 7,500 | 6,810 |  |
| RMS-19.5-LL | 3.250 | 7.500 | 1.5625 | 0.1562 | 11,260 | 8,940 | 7,810 | 7,090 |  |
| RMS-19.75-LL | 3.375 | 7.500 | 1.5625 | 0.1562 | 11,250 | 8,940 | 7,810 | 7,090 |  |
| RMS-20-LL | 3.500 | 8.125 | 1.750 | 0.1562 | 13,660 | 10,830 | 9,460 | 8,600 |  |
| RMS-20.5-LL. | 3.750 | 8.250 | 1.750 | 0.1562 | 13,660 | 10,830 | 9,460 | 8,600 |  |
| RMS-21-LL. | 4 | 8.50 | 1.750 | 0.1562 | 14,780 | 11,730 | 10,250 | 9,310 |  |

Note: Bearing dimension symbols correspond to figures on page 417.

Table A1-23D.-Extra-light Inch-type Hoffmann Precision Roller Bearings
(From engineering data of the Norma-Hoffmann Bearings Corporation)
RXLS Type Extra Light Series


| Bearing No. | Bearing dimensions, in. |  |  |  | Loads in pounds at speed in r.p.m. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | A | $B$ | C | $H$ | 500 | 1,000 | 1,500 | 2,000 | 3,000 |
| RXLS | 2. | 3.3125 | 0.625 | 0.0625 | 1,320 | 1,050 | 915 | 830 | 5 |
| RXLS-2.125 | 2.125 | 3.4375 | 0.625 | 0.0625 | 1,470 | 1,160 | 1,020 | 925 | 805 |
| RXLS-2.25. | 2.25 | 3.5625 | 0.625 | 0.0625 | 1,470 | 1,160 | 1,020 | 925 | 805 |
| RXLS-2.375 | 2.375 | 3.75 | 0.6875 | 0.0625 | 1,570 | 1,250 | 1,090 | 990 | 865 |
| RXLS-2.5 | 2.5 | 3.875 | 0.6875 | 0.0625 | 1,750 | 1,390 | 1,210 | 1,100 | 960 |
| RXLS-2.625 | 2.625 | 4.125 | 0.6875 | 0.0625 | 1,750 | 1,390 | 1,210 | 1,100 | 960 |
| RXLS-2.75 | 2.75 | 4.125 | 0.6875 | 0.0625 | 1,920 | 1,520 | 1,330 | 1, 210 | 1,060 |
| RXLS-2.875 | 2.875 | 4.5 | 0.75 | 0.0937 | 2,250 | 1,780 | 1,560 | 1, 420 | 1,240 |
| RXXLS-3 | 3. | 4.5 | 0.75 | 0.0937 | 2,250 | 1,780 | 1,560 | 1,420 | 1,240 |
| RXLS-3.125 | 3.125 | 4.75 | 0.75 | 0.0937 | 2,250 | 1,780 | 1,560 | 1,420 | 1,240 |
| RXLS-3.25. | 3.25 | 4.75 | 0.75 | 0.0937 | 2,250 | 1,780 | 1,560 | 1,420 | 1,240 |
| RXLS-3.375 | 3.375 | 5. | 0.75 | 0.0937 | 2,450 | 1,950 | 1,700 | 1,540 | 1,350 |
| RXLS-3.5 | 3.5 | 5. | 0.75 | 0.0937 | 2,450 | 1,950 | 1,700 | 1,540 | 1,350 |
| RXLS-3.625 | 3.625 | 5.25 | 0.75 | 0.0937 | 2,660 | 2,110 | 1,840 | 1,670 | 1,460 |
| RXLS-3.75. | 3.75 | 5.25 | 0.75 | 0.0937 | 2,660 | 2,110 | 1,840 | 1,670 | 1,460 |
| RXLS-3.875 | 3.875 | 5.625 | 0.875 | 0.0937 | 3,210 | 2,550 | 2,230 | 2,020 | 1,770 |
| RXLS-4 | 4. | 5.625 | 0.875 | 0.0937 | 3,210 | 2,550 | 2,230 | 2,020 | 1,770 |

Table A1-24.-Average Weights and Over-all Dimensions of Bendix-Stromberg Aircraft Carburetors

| $\begin{aligned} & \text { Model } \\ & \text { NA- } \end{aligned}$ | Dry weight, lb . | Height flange to flange | Over-all height | Over-all width | Over-all depth | Barrel diameter, in. | Total barrel area, sq. in. | Number of barrels | Discharge nozzles diameter, in. | Total dischargenozzle area, sq. in. | $\begin{gathered} \text { Maxi- } \\ \text { mum } \\ \text { vent, in. } \end{gathered}$ | Total maximum net vent area sq. in. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| S2. | 2.55 | 41/4 | 4344 | 5\% 16 | 434 | 17/6 | 1.623 | 1 | 7/16 | 0.150 | 118 | 0.844 |
| S3. | 2.55 | 41/4 | 438 | 5916 | 434 | $111 / 6$ | 2.236 | 1 | 716 | 0.150 | 1388 | 0.844 |
| R3. | 4.80 | 61/8 | 65\% | 67\% | 474 | ${ }^{11} 116$ | 2.236 | 1 | 1/2 | 0.196 | 13/8 | 1.289 |
| R3A. | 4.80 | 614 | 67/6 | 61\% | 43/4 | 1116 | 2.236 | 1 | $1 / 2$ | 0.196 | 138 | 1.289 |
| DD4. | 8.00 | 5\% | 512 | 71/8 | 711/6 | 11516 | 5.896 | 2 | 5/8 | 0.614 | 11/2 | 2.921 |
| R4.. | 4.80 | 6\% | 67/16 | 6516 | 47\% | 115/6 | 2.948 | 1 | 1/2 | 0.196 | 13/2 | 1.571 |
| R4A. | 4.80 | 6\% 3 | 69/6 | $6^{11 / 16}$ | 47/8 | ${ }^{11} / 16$ | 2.948 | 1 | 3/2 | 0.196 | 1216 | 1.721 |
| R4D. | 5.30 | 53/8 | $51 / 2$ | 614 | 534 | 11516 | 2.948 | 1 | 716 | 0.150 | 12/16 | 1.767 |
| T4B. | 12.50 | 75/32 | 75/32 | 91/8 | 71316 | ${ }^{15} 516$ | 8.845 | 3 | 21/32 | 1.015 | 1 $1 / 2$ | 4.287 |
| U4J. | 8.75 | $90^{\circ}$ | 75/8 | 101/8 | 511/16 | 15516 | 5.896 | 2 | 23/32 | 0.811 | 13/2 | 2.723 |
| R5.. | 7.25 | 634 | 7316 | 73\% | 614 | 23/6 | 3.758 | 1 | 27/32 | 0.559 | 178 | 2.202 |
| R5ı. | 7.50 | 63/4 | 73/6 | 61/4 | 61/4 | 2316 | 3.758 | 1 | 27/32 | 0.559 | 178 | 2.202 |
| R5H. | 6.20 | Length 61/2 | 6 | 7\% | 61/2 | 23/16 | 3.758 | 1 | H6 | 0.494 | 118/16 | 2.454 |
| S5A. | 5.50 | 63/6 | 612 | 73/16 | 53/4 | 23156 | 3.758 | 1 | 27/32 | 0.559 | 17/8 | 2.202 |
| Y5D. | 10.25 | 63/82 |  | 65\% | 9516 | 23.16 | 7.516 | 2 | 27/52 | 1.118 | 178 | 4.404 |
| Y5F. | 10.25 | 63/32 | 69/16 | 65\% | 93/8 | 23/6 | 7.516 | 2 | 27/32 | 1.118 | 178 | 4.404 |
| R6.. | 7.25 | 63/4 | 73/16 | 7716 | 614 | 2716 | 4.660 | 1 | 27/32 | 0.559 | 21/6 | 2.782 |
| RGA. | 7.25 | 639 | 7316 | 61/4 | 61/4 | 27/6 | 4.660 | 1 | 27/32 | 0.559 | $21 / 16$ | 2.782 |
| U6TB | 9.50 | ${ }^{69} 9$ | $6^{18}$ \% ${ }^{6}$ | 10\% | 71516 | 27/16 | 9.332 | 2 | 27/32 | 1.118 | 21/6 | 5.564 |
| Y6E. | 12.70 | 6 | ${ }^{6}$ | 71316 | 11916 | ${ }^{27} /{ }^{6}$ | 9.332 | 2 | 7í6 | 0.301 | 21/16 | 6.381 |
| Y6F. | 12.50 | 7 | 7 | 7 | ${ }^{931}$ | 29/6 | 10.314 | 2 | 1 | 1.571 | 2316 | 6.000 |
| Y6G. | 12.87 | 7 | 7516 | 7 | 91/2 | 2916 | 10.314 | 2 | 1 | 1.571 | 2316 | 6.000 |
| Y60. | 12.60 | 7 | 7 | 7 | 91/2 | 2916 | 10.314 | 2 | 1 | 1.571 | 23/16 | 6.000 |
| F7. | 19.80 | 612 | $81 / 2$ | 135\% | 911/16 | 211/6 | 22.691 | 4 | 7/6 | 3.937 | 21/4 | 11.967 |
| F7A. | 18.25 | 5\%8 | 71/6 | 157/16 | 9 | 21/16 | 22.691 | 4 | 716 | 1.079 | $21 / 4$ | 13.156 |
| F7B. | 24.50 | 0312 | $83 / 4$ | 135\% | 107/16 | 21116 | 22.691 | 4 | 1/2 | 4.500 | 214 | 11.404 |
| F7\% | 27.50 | 6312 | $81 / 2$ | 135\% | 105\% | ${ }^{211 / 16}$ | 22.691 | 4 | 1/2 | 4.500 | 214 | 11.404 |

Table A1－24．－Average Weights and Over－all Dimensions of Bendix－Stromberg Aircraft Carburetors．－

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Table A1-25.-Carburetor Flanges, Aircraft Types
S.A.E. Standard
(From S.A.E. "Handbook")


Single barrel (Table $a$ )


Single barrel (Table b)



Flange Thickness
All types of flange shall be of the following thickness.

Flange Thickness, In.
Stud Size
5/16
1/4 3/8
5/16
3/8 . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 13/32

Table A1-25.-Carburetor Flanges, Aircraft Types.-(Continued) Table $a$. Four- and Eight-bolt Flanges

| Nominal size |  | A | $B$ | D | $F$ | $H^{*}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| . |  |  |  |  |  |  |
| No. | Diam. |  |  |  |  |  |
| 2 | 11/4 | 1716 | 134 | 25/16 | 9/32 |  |
| 3 | 152 | 11116 | 11516 | 23/2 | 9/32 |  |
| 4 | 13/4 | 11516 | 23/16 | $23 / 4$ | 9/32 | 48/8 |
| 5 | 2 | 23/16 | 213/32 | 31/32 | 11/32 | 47/8 |
| 6 | 21/4 | 2716 | $21 / 2$ | 33/16 | 13/32 | 51/8 |
| 7 | 21/2 | 21116 | $23 / 4$ | 3716 | 11/32 | 51/2 |
| 8 | 23/4 | 215/16 | 3 | 311/6 | 11/32 | 5\%/6 |
| 9 | 3 | 3316 | 33/16 | 4.4 | 13/32 |  |
| $10^{1}$ | 31/4 | 37/16 | 3716 | 4314 | 13/32 | 65/16 |

* For double-barrel eight-bolt flange type only.

Table $b$. Single-barrel Four-bolt Flange

| Nominal size |  | A | $B$ | $F$ | $R$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Diam. |  |  |  |  |
| 10 | 314 | 3716 | 3888 | 13/82 | 21/8 |
| 11 | $31 / 2$ | 31116 | 3122 | 13/32 | 21/4 |
| 12 | 38/4 | 3156 | 33/4 | 13/82 | 23/8 |
| 13 | 4 | 43/6 | 4 | 13/32 | 21/2 |

Table c. Double-barrel Four-bolt Flange

| Nominal size |  | A | B | $C$ | D | $E$ | Tap | $G$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Diam. |  |  |  |  |  |  |  |
| 4 | 13/4 | 11516 | 338 | 23/16 | 11/4 | - $9 / 32$ | 7/16-14 | 13/32 |
| 5 | 2 | 23/16 | 33/8 | 2716 | 13/8 | 932 | 7/6-14 | 13/32 |
| 6 | 21/4 | 271́6 | 35/8 | 2136 | 1120 | 932 | 7/16-14 | 15/32 |
| 7 | 21/2 | 211/16 | 4 | $2^{1516}$ | 121/92 | - 932 | 7in-14 | 15/32 |
| 8 | 23\% | 21518 | 434 | 33/6 | 12532 | 932 | 7íg-14 | 17/32 |

Table A1-25.-Carburetor Flanges, Aircraft Types.-(Continued) Table $d$. Double-barrel Six-bolt Flange

| Nominal size |  | - $\boldsymbol{A}$ | $B$ | $C$ | D | $E$ | $F$ | ${ }^{\prime} \cdot$ | H |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Diam. |  |  |  |  |  |  |  |  |
| 7 | 21/2 | 21.16 | 21316 | 215/16 | 65/8 | 311/16 | 13/22 | 7/16 | 27/8 |
| 8 | 23/4 | 215/16 | 3 | 3316 | 7116 | 37\% | 11/32 | 716 | 33/32 |
| 9 | 3 | 3316 | 3316 | 3716 | 7916. | 4188 | 13/32 | 15/32 | 35/6 |
| 10 | 314 | 37/16 | 3716 | 31116 | 81/6 | 43\% | 13/32 | 15/32 | 3916 |
| 11 | 3312 | 31116 | $3{ }^{1116}$ | $315 / 16$ | $89 / 16$ | 45゙8 | 13/32 | 15/32 | 313/16 |
| 12 | $33 / 4$ | 31516 | 315/16 | 4316 | 9118 | 47/8, | 13/32 | 15/32 | 4116 |

Table e. Triple-barrel Eight-bolt Flange

| Nominal size |  | A | $B$ | D | $E$ | $F$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. | Diam. |  |  |  |  |  |
| 3 | 11/2 | 111/6 | 11516 | 63/8 | 21/2 | 9/32 |
| 4 | 13/4 | 115/16 | 2316 | 71/8 | 23/4 | 9/32 |
| 5 | 2 . | 2316 | 2716 | 8 | 31\% | $11 / 32$ |

(Conforms substantially with AN Standard.)
Aircraft Engine Division report adopted by the Society, January, 1932.
Table A1-26.-Pesco Fuel-pump Characteristics
(From Pump Engineering Service Corporation)


Table A1-27.-Fuel-pump Mountings, Aircraft-engine Pads S.A.E. Standard
(From S.A.E. "Handbook")


Fig. 1.-Square-type pad. (Conforms substantially with AN Standard, March, 1939.)


Fig. 2.-Old-type pad (August, 1928). (Conforms substantially with AN Standard, January, 1937.)
Report of Aeronautic Division adopted by the Society, August, 1928. Last revision by Aircraft Engine Division, January, 1940.

Table A1-28.-Magneto Selection
Note: The following data should be used for preliminary selections only, and final approval of the selection should be obtained from the manufacturer prior to the starting of construction of the engine.

| Number of cylinders | Arrangement | Scintilla magneto type | Ratio magneto to engine speed $\dagger$ | Magneto rotation* | $\begin{aligned} & \text { Mounting } \\ & \text { flange } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | Opposed | SF4R-8 | 1-1 | Clockwise | S.A.E. 2-bolt flanged type |
| 4 | In-line | SF4R-8 | 1-1 | Clockwise | S.A.E. 2-bolt flanged type |
| 5 | Radial | SF5L-8 | 1.25-1 | Counterclockwise | S.A.E. 2-bolt flanged type |
| 6 | In-line | SF6L-8 | 1.5-1 | Counterclockwise | S.A.E. 2-bolt flanged type |
| 7 | Radial | SF7R-1 | 0.875-1 | 1 each | S.A.E. 3-bolt flange single tyंpe |
| 9 | Radial | SF9L-4 | 1.125-1 | 1 each | S.A.E. 3-bolt flange single type |
| 14 | $\left\lvert\, \begin{aligned} & \text { 2-row ra- } \\ & \text { dial } \end{aligned}\right.$ | SF14L-3 | 0.875-1 | 1 each | S.A.E. 3-bolt flange single type |

[^35]Table A1-29.-S.A.E. Magneto Mounting-flange Data (From S.A.E. "Handbook")


Two-bolt flange, single type (commercial engines to and including six cylinders).


Three-bolt flange, single type (standard flange and drive).
[Conforms substantially with current AN Standard (January, 1941) except bolt slots are wider so $3 / 8-\mathrm{in}$. studs can be used on larger size engines, and flange thickness is larger to allow a standard length of engine studs.]

## Table A1-30.-Aircraft-engine Starters <br> (From Eclipse Aviation Corporation)

Note: The selection should be confirmed by the starter manufacturer prior to final approval of the engine design.

| Type | Description | $\begin{aligned} & \text { Mounting } \\ & \text { flange } \end{aligned}$ | Hand crank available | Weight, lb. | Max. capacity, hp . | $\begin{aligned} & \text { Volt- } \\ & \text { age } \end{aligned}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Inertia |  |  |  |  |  |  |
| Series 6. | Concentric, hand starter | S.A.E.-6" | Yes | 1814 | 400 |  |
| Series 6. | Concentric, hand and electric | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 301/4 | 400 | 12 |
| Series 6. | Concentric, hand and electric | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 301/4 | 400 | 24 |
| Series 6. | Concentric, hand with integral booster magneto | S.A.E.-6" | Yes | 261/2 | 400 |  |
| Series 7... | Vertical, hand starter | S.A.E.-6' ${ }^{\prime \prime}$ | Yes | 31 | 900 |  |
| Series 7. | Vertical, hand and electric | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 391/2 | 900 | 12 |
| Series 7. | Vertical, hand and electric | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 391/2 | 900 | 24 |
| Series 7A. . . | Vertical, hand starter | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 341/2 | 1,000 |  |
| Series 7A. | Vertical, hand and electric | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 43 | 1,000 | 12 |
| Series 7A. | Vertical, hand and electric | S.A.E. ${ }^{\prime \prime}{ }^{\prime \prime}$ | Yes | 43 | 1,000 | 24 |
| Series 11. | Concentric, hand starter | S.A.E.-6' ${ }^{\prime \prime}$ | Yes | 21 | 900 |  |
| Series 11.... | Concentric, hand and electric | S.A.E.-6" ${ }^{\prime \prime}$ | Yes | 343/4 | 900 | 12 |
| Series 11. | Concentric, hand and electric | S.A.E.-6' ${ }^{\prime \prime}$ | Yes | 343/4 | 900 | 24 |
| Series 11.... | Concentric, hand with integral booster magneto | S.A.E.-6' ${ }^{\prime \prime}$ | Yes | 283/4 | 900 |  |
| Series 11A.. | Concentric, hand starter | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 25 | 1,000 |  |
| Series 11A.. | Concentric, hand and electric | S.A.E.- $0^{\prime \prime}$ | Yes | 383/4 | 1,000 | 12 |
| Series 11A.. | Concentric, hand and electric | S.A.E. ${ }^{\prime \prime \prime}{ }^{\prime \prime}$ | Yes | 383/4 | 1,000 | 24 |
| Series 16. | Concentric, hand starter | S.A.E. $6^{\prime \prime}$ | Yes | 21 | 350 |  |
| Direct-cranking Electric |  |  |  |  |  |  |
| Y150....... | Vertical, starter | S.A.E.-5 $5^{\prime \prime}$ | No | 161/4 | 150 | 12 |
| E80 | Concentric, starter | S.A.E. $5^{\prime \prime}$ | No | 19 | 250 | 12 |
| E80. | Concentric, starter | S.A.E.-6 ${ }^{\prime \prime}$ | No | 19 | 250 | 12 |
| F141 | Concentric, starter | S.A.E.-6 ${ }^{\prime \prime}$ | No | 241/2 | 400 | 12 |
| E160. | Concentric, starter | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 321/4 | 900 | 12 |
| E160. | Concentric, starter | S.A.E. 6 $^{\prime \prime}$ | Yes | 321/4 | 1,000 | 24 |
| Hand-turning Gear |  |  |  |  |  |  |
| $4 \mathrm{H4}$. | 4:1 ratio H.T.G. | S.A.E.-5 ${ }^{\prime \prime}$ | Yes | 81/2 | 115 |  |
| BH6. | 6:1 ratio H.T.G. | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 12 | 250 |  |
| 3HB6. | 6:1 ratio H.T.G. with integral booster magneto | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 17 | 250 |  |
| 3 H 8. | 8:1 ratio H.T.G........... | S.A.D.-6' ${ }^{\prime \prime}$ | Yes | 12 | 300 |  |
| $3 \mathrm{HB8} 8$. | 8:1 ratio H.T.G. with booster magneto | S.A.E.-6' ${ }^{\prime \prime}$ | Yes | 17 | 300 |  |
| 3H18. | 18:1 ratio H.T.G. | S.A.E.-6 ${ }^{\prime \prime}$ | Yes | 171/2 | 300 |  |
| Combustion |  |  |  |  |  |  |
| Type I. | Concentric-starter. | S.A.E. $6^{\prime \prime}$ | No | 25 | 550 |  |
| Type II. | Concentric-starter | S.A.E. ${ }^{6 \prime \prime}$ | No | 32 | 1,250 |  |

## Table A1-30.-Aircraft-engine Starters.-(Continued)

## Air Injection

Air-injection starter installations normally require the following component units:

1. Main-engine-driven compressor (weight and mounting depends upon make of engine on which installed).
2. Air-storage tank (standard sizes of tanks 6 in. diameter by 20 in. long and 6 in . diameter by 26 in . long).
3. Air-pressure regulating valve.
4. Air-pressure release valve.
5. Air-pressure gage.
6. Primer.
7. Cylinder injector fittings (one furnished for each cylinder).


#### Abstract

Notes to Air Injection.-Item 1. Compressor will differ depending upon the make of engine on which it is to be installed.

Item 2. Air-storage tank, unless otherwise specified is furnished in the 6- by $20-\mathrm{in}$. size. Items 3 to 7 inclusive are normally common to all installations. The valves covered by items 3 and 4 are furnished assembled in a fully charged tank (item 2) ready for installation and use.


Weight.-The weight of the air-injector starting equipment installed is approximately 32 lb . for a single-motor application, this weight depending upon the peculiarities of each installation in respect to tubing and fittings required, tank size, etc.

Capacity.-The air-injector starting equipment is recommended for sparkignition engines of five or more cylinders and rated up to 250 hp .

Notes to Table.
Mounting Flanges.-See Table A1-31 for dimensional details of the S.A.E. 5 in . and S.A.E. 6 in. diameter engine-starter mounting.

Important.-All cartridge starters incorporate a special 12-tooth engaging jaw requiring a similar engaging member on the engine.

Weights.-a. All weights on hand and electric inertia starters include a suitable solenoid relay for the accelerating motor, which is mounted on and connected electrically to the starter.
b. The weights given above on all starters do not include the required hand crank and cranking extension which unless otherwise specified are furnished with all starters providing manual operation.
c. Weights on all electrically operated starters do not include shielding.
d. Weights listed under Combustion starters include all component parts with standard lengths of intake and exhaust tubings with fittings.

Capacity. -The maximum engine horsepower for which any type starter is recommended is approximate and based upon an average installation on a four-cycle spark-ignition engine of conventional design, operating under normal conditions. Factors other than horsepower ratings must be considered in selecting the proper capacity or type starter for a particular engine. It is therefore recommended that unless reliable data are available, and for initial installations, that the manufacturer be consulted so that an analysis of the requirements can be made and definite recommendations submitted.

## Table A1-30.-Atrcraft-engine Starters.-(Continued)

Voltage.- $a$. All electrically operated starters can be furnished either grounded or ungrounded and shielded or unshielded. Unless otherwise specified, electrically operated starters are furnished as grounded unshielded units. The application of shielding to the various type starters listed above will increase the listed weights as follows:

|  | Grounded | Ungrounded |
| :---: | :---: | :---: |
| Inertia. | $1 / 4 \mathrm{lb}$. | $5 / 16 \mathrm{lb}$. |
| Direct-cranking electric | $1 / 16 \mathrm{lb}$. | $1 / 8 \mathrm{lb}$. |

b. The fixing-control switch of the combustion starters and the electric connection at the loading breech incorporates threaded shielding outlets.
c. Integral booster magnetos furnished on series 6 and series 11 inertia starters incorporate threaded shielding at the electrical outlets.

Table A1-31.-Starting-motor Mountings, Aircraft-engine Pads

> S.A.E. Standard
(From S.A.E. "Handbook")


Fig. 1.-Three-jaw-clutch development. Fig. 2.-Twelve-jaw-clutch development at 2.375 in . diameter.

Starter Mounting and Clutch Dimensions

| Starter size | Clutch jaws | A | $\begin{gathered} B \\ \pm 0.005 \end{gathered}$ | $\left\|\begin{array}{c} C \\ +0.003 \\ -0.000 \end{array}\right\|$ | D | Clearance |  | $\begin{gathered} F \\ \text { studs } \end{gathered}$ | $G$ | H | $J$ | $\begin{gathered} K \\ \text { drill } \end{gathered}$ | $L$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  | $E$ | $E^{\prime}$ |  |  |  |  |  |  |
| Small. | 3 | 5.000 | 4.000 | 3.000 | 2.250 | 3.000 | 1.625 | 516-24 | 0.813 | 0.625 |  |  | 1.000 |
| Medium | 3 or | 6.000 | 5.000 | 4.125 | 2.250 | 4.125 | 1.500 | 38-24 | 0.938 | 0.813 | 0.125 | \#36 | $\begin{gathered} 1.688 \\ \max . \end{gathered}$ |
|  | 12 |  |  |  |  |  |  | 7/16-20 | 1.063 | 0.813 | 0.125 | \#36 | 1.688 |
| Large. | $\begin{gathered} 3 \text { or } \\ 12 \end{gathered}$ | 7.000 | 5.750 | 4.625 | 3.250 | 4.625 | 1.500 | /16-20 | 1.063 | 0. |  | (0.106) | max. |

Stud threads to be American Standard Fine (NF).
(Conforms substantially with AN Standard, March, 1939.)
Report of Aeronautic Division adopted by the Society, Augast, 1928. Last revision by Aircraft Engine Division, March, 1939.

Table A1-32.-Single-voltage Generators
(From Eclipse Aviation Corporation)
Note: The selection should be confirmed by the generator manufacturer prior to final approval of the engine design.

Ratings

| Type | Volts | Amperes | Watts | Weight, lb. | Mounting pad |
| :---: | :---: | :---: | :---: | :---: | :---: |
| AL-1 (3d brush) | 15 | 15 | 225 | 173/4 | 4-bolt type |
| $G$. | 15 | 15 | 225 | 153/4 | 4-bolt type |
| D. | 15 | 25 | 375 | 211/4 | 4-bolt type |
| $E$. | 15 | 50 | 750 | 311/4 | 4-bolt type |
| DG-4. | 30 | 10 | 300 | 21 |  |
| E. | 30 | 20 | 600 | 311/4 | 4-bolt type |

Permanent mount control box (3 unit for 15 - or 30 -volt operation). $41 / 2 \mathrm{lb}$. Permanent mount control box ( 2 unit for 15 -volt operation)....... $21 / 4 \mathrm{lb}$. Permanent mount control box ( 2 unit for 3 d brush, generator)..... 2 lb . Quick detachable control box ( 3 unit for 15 - or 30 -volt operation).. 5 lb . Control panel (2 unit for 15-volt operation)......................... . . 3 lb . FB-5 filter unit (for 15- or 30-volt operation)....................... . . 4 lb.

Note: The preceding rated outputs are obtained at a generator speed of 2,250 to 4,200 r.p.m. A minimum speed of 2,250 r.p.m. is readily obtainable at cruising speed from the generator drives of all standard types of aircraft engines, as the gearing to the drive shaft is normally at a ratio of $11 / 2$ times engine speed. The ratings given as 15 and 30 volts are the values required for operating with 12 - and 24 -volt battery systems, respectively. The foregoing weights include shielded terminal covers which are standard on all generators, control boxes, and filter unit. The covers are threaded for the attachment of metallic conduit for radio shielding.

Atrcraft Generator.Mountings S.A.E. Standard (From S.A.E. "Handbook")


Generator mounting pad, four-bolt type. (Conforms substantially with AN Standard, March, 1939.)

Table A1-33.-Tachometer Drive, Aircraft
S.A.E. Standard
(From S.A.E. "Handbook")
Drive for Mechanical Types


Engine connection.


Tachometer end of drive shaft.


Tachometer connection.


Note: Tachometer drives to rotate at half engine-crankshaft speed.
Report of the Aeronautic Division adopted by the Society, March, 1918. Last revision by the Aircraft Engine Division, January, 1939.
${ }^{1}$ S.A.E. Special Pitch thread, Class 3.


Fra. A1-1.-Wing-loading data for 54 American airplanes.


Frg. A1-2.-Mechanical efficiencies at full throttle. [(a) Ricardo, High Speed Internal Combustion Engines, p. 275; (b) Marks, The Airplane Engine, p. 24 (Liberty 12); (c) Judge, Automobile and Aircraft Engines, p. 410.]


Fia. A1-3.-Reciprocating-weight-cylinder-displacement data for 25 airplane engines.


Fig. A1-4.-Reciprocating-weight-cylinder-diameter data for 25 airplane engines.


Fig. A1-5.-Rotating weights per crankpin for radial engines.



Fra. A1-6.-S.A.E. propeller-shaft sizes vs. rated brake horsepower.


Frg. Al-7.-Cylinder cooling-fin dimensions from several current makes of aircraft engines.

lb. per sq.in.
FIG. A1-8.-Effect of mean gas velocity through inlet valve on rated b.m.e.pfor several nonsupercharged aircraft engines.

## APPENDIX 2

Table A2-1.-Correlation of Numbering Systems for Aluminum and Magneshum Alloys
(From Product Engineering, November 1940, and "Aluminum in Aircraft," 1941)

| Alloy trade designation | Federal | Army | Navy | S.A.E. | A.S.T.M. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Aluminum Rolled Sheet (for Baffles, Cowling, Etc.) |  |  |  |  |  |
| 17 S 24 S | QQ-A-353 QQ-A-355 | Federal Federal | 47A3c 47 A 10 | 26 24 | B78-36T |
| Aluminum Sand Castings (for Cylinder Heads, Crankcases, Etc.) |  |  |  |  |  |
| 142 | QQ-A-601 | AN-QQ-A-379 | AN-QQ-A-379 | 39 | B26-37T |
| 355 | QQ-A-60i | AN-QQ-A-376 | AN-QQ-A-376 | 322 | B26-37T |
| A355 | QQ-A-601 | Federal | $\begin{aligned} & \text { M212a } \\ & (8-24-34) \end{aligned}$ |  |  |
| 195 | QQ-A-601 | AN-QQ-A-390 | AN-QQ-A-390 | 38 | B26-37T |
| Aluminum Permanent-mold Castings (for Pistons, Rocker Box Covers, Etc.) |  |  |  |  |  |
| 122 | QQ-A-596 | . . . . . . . . . ${ }^{\text {a }}$. | 46A15 | 34 | B108-38T |
| A132 | QQ-A-596 | AN-QQ-A-386 | AN-QQ-A-386 | 321 | B108-38T |
| 355 | QQ-A-596 |  | $46 \mathrm{Al}{ }^{5}$ | 322 |  |
| Aluminum Forgings (for Pistons, Crankcases, Connecting Rods, Impellers, Etc.) |  |  |  |  |  |
| 14 S | QQ-A-367a | Federal | 46A7b |  | - |
| 18 S | QQ-A-367a | Federal | 46A7b |  |  |
| 25 S | QQ-A-367a | Federal | 46 A 7 b | 27 |  |
| 32S | QQ-A-367a | Federal | 46A7b |  |  |
| A51S | QQ-A-367a | Federal | 46 A 7 b | 280 |  |
| Magnesium Sand- and Permanent-mold Castings <br> For (AM 240) Cover Plates, Valve Covers <br> (AM 260) Accessory Drive Housings <br> (AM 265) Crankcases |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
|  |  |  |  |  |  |
| 4 |  |  |  |  |  |
| AM240 or G |  |  |  | $\cdots$ | B80-36T |
| AM260 |  |  | M-112g | $\ldots$ | B80-361 |
|  |  |  | (3-15-40) |  |  |
| AM265 or H |  | 57-74-1C | $\begin{aligned} & \mathrm{M}-112 \mathrm{~g} \\ & (3-15-40) \end{aligned}$ | . $\cdot$ | 1380-36T |

NOTE: See references for other alloys.

Table A2-2.-Nominal Composition of Aluminum and Magnesium Alloys*

| Alloy designation | Per cent of alloying elements, aluminum and normal impurities constitute the remainder |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Copper | Iron | Silicon | Chromium | Magnesium | Nickel | Manga- nese |
| Aluminum Sand-casting Alloys |  |  |  |  |  |  |  |
| 142 | 4.0 | ... | . . . | $\ldots$ | 1.5 | 2.0 |  |
| 195 | 4.0 |  |  |  |  |  |  |
| 355 | 1.3 | $\ldots$ | 5.0 |  | 0.5 |  |  |
| A355 | 1.4 |  | 5.0 |  | 0.5 | 0.8 | 0.8 |

Aluminum Permanent-mold-casting Alloys

| 122 | 10.0 | 1.2 | $\ldots$ | $\ldots$ | 0.2 |  |  |
| ---: | ---: | ---: | ---: | :--- | :--- | :--- | :--- |
| A132 | 0.8 | 0.8 | 12.0 | $\ldots$ | 1.0 | 2.5 |  |
| 355 | 1.3 | $\ldots$ | 5.0 | $\ldots$ | 0.5 |  |  |

Aluminum Wrought Alloys

| 14 S | 4.4 | $\ldots$ | 0.8 | $\ldots$ | 0.4 | $\ldots$ | 0.8 |
| ---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 17 S | 4.0 | $\ldots$ | $\ldots$ | $\ldots$ | 0.5 | $\ldots$ | 0.5 |
| 18 S | 4.0 | $\ldots$ | $\ldots$ | $\ldots$ | 0.5 | 2.0 |  |
| 24 S | 4.5 | $\ldots$ | $\ldots$. | $\ldots$ | 1.5 | $\ldots$ | 0.6 |
| 25 S | 4.5 | $\ldots$ | 0.8 | $\ldots$ | $\ldots$ | $\ldots$ | 0.8 |
| 32 S | 0.9 | $\ldots$ | 12.5 | $\ldots$ | 1.0 | 0.9 |  |
| A51S | $\cdots$ | $\ldots$ | 1.0 | 0.25 | 0.6 |  |  |


|  | Per cent of alloying constituents, magnesium constitutes |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| the remainder |  |  |  |  |  |
| Alloy <br> designa- <br> tion | Aluminum |  |  |  | Manga- <br> nese |
|  | Zinc | Silicon | Total <br> impurities |  |  |

Magnesium Sand- and Permanent-mold-casting Alloys

| AM240 | $9.0-11.0$ | $0.10 \min$. | $0.3 \max$. | $0.5 \max$. | 0.3 max. |
| :--- | :--- | :--- | :--- | :--- | :--- |
| AM260 | $8.75-9.25$ | 0.10 min. | $1.8-2.2$ | 0.3 max. | 0.3 max. |
| AM265 | $5.3-6.7$ | 0.15 min. | $2.5-3.5$ | 0.5 max. | 0.3 max. |

[^36]
## Table A2-3.-Physical Constants of Aluminum and <br> Magnesium Alloys

(From "Alcoa Aluminum and Its Alloys," and "Mazlo Magnesium Alloys")

| Alloy designation | Density, lb. per cu. in. | Thermal* conductivity at $100^{\circ} \mathrm{C}$., c.g.s. units | Average coefficients of thermal expansion per deg. $F$. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $68-212^{\circ} \mathrm{F}$. | $68-392^{\circ} \mathrm{F}$. | $68-572^{\circ} \mathrm{F}$. |
| Aluminum Sand-casting Alloys |  |  |  |  |  |
| 142 | 0.099 | 0.35 | 0.0000125 | 0.0000130 | 0.0000136 |
| 195 | 0.100 | 0.34 | 0.0000127 | 0.0000133 | 0.0000138 |
| 355 | 0.097 | 0.33 | 0.0000122 | 0.0000127 | 0.0000133 |
| A355 | 0.098 | 0.31 | 0.0000119 | 0.0000125 | 0.0000130 |
| Aluminum Permanent-mold-casting Alloys |  |  |  |  |  |
| 122 | 0.103 | 0.31 | 0.0000122 | 0.0000127 | 0.0000130 |
| A132 | 0.097 |  | 0.0000105 | 0.0000111 | 0.0000116 |
| 355 | 0.097 | 0.33 | 0.0000122 | 0.0000127 | 0.0000133 |
| Aluminum Wrought Alloys |  |  |  |  |  |
| 14 S | 0.101 | 0.37 | 0.0000122 | 0.0000130 | 0.0000138 |
| 17 S | 0.101 | 0.28 | 0.0000122 | 0.0000130 | 0.0000138 |
| 18S | 0.101 | 0.37 | 0.0000122 | 0.0000130 | 0.0000138 |
| 24 S | 0.100 | 0.28 | 0.0000122 | 0.0000130 | 0.0000138 |
| 25 S | 0.101 | 0.37 | 0.0000122 | 0.0000130 | 0.0000138 |
| 32S | 0.097 | 0.32 | 0.0000108 | 0.0000114 | 0.0000119 |
| A51S | 0.097 | 0.41 | 0.0000130 | 0.0000136 | 0.0000141 |
| Magnesium Sand and Permanent-mold Castings |  |  |  |  |  |
| AM240 | 0.066 | 0.17 | Mean coefficient of thermal expansion ( 65 to $750^{\circ} \mathrm{F}$.) per deg. F . $=0.000016$ for these magnesium alloys |  |  |
| AM260 |  |  |  |  |  |
| AM265 | 0.066 | $\begin{aligned} & 0.18 \\ & \text { approx. } \end{aligned}$ |  |  |  |

[^37]
## Table A2－4．－Mechanical Properties of Aluminum and Magnesium Alloys ${ }^{1}$

（From＂Alcoa Aluminum and Its Alloys＂and＂Mazlo Magnesium Alloys＂）

| Alloy <br> designation | Min． for | alues ecs． | Typical values（not guaranteed） |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Tension ${ }^{2}$ |  | Tension ${ }^{2}$ |  |  | Com－ pres－ sion ${ }^{3}$ |  |  | Fa － tigue ${ }^{5}$ | Den－ sity |
|  |  |  |  |  |  |  |  |  |  |  |
| Aluminum Sand－casting Alloys |  |  |  |  |  |  |  |  |  |  |
| 142－T61 | 32，000 | 4 | 32，000 | 37，000 | 0.5 | 47，000 | 100 | 32，000 | 8，000 | 0.099 |
| 195－T6 | 32，000 | 3.0 | 22，000 | 36，000 | 5.0 | 25，000 | 80 | 30，000 | 6，500 | 0.100 |
| 355－T6 | 32，000 | 2.0 | 25，000 | 35，000 | 3.5 | 29，000 | 80 | 30，000 | 8，500 | 0.097 |
| A355－T51 | 25，000 | 4 | 24，000 | 28，000 | 1.5 | 24，000 | 65 | 22，000 | 8，500 | 0.099 |
| Aluminum Permanent－mold－casting Alloys |  |  |  |  |  |  |  |  |  |  |
| 122－T551 | 30，000 | 4 | 35，000 | 37，000 | 0.0 | 40，000 | 115 | 27，000 | 8，500 | 0.104 |
| A 132－T551 | 31，000 | 4 | 28，000 | 36，000 | 0.5 | 30，000 | 105 | 24，000 |  | 0.097 |
| 355－T6 | 37，000 | 1.5 | ［26，000 | 43，000｜ | 4.0 | 26，000 | 90 | 130，000 |  | 0．097 |

Magnesium Sand－and Permanent－mold－casting Alloys

| AM240－T4 | 29,000 | 6.0 | 12,000 | 35,000 | 9.0 | $\cdots$ |  | 52 | 20,000 | 11,000 |
| :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| 0.066 |  |  |  |  |  |  |  |  |  |  |
| AM240－T6 | 29,000 | 2.0 | 16,000 | 35,000 | 4.0 | $\cdots \cdots$ | 60 | 21,000 | 8,000 |  |
| AM260－T4 | 30,000 | 6.0 | 14,000 | 39,000 | 10.0 | $\cdots \cdots$ | 63 | 20,000 | 9,000 |  |
| AM265－T4 | 30,000 | 6.0 | 12,000 | 37,000 | 9.0 | $\cdots \cdots$ | 51 | 18,000 | 11,000 | 0.066 |

Aluminum Forging Alloys ${ }^{\text {s．7 }}$

${ }^{1}$ See references for additional data．
2 Tension and hardness values determined from standard $3,2-\mathrm{in}$ ．diameter test specimens．
${ }^{3}$ Results of tests on specimens having an $L / R$ ratio of 12.
${ }_{4}$ Not specified．The error in determining low elongations is comparable with the value being measured．
${ }^{5}$ Endurance limits are based on $500,000,000$ reversals．
－Properties for aluminum forging alloys apply to forgings up to 4 in ．in diameter or thickness．Long axis of test specimens taken parallel to direction of grain flow．
${ }^{7}$ Yield and hardness data on aluminum forging alloys are minimum specification values．
Modulus of elasticity for aluminum alloys， $10,300,000 \mathrm{lb}$ ．per sq．in．
Modulus of elasticity for magnesium alloys， $6,500,000 \mathrm{lb}$ ．per sq．in．

Table A2-5.-Typical Tensile Properties of Aluminum and
Magnesium Ahloys at Elevated Temperatures (From "Alcoa Aluminum and Its Alloys" and "Mazlo Magnesium Alloys")


Table A2-6.-S.A.E. Steel Numbering System<br>S.A.E. Standard

(From S.A.E. "Handbook")
Compositions that do not conform to the S.A.E. compositions, or that are not included in the S.A.E. Standard, should not bear the prefix "S.A.E."
(Note: For detailed data on chemical composition, grain-size charts, heat-treatments, hardness tests, magnaflux data, physical properties, etc., see Steel Specifications in S.A.E. "Handbook.")

A numeral index system is used to identify the compositions of the S.A.E. steels, which makes it possible to use numerals on shop drawings and blueprints that are partly descriptive of the composition of material covered by such numbers. The first digit indicates the type to which the steel belongs; thus " 1 -" indicates a carbon steel; " $2-$ " a nickel steel and " 3 -" a nickel chromium steel. In the case of the simple alloy steels, the second digit generally indicates the approximate percentage of the predominant alloying element. Usually the last two or three digits indicate the average carbon content in "points" or hundredths of 1 per cent. Thus " 2340 " indicates a nickel steel of approximately 3 per cent nickel ( 3.25 to 3.75 ) and 0.40 per cent carbon ( 0.35 to 0.45 ).

In some instances, in order to avoid confusion it has been found necessary to depart from this system of identifying the approximate alloy composition of a steel by varying the second and third digits of the number. An instance of such departure is the steel numbers selected for several of the corrosionand heat-resisting alloys.

The basic numerals for the various types of S.A.E. steel are as follows:

| Type of Steel | $\begin{aligned} & \text { Numerals } \\ & \text { (and Digits) } \end{aligned}$ |
| :---: | :---: |
| Carbon steels | 1xxx |
| Plain carbon | 10xx |
| Free cutting, (screw stock). | 11xx |
| Free cutting, manganese. | X13xx* |
| Manganese | 13xx |
| Nickel steels. | 2 xxx |
| 3.50 per cent nickel. | 23xx |
| 5.00 per cent nickel. | 25xx |
| Nickel chromium steels. | 3 xxx |
| 1.25 per cent nickel, 0.60 per cent chromium. | 31xx |
| 1.75 per cent nickel, 1.00 per cent chromium. | 32 xx |
| 3.50 per cent nickel, 1.50 per cent chromium. | 33 xx |
| 3.00 per cent nickel, 0.80 per cent chromium. | 34xx |
| Corrosion and heat-resisting steels. | 30 xxx |
| * The prefix " $X$ " is used in numerous instances to de elements. <br> Report on Iron and Steel Division adopted January, 191 | ons in the range <br> ision January, 194 |

Table A2-6.-S.A.E. Steel Numbering System.-(Continued)
Molybdenum steels. ..... 4 xxx
Chromium. ..... 41xx
Chromium-nickel ..... 43xx
Nickel ..... 46 xx and 48 xx
Chromium steels ..... 5xxx
Low-chromium ..... 51xx
Medium-chromium ..... 52xxx
Corrosion- and heat-resisting. ..... 51xxx
Chromium-vanadium steels. 6 xxx
Silicon-manganese steels ..... $9 x x x$
Table A2-7.-Main and Connecting-rod Bearings
S.A.E. Standard
(From S.A.E. "Handbook")

During the past few years, new materials for high-duty bearings have been. developed which it is believed are now sufficiently stabilized for standardization. Accordingly, the previous specifications have been revised, new ones added, and all grouped under the heading main and connecting-rod bearings.

The choice of the material to use for main and connecting-rod bearings depends upon a number of factors. The resistance to fatigue of bearing materials depends to a great extent upon the design of the bearing, the strength and rigidity of the supporting structure, the thickness of the backing metal (steel or bronze), the thickness of the bearing material, and the physical properties of the bond between the bearing material and the backing. The resistance to corrosion depends upon the chemical composition and characteristics of both lubricant and bearing alloy and upon temperature and other operating conditions.

The S.A.E. tin- and lead-base babbitts have nonscoring and nonwearing properties and are resistant to corrosion from organic acidity of the type normal to lubricating oil, but they are low in resistance to fatigue. Copperlead bearings are inferior to tin- and lead-base babbitts in nonscoring but they are greatly superior in resistance to fatigue. Cadmium bearings may approach the tin- or lead-base babbitts in nonscoring and the copper-lead bearings in resistance to fatigue, depending upon design and operating conditions. However, the S.A.E. copper-lead and the S.A.E. cadmium bearings may corrode if operated at sufficiently high temperatures using lubricants containing animal or vegetable oil additions or using mineral oils which develop acidic compounds on oxidation. Numerous satisfactory applications of these two alloys are made in cases where such acidity is not present and does not develop in service.

Many other alloys are sometimes used for main and connecting-rod bearings, depending upon design and operating conditions. Reference should be made to the S.A.E. brass, bronze and copper-alloy specifications for data in regard to the composition and properties of these other bearing materials.

Table A2-7.-Main and Connecting-rod Bearings.-(Continued)
The analysis of finished bearings shall be made from a sample taken between the bearing surface and a point midway between the bearing surface and the bonding material.

Babbitt Metals

| Composition in percentage | S.A.E. 10 |  | S.A.E. 110 |  | S.A.E. 11 |  | S.A.E. 13 |  | S.A.E. 14 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bearing | Ingot | Bearing | Ingot | Bearing | Ingot | Bearing | Ingot | Bearing | Ingot |
| Tin, min. | 90.0 | 90.75 | 87.75 | 89.0 | 86.0 | 87.25 | 4.5- | 4.75- | 9.25- | 9.75 |
|  |  |  |  |  |  |  | 5.5 | 5.25 | 10.75 | 10.25 |
| Antimony | 4.0- | 4.25- | 7.0- | 7.25- | 6.0- | 6.5- | $9.75-$ | 9.75- | 14.0- | 14.75- |
|  | 5.0 | 4.75 | 8.5 | 8.25 | 7.5 | 7.0 | 10.75 | 10.25 | 16.0 | 15.25 |
| Lead, max. | 0.35* | 0.35 | 0.35* | 0.35 | 0.35 | 0.35 | 86.0 | 85.5 | 76.0 | 75.25 |
| Copper, max. . | 4.0- | $4.25-$ | 2.25- | 2.5- | 5.0- | 5.5- | 0.50 | 0.50 | 0.50 | 0.50 |
|  | 5.0 | 4.75 | 3.75 | 3.5 | 6.5 | 6.0 |  |  |  |  |
| Iron, max.. | 0.08 | 0.08 | 0.08 | 0.08 | 0.08 | 0.08 |  |  |  |  |
| Arsenic, max... | 0.10 | 0.10 | 0.10 | 0.10 | 0.10 | 0.10 | 0.60 | 0.60 | 0.60 | 0.60 |
| Bismuth, max.. | 0.08 | 0.08 | 0.08 | 0.08 | 0.08 | 0.08 |  |  |  |  |
| Zinc and aluminum.......... | None | None | None | None | None | None | None | None | None | None |

* A maximum of 0.60 per cent lead is permissible in finished-steel or bronze-backed bearings provided a lead-tin solder has been used in bonding the bearing material to the backing metal.

Typical compositions of a rolled-bronze split bushing and a composite cast alloy on a steel back are as follows:

| Composition in percentage | S.A.E. 791 <br> - rolled or wrought | S.A.E. 792 cast lining |
| :---: | :---: | :---: |
| Copper. | 86.0-88.0 | 78.0-82.0 |
| Tin. | 3.50-4.50 | 9.0-11.0 |
| Zinc | 3.00-5.00 |  |
| Lead. | 3.50-4.50 | 9.0-11.0 |
| Iron, max. | 0.10 | 0.30 |
| Phosphorus, max. |  | 0.01 |
| Other impurities, max. | 0.20 | 0.30 |

S.A.E. 791 is a rolled split-bushing alloy and is similar in many of its properties to the cast alloy S.A.E. 40.

Table A2-7.-Main and Connecting-rod Bearings.-(Continued)
S.A.E. 792 is the cast-bronze liner for a rolled split bushing made with a steel backing, usually S.A.E. 1010 or S.A.E. 1015. This bronze is similar in many of its properties to the cast alloy S.A.E. 64.

## Graphite Bronze and Sintered Alloy Bearings

## General Information

Graphite bronze bearings may, in some installations, replace cast or wrought bearings. One type is a split bushing with indentations rolled into its inner surface which, in the case of graphite bearings, are filled under pressure with graphite paste. Four alloys are in general use as follows:

| Composition in percentage | Alloys |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | A | B | C | D |
| Copper. | 89.0-91.0 | Remainder | 65:5゙-68.5 | Remainder |
| Tin. | 0.25-0.75 | 3.5-4.5 |  | 4.0-6.0 |
| Lead. |  | 3.5-4.5 | 3.5-4.5 | 0.75-1.25 |
| Zinc.. | Remainder | 3.25-4.75 | Remainder | 0.35 max. |
| Iron, max. | 0.10 | 0.10 | 0.10 | 0.05 |
| Other impurities, max. | 0.20 | 0.20 | 0.20 |  |

The temper of the wrought strip metal used for these bushings is usually 1 to 3 Brown and Sharpe gage numbers hard, depending on the hardness specified by the purchaser.

The minimum Rockwell hardness of the finished bushing is 95 for alloy A, 90 for alloy B, and 80 for alloy C on the B scale, using a $1 / 8$-in. diameter ball and $100-\mathrm{kg}$. load.

The split graphite bronze bushings are used where the motion is oscillatory and not rotary, such as in rocker arms, steering knuckles and arms, and piston pins, and for starting motors, distributor shafts, and places where rotary speed is not high and unit load is low. They are also used on the chassis frame, in brake systems, etc.

Another type of graphite bronze bearing is made by molding into the desired shape mixtures of graphite with powdered metals or metallic compounds and heat-treating to effect alloying of the metallic ingredients. The bushings are then sized to definite finished dimensions, which results in a porous structure capable of absorbing appreciable quantitics of the lubricant and having graphite uniformly dispersed throughout the mass. These bushings can be manufactured in various porosities, densities, and load-carrying capacities, depending upon the use to which they are to be put. The porosity can be varied from practically zero to as high as 30 per cent by volume. These bushings are usually finished to the final dimensions and require no finish machining, but they must be properly supported.

Table A2-7.-Main and Connecting-rod Bearings.-(Continued) Other bearing materials, with or without graphite and having the properties of cast or wrought bearing alloys, may be made by the powder and sintering processes.

Report on Non-ferrous Metals Division adopted June, 1911. Last revision January, 1940.

$$
\begin{gathered}
\text { Table A2-8.-Brass and Bronze Castings Suitable for } \\
\text { Bushings, Etc. } \\
\text { (From S.A.E. "Handbook") }
\end{gathered}
$$

General Information. The following minimum properties should be attained from standard tension test specimens poured from this alloy in sand molds and tested without machining, provided that proper foundry practices are used.
Tensile strength, lb. per sq. in. ..... 30,000
Yield point, lb. per sq. in ..... 12,000
Elongation in 2 in . or proportionate gage length, per cent. ..... 10

Combining strength with fair machining qualities, this general utility bronze is especially good for bushings subject to heavy loads and severe working conditions.

Spec. No. 64-Phosphor-bronze Castings


General information. The following minimum properties should be attained from standard tension test specimens poured from this alloy in sand molds and tested without machining, provided that proper foundry practices are used.

Tensile strength, lb. per sq. in. . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 25,000
Yield point, lb. per sq. in 12,000
Elongation in 2 in . or proportionate gage length, per cent.

# Table A2-8.-Brass and Bronze Castings Stutable for Bushings, Etc.-(Continued) 

This metal is an excellent composition for use where antifraction qualities are desired standing up exceedingly well under heavy loads and severe usage.

This specification practically conforms in composition with ASTM B66-38.

Spec. No. 66-Bronze Backing for Lined Bearings
Composition
Copper.
83.00-86.00

Tin.
$4.50-6.00$
Lead
8.00-10.00

Zinc, max
2.00

Other impurities, max. . . . . . . . . . . . . . . . . . . . . 0.25
General Information. The following minimum properties should be attained from standard tension test specimens poured from this alloy in sand molds and tested without machining, provided that proper foundry practices are used.
Tensile strength, lb. per sq. in ..... 25,000
Yield point, lb. per sq. in ..... 12,000
Elongation in 2 in . or proportionate gage length, per cent. ..... 8

This composition is recommended as an inexpensive but suitable alloy for bronze-backed bearings.

## Spec. No. 660-Bronze Bearing Castings

| Composition | \% |
| :---: | :---: |
| Copper. | 81.00-85.00 |
| Tin. | 6.50-7.50 |
| Lead. | 6.00-8.00 |
| Zinc. | 2.00-4.00 |
| Iron, max. | 0.20 |
| Antimony, max | 0.20 |
| Aluminum. | None |
| Other impurities, max | 0.50 |

General Information. This alloy is one of the widely used compositions for bronze bearings. In the automotive industry, it is used extensively in applications such as spring bushings, torque-tube bushings, steering-knuckle bushings, piston-pin bushings, and washers.

The following minimum properties should be attained from standard tension test specimens poured in sand molds and tested without machining, provided that proper foundry practices are used.

## Table A2-8.-Brass and Bronze Castings Suitable for Bushings, Etc.-(Continued)

Tensile strength, lb. per sq. in.................. . . . . . . . . . . . . . . . . . . . 30,000
Yield point, lb. per sq. in...... . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . 14,000
Elongation in 2 in . or proportionate gage length, per cent......... 18
This alloy is essentially the same in chemical and physical properties as alloy No. 3B of ASTM B30-40T.

Note: For other brass, bronze, and copper alloys, see S.A.E. "Handbook."

Table A2-9.-Ferrous Metals Used in Engine Construction (From S.A.E. Jour., Vol. 40, No. 4, April, 1937)

| Chemical composition |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Carbon | Manga- nese | Silicon | Nickel | Chromium | Tungsten | Molybdenum | Vanadium | Other elements | S.A.E. No. or trade designation |
| 0.05 | 0.45 |  | . . . $\cdot$. | $\ldots$ | $\ldots$ | . . $\cdot$ | $\ldots$ | ........ | 1010 |
| 0.15 | 0.45 | . . . | . . . . |  | $\ldots$ |  | . . |  | 1015 |
| 0.20 | 0.45 | . . . | . . . . | . . . . | . . . | . . . | . . |  | 1020 |
| 0.35 | 0.65 |  |  |  | . . . |  | .. |  | 1035 |
| 0.50 | 0.65 | $\cdots$ | -... | . . . . $\cdot$ | $\cdots$ | $\cdots$ | $\cdots$ |  | 1050 |
| 0.90 | 0.35 | $\cdots$ | $\ldots$ | .... | $\ldots$ | $\ldots$ | $\ldots$ |  | 1090 |
| 0.95 | 0.35 | . . . | . . . . | . . . . | $\ldots$ | $\ldots$ |  |  | 1095 |
| 0.20 | 0.75 | $\ldots$ | - | . . . . | $\ldots$ | $\cdots$ | $\cdots$ | S-0.11 | 1120 |
| 0.30 | 0.65 |  | 3.50 |  |  |  | $\cdots$ |  | 2330 |
| 0.40 | 0.65 | $\cdots$ | 3.50 | . . . . |  | . . . | . . |  | 2340 |
| 0.15 | 0.45 | $\cdots$ | 1.25 | 0.60 | $\ldots$ | $\ldots$ | $\cdots$ | $\ldots . .$. | 3115 |
| 0.40 | . 0.75 | . . . | 1.25 | 0.80 |  | . . . | ... | . . . . . . . | X-3140 |
| 0.40 | 0.45 |  | 1.75 | 1.10 |  | $\ldots$ | . . |  | 3240 |
| 0.50 | 0.45 |  | 1.75 | 1.10 | $\ldots$ |  | .. |  | 3250 |
| 0.15 | 0.45 | $\cdots$ | 5.00 | . . . . | $\cdots$ | $\cdots$ | $\cdots$ |  | 2515 |
| 0.12 | 0.45 | $\cdots$ | 3.50 | 1.50 | $\ldots$ | $\cdots$ | $\ldots$ |  | 3312 |
| 0.30 | 0.50 | . . . | $\cdots$ | 0.95 |  | 0.2 | . . . |  | X-4130 |
| 0.40 | 0.65 | . . . | 1.75 | 0.70 | $\ldots$ | 0.35 | . . |  | 4340 |
| 1.0 | 0.30 | . . . | . . . . | 1.35 |  | ... | $\cdots$ |  | 52100 |
| 0.35 | 0.75 | . . . | $\ldots$ | 0.95 | $\ldots$ | $\cdots$ | 0.2 | . . . . . . | 6135 |
| 0.50 | 0.75 | $\ldots$ | $\ldots$. | 0.95 | $\ldots$ | $\cdots$ | 0.2 |  | 6150 |
| 0.90 | 0.35 | $\cdots$ |  | 0.90 |  | $\therefore \cdot$ | 0.2 |  | 6190 |
| 0.43 | 0.55 | $\ldots$ |  | 1.6 |  | 0.4 |  | Al. 1.2 | Nitralloy |
| 0.35 | 0.45 | $\ldots$ |  | 1.2 |  | 0.2 |  | Al. 1.2 | Nitralloy |
| 0.07* | 0.45 | $\ldots$ | 7.0* | 17* |  |  |  | Ti-0. 2 | 30905 |
| 0.60 | 0.3 | $\cdots$ |  | 3.5 | 13 | . | $\ldots$ |  | 71360 |
| 0.65 | 0.3 | $\ldots$ | $\cdots$ | 3.5 | 16 | .... |  |  | 71665 |
| 0.45 | 0.40 | 3.0 | . | 8.0 | . . . | 1.5 |  |  | Cr-Si-W |
| 0.30 | 0.30 | 2.50 | 8:0 | 12.5 | $\cdots$ | . . . |  |  | $\mathrm{Cr}-\mathrm{Ni}-\mathrm{Si}$ |
| 0.45 | 0.50 | 1.25 | 14.0 | 14.0 | 2.5 |  |  |  | Cr-Ni-W-Si |
| 1.20 | 0.50 | 1.2 | $\cdots$ | 18 | $\ldots$ | 0.6 |  |  | Cr-Si-Mo |
| 1.2 | 0.5 | 0.5 |  | 13 |  | 0.9 |  | Co-1. 3 | $\mathrm{Co}-\mathrm{Cr}$ |
| 1.0 | 0.5 | 1.5 | 0.6 | 13.5 | 3.5 | 0.6 |  |  | 13.5 Cr |

[^38]Table A2-9.-Ferrous Metals Used in Engine Construction.-
(Continued)

| Mechanical properties |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Tensile strength, lb. per sq. in. | Yield strength, lb. per sq. in. | Elongation 2 in. \% | Re-duction in area, \% | Application |
| 38,000 | 20,000- | 35 | .. | Ferrules, clips, lock wire |
| 45,000 | 25,000 | 22 |  | Camshaft, washers, ball ends |
| 55,000 | 36,000 | 22 | - | Nuts, screws, counterweights, flanges |
| 80,000 | 50,000 | 20 | - | Shafts, sleeves, nuts, rivets |
| 100,000 | 75,000 | 16 | . | Cylinder barrels, keys |
| 225,000 | 350,000 | -• | . | Springs |
| ........ | . . . . . . | $\cdots$ | $\cdots$ | Shims, wearing parts, valve mechanism |
| 55,000 |  | $\cdots$ | $\cdots$ | Screws, nuts, dowels for minor attachments |
| 125,000 | 100,000 | 15 | 50 | Bolts, studs, nuts, shafts |
| 135,000 | 110,000 | 15 | 50 | Connecting rods, gears |
| 130,000 | 90,000 | 16 | 40 | Gears, piston pins |
| 130,000 | 100,000 | 17 | 50 | Bolts, studs, shafts ${ }^{*}$ |
| 135,000 | 110,000 | 15 | 50 | Crankshaft, drive shafts |
| 225,000 | 200,000 | 10 | 40 | Gears, pins |
| 170,000 | 145,000 | 14 | 45 | Gears, cams, crankshaft |
| 160,000 | 135,000 | 15 | 50 | Gears, drive shafts, cams |
| 95,000 | 75,000 | 12 | . | Washers, shims, spacers, tubes |
| 160,000 | 140,000 | 15 | 50 | Crankshaft, connecting rods |
|  |  |  | - .. | Balls, bearings, knuckle pins |
| 150,000 | 120,000 | 15 | 50 | Gears, shafts, propeller hubs |
| 220,000 | 200,000 | 10 | $\cdots$ | Piston pins, gears, drive shafts, tappets, springs, ball ends, dowels, tappets, bolts, studs |
| 135,000 | 100,000 | 18 | 55 | Gears, cylinders |
| 120,000 | 80,000 | 15 | 45 | Piston pins, shafts, pump liners, bushings |
| 100,000 | 35,000 | 40 | . | Exhaust manifolds, supercharger casing |
| 55,000* |  | $\cdots$ | $\cdots$ | Valve, inlet |
| 60,000* |  | . | $\cdots$ | Valve, inlet tips |
| 50,000* |  | . | . | Valves, inlet |
| 60,000* |  | .. | $\ldots$ | Valves, inlet |
| 80,000* |  | $\cdots$ | . | Valves, inlet and exhaust, supercharger buckets |
| 50,000* |  | . | . | Valves, inlet and exhaust |
| 60,000* |  |  | . | Valves, exhaust |
| 50,000* |  | $\cdots$ | . | Valves, exhaust |

* Tensile strength at $1200^{\circ} \mathrm{F}$. All other tensile properties are typieal specification values.

Table A2－10．－Nonferrous Metals Used in Engine Construction （From S．A．E．Jour．，Vol．40，No．4，April，1937）

|  | Chemical composition |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & \text { 着 } \\ & \text { 若 } \\ & \text { 品 } \end{aligned}$ | $\begin{aligned} & \text { प̈ } \\ & 0.0 \\ & 0 \\ & 0 \end{aligned}$ | 药. | 哭 | $\begin{gathered} \vec{W} \\ \stackrel{W}{H} \end{gathered}$ |  | 를 | $\begin{aligned} & \text { 豆 } \\ & \text { 考 } \\ & \hline \end{aligned}$ |  | $\begin{aligned} & \text { 蔦 } \\ & \text { Hum } \\ & \text { 总 } \\ & \text { 芯 } \end{aligned}$ | $\begin{aligned} & \text { 品 } \\ & \text { 号 } \end{aligned}$ |  |
| Aluminum base | 94 | 4 | － |  |  |  |  |  | 0.5 | 0.5 |  | 26 |
|  | 93 | 4.2 | ． |  |  |  |  |  | 1.5 | 0.6 |  | 24 |
| Bar． | ． 97 |  | ． |  |  |  |  |  | 2.5 |  | 0.25 | NF－1 |
| Sheet． | 91 | 4.0 |  |  |  |  |  | 2.0 | 0.6 |  |  | NF－2 |
| Tube．．．．．．．． | ． 96.5 |  |  |  |  | 1.0 |  |  | 0.7 | $\cdots$ | 0.25 | 28 |
| Forgings．．．．．． | 85 | 1.0 | ． |  |  | 12.0 |  | 1.0 | 1.0 |  |  | NF－3 |
| （ | 92 | 8 | ． |  |  |  |  |  |  |  |  | 30 |
| Sand castings | 88 | 10.0 | ． |  |  |  |  |  | 0.2 |  |  | 34 |
| ， | 93 | 4 | $\ldots$ |  |  |  |  | 2.0 | 1.5 |  |  | 39 |
| Weight lb．per | 92 | 4.5 | ． |  |  | 1.2 |  |  | ．．．． | 0.3 |  | 38 |
| cu．in． | 84 | 1.0 | $\ldots$ |  |  | 14.0 |  | 2.0 | 1.0 |  |  | 321 |
| 0．092－0．105 | 92 | 1.2 | ． |  |  | 5.0 |  |  | 0.5 |  |  | 322 |
| （ | 94 | ．．． | ． |  |  | 5.0 |  |  | ．．．． |  |  | 35 |
|  | 93 |  | $\cdots$ |  |  | 1.5 |  |  | 3.8 |  |  | 320 |
| 1 | 88 |  |  |  |  |  |  |  | 10.0 |  |  | 324 |
|  |  | 4.0 | ． |  |  | 5.0 |  |  |  |  |  | 307 |
| Die castings | 87 |  |  |  |  | 12 |  |  |  |  |  | 305 |
| Magnesium base | 6.5 | 0.5 |  |  |  |  |  |  |  | 0.2 |  | NF－4 |
| Forgings | 10 |  | ． |  |  |  |  |  | 88 | 0.1 |  | NF－5 |
| Castings | 8 |  |  |  |  |  |  |  | 90 | 0.2 |  | NF－6 |
| Weight，lb．per ou．in． 0．064－0．066 | 6 |  | 3 |  |  |  |  |  |  | 0.2 |  | NF－7 |
| Copper base | ．．．． | 99.5 |  |  |  |  |  |  |  |  |  | 71－75 |
|  |  | 60 | 37 |  | 2.0 |  |  |  |  |  |  | 72－88 |
| Wire． |  | 66 | 34 |  |  |  |  |  |  |  |  | 70 |
| Sheet． |  | 94 | ． | 5.0 |  |  |  |  |  | P0． 4 |  | 77 \＆ 81 |
| Tube． |  | 98 | ． |  |  |  |  |  |  | Be2． 3 |  | NF－8 |
|  | 9 | 88 | ． |  |  |  | 3 |  |  |  |  | 701 |
| Weight，lb．per cu．in $\qquad$ | 10 | 81 | $\cdots$ |  |  |  | 2.5 | 5 |  | 1 |  | NF－9 |
| 0．27－0．35．．． |  | 58 | 42 |  |  |  |  |  |  | 1 |  | NF－10 |
|  |  | 85 | 5 | 5 | 5 |  |  |  |  |  |  | $\cdot 40$ |
|  |  | 88 | 2 | 10 |  |  |  |  |  |  |  | 62 |
| （ |  | 88 |  |  | 1.5 |  |  |  | ．．．．． |  |  | 63 |
| Cating．．．．． |  | 84 |  |  | 9 |  |  |  |  |  |  | 66 |
| Castings．．．．．$\{$ | 10 | 89 |  |  | ．．． |  | 1 |  |  |  |  | 68 |
| $\pi$ | 11 | 79 |  | 5 |  |  |  | 5 |  |  |  | NF－11 |
|  |  | 80 |  |  | 5 |  |  |  |  |  |  | NF－12 |
|  |  | 70 |  |  | 25 |  |  |  |  |  |  | NF－13 |
| 1 |  | 83 |  | 10 | 3 |  |  | 4 |  |  |  | NF－14 |
| Tin base．．．．．．$\{$ |  | 4.5 |  | 90 |  |  |  |  |  |  | Sh7 | 10 |
|  |  |  |  | 50 | 50 |  |  |  |  |  |  |  |
| Silver base． |  | 30 | 25 |  |  |  |  |  |  | Ag45 |  |  |
| Lead base． |  |  |  | 90 |  |  |  |  |  | Ag6 |  |  |
| Nickel base．．．．\｛ |  |  | ． |  |  |  |  | 97 |  | 3 |  |  |
|  |  |  | ． |  |  |  | 10 | 70 |  |  | 15 |  |
| Cobalt base．．．．．$\{$ |  | ．． | $\cdots$ |  |  | 1 | ．．． | ．．． | W－14 | Co－52 | 27 |  |
| Cobalt base．．．．．$\{$ |  | ．．．． | ． |  |  | 2 |  |  | W－4 | Co－65 |  | ．．．．． |

[^39]Table A2-10.-Nonferrous Metals Used in Engine Construction.(Continued)

\begin{tabular}{|c|c|c|c|c|c|}
\hline \multicolumn{5}{|c|}{Mechanical properties} \& \multirow[b]{2}{*}{Application} <br>
\hline  \&  \&  \&  \&  \& <br>
\hline 55,000 \& 32,000 \& 16 \& 90 \& 13,000 \& Washers, rivets, deflectors <br>
\hline 62,000 \& 40,000 \& 15 \& 100 \& 14,000 \& Washers, rivets, deflectors small forgings <br>
\hline 29,000 \& 14,000 \& 20 \& 60 \& 14,000 \& Tubes <br>
\hline 55,000 \& 35,000 \& 8 \& 95 \& \& Pistons <br>
\hline 43,000 \& 34,000 \& 12 \& 90 \& 11,000 \& Large forgings <br>
\hline 55,000 \& 40,000 \& 5 \& 100 \& 14,000 \& Pistons <br>
\hline 18,000 \&  \& .... \& \& \& Cases, coverplates, oil sump <br>
\hline 30,000 \& 18,000 \& \& 100 \& \& Cylinder heads <br>
\hline 32,000 \& 18,000 \& 1 \& 95 \& 8,000 \& Cylinder heads, pistons, bearings <br>
\hline 32,000 \& 18,000 \& 3 \& 80 \& 9,000 \& Crankcase, gear housing <br>
\hline 32,000 \& 18,000 \& $\therefore$ \& 100 \& .... .... \& Pistons <br>
\hline 32,000 \& 20,000 \& 2 \& 90 \& 7,500 \& Miscellaneous castings <br>
\hline 16,000 \& 7,000 \& 2 \& 40 \& 5,000 \& Oil pans, gear-case covers <br>
\hline 18,000 \& 10,000 \& .... \& \& \& Castings requiring high corrosion resistance <br>
\hline 40,000 \& 22,000 \& 11 \& 85 \& 7,500 \& High stressed castings <br>
\hline 32,000 \& \& 2 \& \& \& Accessory housings, covers <br>
\hline 29,000 \& \& 3 \& \& \& Accessory housings, covers <br>
\hline 42,000 \& 24,000 \& 5 \& \& 15,000 \& Nose section, forging <br>
\hline 30,000 \& 18,000 \& 1 \& 65 \& 9,000 \& Nose section, gear-case covers, housings, rear-end crankcase <br>
\hline 29,000 \& 10,000 \& 6 \& 48 \& 7,500 \& Crankcase <br>
\hline 32,000 \& 18,000 \& 4 \& 65 \& 9,000 \& Miscellaneous castings <br>
\hline 34,000 \& 10,000 \& 50 \& \& 11,000 \& Tube, shims <br>
\hline 55,000 \& 25,000 \& 30 \& 60 \& \& <br>
\hline \& .... \& \& \& \& Bolts, shims Bushings <br>
\hline 55-100,000 \& . \& 15.1 \& \& 20,000 \& Bushings <br>
\hline 160,000 \& 130,000 \& 5 \& 300 \& 30,000 \& Bushings, springs <br>
\hline 80,000 \& 40,000 \& 15 \& 160 \& 25,000 \& Valve guides, bushings <br>
\hline \& \& \& 200 \& \& Valve seats <br>
\hline 85,000 \& 40,000 \& 20 \& . . . . \& \& Counterweights <br>
\hline 26,000 \& 12,000 \& 15 \& B-80 \& .. \& Fuel- and oil-line connections <br>
\hline 30,000 \& 15,000 \& 14 \& B-85 \& \& Bushings <br>
\hline 30,000 \& 12,000 \& 10 \& ..... \& \& Bushings <br>
\hline 25,000 \& 12,000 \& 8 \& .... \& \& Bushings <br>
\hline 80,000 \& 50,000 \& 4 \& 170 \& ........ \& Valve seats, propeller cones <br>
\hline 85,000 \& \& 3.5 \& 230 \& \& Valve seats, propeller cones <br>
\hline \& \& \& \& \& Oil-seal rings <br>
\hline \& \& \& 45 \& \& Bushings <br>
\hline \& \& \& \& \& Exhaust valve guides <br>
\hline \multirow[b]{4}{*}{$\begin{array}{r}440 \dagger \\ 1550\end{array}+$} \& \& \& \& \& Bearings <br>
\hline \& \multirow[t]{3}{*}{…
....

$\ldots . . .$.} \& \& \& $360^{\circ} \mathrm{F}$. $\ddagger$ \& Solder <br>
\hline \& \& \& \& $1250^{\circ} \mathrm{F}$. $\ddagger$ \& Solder <br>
\hline \& \& \& \& $580^{\circ} \mathrm{F} . \ddagger$ \& Solder <br>

\hline $1550 \dagger$ \& \multirow[t]{4}{*}{$$
30,000
$$} \& \& \& \& Spark-plug electrodes <br>

\hline \multirow[t]{3}{*}{80,000} \& \& 25 \& \& \& Exhaust equipment <br>
\hline \& \& \& 600 \& \& Stellite No. 1 valve tips <br>
\hline \& \& \& 450 \& .......... \& Stellite No. 6 valve seat facing <br>
\hline
\end{tabular}

[^40]Table A2-11.-Principal Engine Parts and
Representative Specifications*
(From S.A.E. Jour., V̇ol. 40, No. 4, April, 1937)

| Name of part | Spec. No. | Hardness | Spec. No. | Hardness | Spec. No. | Hardness | Spec. No. | Hardness |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Cylinder barrels. | 1050 | 225 | 4140 | . 300 | Nitralloy | 900 |  |  |
| Cylinder heads. | 39 | 65 | 34 | 65 |  |  |  |  |
| Piston........ | 321 | 100 | NF-2 | 100 | NF-3 | 115 | 39 | 110 |
| Piston rings. | ${ }_{\text {Castiron }}$ | C-100 | $\mathrm{Cr}-\mathrm{Ni}-\mathrm{Si}$ | C-40 | Cr-Si-Mo | C-50 | 71360 | C-45 |
| $V$ alve, exhaust | $\mathrm{Cr}-\mathrm{Si}-\mathrm{Mo}$ | C-50 | $\mathrm{Cr}-\mathrm{Ni}-\mathrm{W}-\mathrm{Si}$ | C-15 | $\mathrm{Co}-\mathrm{Cr}$ | C-55 | 13.5 Cr | C-50 |
| Valve, guide. | 68 | 175 | 701 | 160 | $\mathrm{Co}-\mathrm{Cr}$ | C-50 | ${ }^{62}$ | B-85 |
| $V$ alve, spring | 1095 | C-44 | 6150 | C-44 |  |  |  |  |
| $V$ alve, spring washer | 3135 | C-35 | 6150 | C-40 |  |  |  |  |
| Valve, spring retainer | 3250 | C-50 | 6150 | C-40 |  |  |  |  |
| Vn!va ceat . | 68 | 225 | NF-9 | 200 | $\mathrm{Cr}-\mathrm{Ni}-\mathrm{W}-\mathrm{Si}$ | C-15 | 701 | 160 |
| Yv. ic! w-m | 1085 |  |  |  |  |  |  |  |
| Rocker arm. | 3140 | C-30 | 6150 | C-30 | 2330 | C-30 |  |  |
| Rocker-arm hub bolt. | 3140 | C-32 | 6150 | C-25 | 3312 | C-60 |  |  |
| Rocker-arm bearing. | Ball |  | Roller |  |  |  |  |  |
| Rocker-arm cup. | 10115 | C-62 | - 3250 | C-42 | 52100 | C-60 | 6180 | C-55 |
| Push rod, tube. | 26 |  | X-4130 | C-35 | 1025 |  |  |  |
| Push rod, ball end | 1015 | C-62 | 3250 | C-46 | 1095 | C-50 |  |  |
| Push rod, roller. | 3115 | C-60 | 3215 | C-60 |  |  |  |  |
| Push rod, roller pi | 3140 | C-40 | 3250 | C-50 | 6150 | C-52 |  |  |
| Cam. | 3250 | C-55 | 2515 | C-60 |  |  |  |  |
| Camshaft. | 1015 | C-60 |  |  |  |  |  |  |
| Com hearing | 64 | B-75 | 62 | B-85 |  |  |  |  |
|  | 3312 | C-60 | 3140 | C-38 | 2515 | C-55 |  |  |
| Crankease, main.......... | 322 | 80 | 38 | 80 | 28 | 115 |  |  |
| Crankcase, front; rear; blower section. | 322 | 80 | 38 | 80 | NF-5 and 6 | 45 |  |  |
| Impeller. ................. | 26 | 115 | 27 | 100 |  |  |  |  |
| Impeller shaft ............. | 2515 | C-60 | 3312 | C-60 | Nitralloy | 900 |  |  |
| Impeller-shaft bearing...... | Ball |  |  |  |  |  |  |  |
| Crankshaft................ | X-3140 | 260 | 3240 | 280 | 4340 | 320 | 2515 | C-60 |
| Crankshaft counterweights | 1035 | 160 | 43 | 140 | 640 |  |  |  |
| Crankshaft extension. | 3140 | C-40 | 3250 | C-45 | 2515 | C-55 |  |  |
| Propoller-hith nut | 6135 | 250 | 3312 | C-60 | 2330 | C-30 |  |  |
|  | 68 | 210 | 65 | 160 |  |  |  |  |
|  | 3140 | 270 | 4340 | 350 | 2340 | 340 |  |  |
| Pin, piston. | 6150 | C-50 | 3312 | C-60 | 3250 | C-47 | Nitralloy | 900 |
| Pin, knuckle. | 3312 | C-60 | 3120 | C-60 | 52100 | C-60 |  |  |
| Pin, buskinge ${ }^{\text {a }}$, | 62 | 150 | 63 | 130 |  |  |  |  |
|  | 3250 | C-35 | $6150{ }^{\circ}$ | C-35 | 3140 | C-30 |  |  |
| Studs, cylinder | 6150 | C-26 | 3140 | C-30 |  |  |  |  |
| Nuts. . . . . . . . . . . . . . . | 6150 | B-95 | 3140 | C-25 | 2330 | C-20 |  |  |
| Gears, reduction; camshaft drive; accessory drive... . | 3250 | C-45 | 3312 | C-60 | 2515 | C-60 | Nitralloy |  |
| Housings, accessory drive... | 30 | 70 | 322 | 50-80 | 38 | 50-70 | NF-5 and 6 | 45 |
| Housings, accessory drive covers | 30 | 70 | 322 | 50-80 | 35 | 45 | 38 | 50-70 |
| Sump, oil; scoops, air. .... | 30 | 70 | 35 | 45 | NF-5 | 45 |  |  |

* By S.A.E. number except as noted.

 respectivelv.


# Table A2-12.-Copper Alloys Suitable for Miscellaneous Engine Parts <br> (From S.A.E. "Handbook") <br> Spec. No. 62-Hard Bronze Castings 



General Information. The following minimum properties should be attained from standard tension test specimens poured from this alloy in sand molds and tested without machining, provided that proper foundry practices are used.
Tensile strength, lb. per sq. in ..... 30,000
Yield point, lb. per sq. in ..... 15,000
Elongation in 2 in . or proportionate gage length, per cent ..... 14

This alloy is suitable wherever a strong general utility bronze is required. It may be used for severe working conditions where heavy pressures obtain, as in gears and bearings.

This specification conforms in composition with A.S.T.M. B60-36.

> Spec. No. 68-Cast Aluminum Bronze

|  |  |  |
| :---: | :---: | :---: |
| Composition | Grade A | Grade B |
| Copper. | 87.00-89.00 | 89.50-90.50 |
| Aluminum. | 7.00-9.00 | 9.50-10.50 |
| Iron | 2.50-4.00 | Not over 1.00 |
| Tin, max | 0.5 | 0.2 |
| Total | 1.0 | 0.5 |

General Information. Standard test bars cast in sand and tested without machining should give the following minimum mechanical properties:

|  | Grade A | Gr |
| :---: | :---: | :---: |
| Tensile strength, lb. per sq. in. (as cast).............. 65,000 65,000 |  |  |
| Tensile strength, lb. per sq. in. (as heat-treated and drawn).. |  | 80,000 |
| Yield point (as cast) | 25,000 | 25,000 |
| Yield point (as heat-treated). |  | 50,000 |
| Elongation in 2 in., per cent (as cast). | 20 | 15 |
| Elongation in 2 in., per cent (as heat-treated) |  | 4 |

This is a corrosion-resistant alloy of great strength with a hardness equal to that of manganese bronze and under certain conditions has good bearing qualities. It is used for worm wheels, gears, and similar parts.

## Table A2-12.-Copper Alloys Suitable for Miscellaneous Engine Parts.-(Continued)

This specification conforms with the composition and physical properties of A.S.T.M. B59-39.

Report on Non-ferrous Metals Division adopted June, 1911. Last revision, January, 1940.

Spec. No. 701-Wrought Aluminum Bronze
(Annealed, Hot Rolled, or Forged)
Note: Prior to January, 1933, this specification was published as S.A.E. Specification 69.

| Composition | \% |
| :---: | :---: |
| Copper. | 88.00-95.00 |
| Aluminum. | 4.50-10.00 |
| Iron, max..... . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . . | 4.00 |
| Other additions including nickel, tin, and manganese, max. | 2.00 |
| Other impurities including zinc and lead, max. | 0.25 |
| Mechanical requirements |  |

Tensile Test Data

| Diameter or thickness, in. | Width, in. | Ultimate strength, lb. per sq. in. min. | Yield point, lb. per sq. in. min. | Elongation in 2 in ., per cent min. |
| :---: | :---: | :---: | :---: | :---: |
| Rods and bars: |  |  |  |  |
| Over To and inc. |  |  |  |  |
| 0 0.50 |  | 80,000 | 40,000 | 15 |
| $0.50 \quad 1.0$ |  | 75,000 | 37,500 | 15 |
| 1.0 |  | 72,000 | 35,000 | 20 |
| Shapes, all sizes. |  | 75,000 | 30,000 | 15 |
| Plates, sheets, and strips: |  |  |  |  |
| 00.5 | Less than 30 | 60,000 | 24,000 | 25 |
| $0 \quad 0.50$ | Over 30 | 55,000 | 22,000 | 25 |
| 0.50 | All | 50,000 | 20,000 | 30 |

General Information. This is a corrosion-resistant alloy of great strength with a hardness equal to manganese bronze.' It has good bearing and antifrictional properties. Wrought aluminum bronze is used for diaphragms, gears, forgings, for its color, strength, resistance to corrosion and wear and for its properties at elevated temperature. Valve seats and bushings are hot forged for use on internal-combustion engines. The 10 per cent alloy can be heat-treated in a manner similar to steel. Its physical properties are improved to some extent by heating and quenching.

Note: For other data on this adloy, see S.A.E. "Handbook."


Frg. A2-1.-Approximate relation between Brinell, Rockwell, and Shore hardnesses and the strength of structural alloy steel. (From data of the International Nickel Company.)

APPENDIX 3
Table A3-1.-Properties of Various Beam Cross Sections (From Marks, "Mechanical Engineers' Handbook")

| Section | Moment of <br> inertia $(=I)$ | Section <br> modulus <br> $(=I / C)$ | Radius of <br> gyration <br> $(k=\sqrt{I / A})$ |
| :---: | :---: | :---: | :---: |

Table A3-2.-Definition of Spur-gear Tooth Parts (From data of Foote Brothers Gear and Machine Company)
The addendum circle is the circle that limits the tops of the teeth.

The pitch circle is the trace of the pitch cylinders on which the tooth curves are formed.

The dedendum, or root circle, is the circle that
 limits the bottom of the tooth.

The clearance is the amount by which the tops of the teeth of one wheel clear the bottoms of the spaces of the other, as they pass the line of centers.

The working-depth circle is a circle of radius equal to that of the dedendum circle plus the clearance.

The face is that part of the tooth lying between the pitch and addendum circles.

The flank is that part of the tooth lying between the pitch and dedendum circles.

The thickness of the tooth is its width measured on the pitch circle.
The width of space is the space between the teeth measured on the pitch circle.

The backlash is the difference between the thickness of a tooth and the space into which it meshes, measured on the pitch circles.

The pitch diameter is the diameter of the pitch circle. It is the diameter that is used in making all calculations for the size of gears.

The circular pitch is the distance in inches between similar points of adjacent teeth, measured along the pitch circle. It is the thickness of the tooth plus the width of a space, measured on the pitch circle.

The diametral pitch is the number of teeth on the gear per inch of diameter of the pitch circle. Circular pitch times diametral pitch $=\pi$.

The diametral pitch, or module, is the distance in inches obtained by dividing the diameter of the pitch circle by the number of teeth in the gear.

The chordal pitch is the length of a strajght line drawn from the pitch points of two adjacent teeth. Chordal pitch $=$ diameter of pitch circle times sine ( 180 deg. + number of teeth). Chordal pitch is used with chain or sprocket wheels, to conform to the pitch of the chain.

The angles of action are the angles through which the gears turn while a pair of teeth are in action. If the diameters are not alike, these angles will be inversely as the radii of the pitch circles, since the arcs which subtend them are equal.

The angle of approach is the angle through which a gear turns from the beginning of contact of a pair of teeth until contact reaches the pitch point.

The angle of recess is the angle through which a gear turns while the contact point of a pair of teeth moves from the pitch point to the point where the teeth pass out of contact. Angle of approach + angle of recess $=$ angle of action.

Table A3-3.-Standard 141/2- and 20-deg. Involute Gears ${ }^{1,2}$
As the result of work by the American Standards Association, gear-tooth profiles and dimensions have been standardized. Gears having a $14 \frac{1}{2}-\mathrm{deg}$. pressure angle are made either in the composite (part involute and part cycloidal) type or in the $141 / 2$-deg. full-depth involute type. The composite type is stronger but more difficult to machine accurately. The two types are not interchangeable. ${ }^{1}$ Gears of the $20-\mathrm{deg}$. full-depth involute type have teeth that are thicker at the base and therefore they are stronger than the $141 / 2$-deg. pressure angle gears. However, the force tending to separate mating gears is greater with the $20-\mathrm{deg}$. pressure angle than with the $141 / 2$-deg. pressure angle and this may be a disadvantage in some instances. Still greater gear tooth strength may be had by using the $20-\mathrm{deg}$. involute stub tooth (see Table A3-4).

The American Standards Association recommends the following proportions for $141 / 2-\mathrm{deg}$. composite, $141 / 2-\mathrm{deg}$. full-depth involute and $20-\mathrm{deg}$. full-depth involute gears. ${ }^{1}$

Dimensions for 141/2-deg. Composite, 141/2-deg. Full-depth, 20-deg. Full-depth Gears

| Part | In terms of diametral pitch, in. | In terms of circular pitch, in. |
| :---: | :---: | :---: |
| Addendum | $1.0 / P_{\text {d }}$ | $0.3183 \times P_{\text {c }}$ |
| Minimum dedendum | $1.157 / P_{d}$ | $0.3683 \times P_{\text {c }}$ |
| Working depth. | $2.0 / P_{d}$ | $0.6366 \times P_{c}$ |
| Minimum total depth | $2.157 / P_{d}$ | $0.6866 \times P_{\text {c }}$ |
| Minimum clearance | $0.157 / P_{d}$ | $0.0500 \times P_{c}$ |
| Pitch diameter. | $N / P_{d}$ | $0.3183 \times M \times P_{0}$ |
| Outside diameter. | $\frac{N+2}{P_{d}}$ | $0.3183 \times(N+2) \times P_{c}$ |

[^41]
## Table A3-4.-Stub-tooth Gears ${ }^{1,2}$

The advantages of the stub-tooth gear as compared with the standard involute 1412-deg.-pressure-angle spur gears are as follows: ${ }^{2}$

1. Equal arc of rolling action.
2. Reduction of sliding action.
3. More even wearing contact.
4. Longer life.
5. Greater strength.
6. Possibility of decreasing pitch.
7. Reduction of noise.
8. Less distortion in hardening.

Strength is the factor that is generally uppermost in the designer's mind when he is laying out a gear-tooth form of gearing that will be subjected to shocks or intermittent loads. It is the fact of increased strength that has been largely instrumental in advancing the popularity of the stub-tooth gear. This type of tooth has been successfully applied in the manufacture of automobile and airplane gear drives. ${ }^{2}$

A shortening and widening of the tooth at the base results from increasing the pressure angle from $141 / 2$ to 20 deg . As a general rule, stub-tooth gears with less than 25 tecth are about 25 per cent stronger than standard $20-\mathrm{deg}$. full-depth involute teeth and 40 per cent stronger than $141 / 2-\mathrm{deg}$. involute teeth. For larger numbers of teeth, the gain in strength is somewhat less. ${ }^{2}$

The American Standards Association recommends the following proportions for 20-deg. stub-tooth gears: ${ }^{1}$

Dimensions for 20-deg. Stub Gears

| Part | In terms of diametral pitch, in. | In terms of circular pitch, in. |
| :---: | :---: | :---: |
| Addendum | $0.8 / P_{d}$ | $0.2546 \times P_{\text {c }}$ |
| Minimum dedendum | $1.0 / P_{d}$ | $0.3183 \times P_{c}$ |
| Working depth. | $1.6 / P_{d}$ | $0.5092 \times P_{\text {c }}$ |
| Minimum total depth. | $1.8 / P_{d}$ | $0.5729 \times P_{d}$ |
| Minimum clearance | $0.2 / P_{d}$ | $0.0637 \times P_{0}$ |
| Pitch diameter | $N / P_{d}$ | $0.3183 \times N \times P_{c}$ |
| Outside diameter. | $\frac{N+1.6}{P_{d}}$ | $D+(2$ addendums) |

[^42]
## Table A3-5.-Internal Gears ${ }^{1,2}$

Internal gear dimensions may be found by the same formulas as for external gearing except for modifications made necessary by the fact that the center distance in internal gearing is equal to the difference between the two pitch radii instead of their sum. In addition, the term inside diameter takes the place of outside diameter in external gearing. Inside diameter is the diameter of the hole in the gear blank before the teeth are cut.


Internal gear details.
Internal gears have several desirable characteristics: ${ }^{1}$

1. Much stronger teeth due to greater base width.
2. Less sliding action, hence less wear.
3. Higher efficiency.
4. More teeth in contact.
5. Smoother operation.
6. More compact design.

For internal gears of the same material as their pinions, it is unnecessary to calculate the strength because, ( $a$ ) the torque arm is greater, hence the torque force is less than on the pinion, and (b) the teeth are much stronger than the pinion teeth because of greater base width.

[^43]Table A3-6.-Simple Epicyclic Gearing ${ }^{1,2,3}$
The principle of operation of the simple epicyclic gear train is illustrated in the accompanying diagram where $S$ is the sun pinion, $P$ is the planet pinion, $G$ is the internal gear, and $A$ is the arm carrying $P$.


The following formulas give the speeds, pitch-line velocities, and loads for the six most commonly used cases. In these formulas:
$N_{G}=$ number of teeth in internal gear $G$.
$N_{P}=$ number of teeth in planet pinion $P$.
$N_{S}=$ number of teeth in sun pinion $S$.
$E=$ center distance of gears $S$ and $P$.
$V=$ pitch-line velocity of transmitted load, f.p.m.
$V_{G}=$ pitch-line velocity of tooth engagement on $G$, f.p.m.
$V_{S}=$ pitch-line velocity of tooth engagement on $S$, f.p.m.
$V_{A}=$ velocity of center of planet pinion $P$, f.p.m.
$n=$ r.p.m. of driving member.
$W=$ transmitted load, lb .
$W_{G}=$ tooth load on $G, \mathrm{lb}$.
$W_{S}=$ tooth load on $S, \mathrm{lb}$.
$W_{A}=$ load at center of pinion, lb .
$Q=$ driving torque, in. lb .
$h p .=$ number of horsepower transmitted.
${ }^{1}$ Data of Foote Brothers Gear and Machine Company.
${ }^{2}$ Schwamb, Merill, and James, "Elements of Mechanism."
3 Buckingham, "Manual of Gear Design."
Table A3-6.-Internal Gears.-(Continued)

| Case No. | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Stationary member. . | A | A | , $a^{\text {a }}$ | $S$ | $G$ | S |
| $\begin{aligned} & \text { Driving mem } \\ & \text { ber......... } \end{aligned}$ | $S$ | $G$ | $A$ | A | S | G |
| $\begin{aligned} & \text { Driven mem- } \\ & \text { ber. ....... } \end{aligned}$ | $G$ | $S$ | $S$ | G | A | A |
| $\begin{gathered} \hline \text { Reduction } \\ \text { ratio...... } \end{gathered}$ | $\frac{N S}{\bar{N} \theta}$ | $\frac{N_{G}}{N_{S}}$ | $\frac{N_{\sigma}+N_{s}}{N_{s}}$ | $\frac{N a+N s}{N a}$ | $\frac{N s}{N_{G}+N s}$ | $\frac{N a}{N G+N s}$ |
| R.p.m. of A.. | 0 | 0 | $n$ | $n$ | $n\left(\frac{N s}{N G+N s}\right)$ | $n\left(\frac{N G}{N a+N s}\right)$ |
| R.p.m. of S.. | $n$ | $n\left(\frac{N_{\theta}}{N_{S}}\right)$ | $n\left(\frac{N_{G}+N s}{N_{G}}\right)$ | 0 | $n$ | 0 |
| R.p.m. of P.. | ${ }^{n}\left(\frac{N_{s}}{N_{P}}\right)$ | $n\left(\frac{N_{G}}{\bar{N}_{S}}\right)$ | ${ }^{n}\left(\frac{N_{G}}{N_{P}}\right)$ | $n\left(\frac{N s}{N_{P}}\right)$ | $n\left(\frac{N_{G}}{N_{P}}\right)\left(\frac{N_{S}}{N_{G}+N_{S}}\right)$ | $n\left(\frac{N S}{N_{P}}\right)\left(\frac{N_{G}}{N_{G}+N_{S}}\right)$ |
| R.p.m. of G. . | $n\left(\frac{N s}{N_{G}}\right)$ | $n$ | 0 | $n\left(\frac{N_{G}+N_{S}}{N_{G}}\right)$ | 0 | $n$ |
| V........... | $0.5236 n \mathrm{E}\left(\frac{N S}{N S+N_{P}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)$ | $0.5236 n E$ | $0.5236 n E$ | $0.5236 n E\left(\frac{N_{s}}{N_{s}+N_{P}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)$ |
| Vs.......... | $0.5236 n E\left(\frac{N s}{N s+N_{P}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N s+N_{P}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{S}+N_{P}}\right)$ | $0.5236 \mathrm{nE}\left(\frac{N_{S}}{N s+N_{P}}\right)$ | $0.5236 n \mathrm{E}\left(\frac{N_{S}}{N_{S}+N_{P}}\right)\left(\frac{N_{G}}{N_{G}+N_{S}}\right)$ | $0.5236 n E\left(\frac{N_{S}}{N_{S}+N_{P}}\right)\left(\frac{N_{G}}{N_{G}+N_{S}}\right)$ |
| $V_{\text {A }} \ldots \ldots . . .$. | 0 | 0 | $0.5236 n E$ | 0.5236 nE | $0.5236 \pi E\left(\frac{N s}{N G+N s}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}+N_{S}}\right)$ |
| Va......... | $0.5236 n E\left(\frac{N s}{N_{G}-N_{P}}\right)$ | $\underline{0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)}$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)$ | $0.5236 n E\left(\frac{N S}{N G-N_{P}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)\left(\frac{N_{s}}{N_{G}+N_{S}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P}}\right)\left(\frac{N_{s}}{N_{G}+N_{s}}\right)$ |
| $\begin{aligned} & W=\frac{33,000 \mathrm{hp} .}{V} \\ & \text { or } \rightarrow \ldots \ldots . \end{aligned}$ | $\frac{Q}{E}\left(\frac{N s+N_{P}}{N s}\right)$ | $\frac{Q}{E}\left(\frac{N_{G}-N_{P}}{N_{G}}\right)$ | $\frac{Q}{E}$ | $\frac{Q}{E}$ | $\frac{Q}{E}\left(\frac{N_{s}+N_{P}}{N_{s}}\right)$ | $\frac{Q}{E}\left(\frac{N_{G}-N_{P}}{N_{G}}\right)$ |
| Ws.... | W | $W\left(\frac{N_{s}+N_{P}}{N_{G}-N_{P}}\right)$ | $W\left(\frac{N S+N_{P}}{N S+N_{G}}\right)$ | $W\left(\frac{N_{s}+N_{P}}{N_{s}+N_{G}}\right)$ | W | $W\left(\frac{N_{S}+N_{P}}{N_{G}-N_{P}}\right)$ |
| $W_{4}$. | $W\left(\frac{N s+N_{G}}{N s+N_{P}}\right)$ | $W\left(\frac{N_{S}+N_{G}}{N_{G}-N_{P}}\right)$ | W | W | $W\left(\frac{N a+N s}{N s+N_{P}}\right)$ | $W\left(\frac{N_{G}+N_{s}}{N_{G}-N_{P}}\right)$ |
| W ${ }_{\text {c }}$ | $W\left(\frac{N_{G}-N_{P}}{N_{S}+N_{P}}\right)$ | If | $W\left(\frac{N_{G}-N_{P}}{N s+N G}\right)$ | $W\left(\frac{N G-N_{P}}{N s+N_{G}}\right)$ | $W\left(\frac{N Q-N_{P}}{N s+N_{P}}\right)$ | W |

Table A3-7.-Compound Epicyclic Gearing ${ }^{1,2,3}$
The principle of operation of the compound epicyclic gear train is illustrated in the accompanying diagram where $S$ is the sun pinion, $G$ is the internal gear, A is the arm carrying $P_{S}$ and $P_{G}, P_{G}$ is the planet gear meshing with $G, P_{S}$ is the planet gear meshing with $S P_{G}$ and $P_{S}$ are both keyed to shaft $M_{3}$.


The following formulas give the speeds, pitch-line velocities, and loads for the six most commonly used cases. In these formulas:
$N_{G}=$ number of teeth in internal sun gear.
$N_{P S}=$ number of teeth in planet pinion meshing with $S$.
$N_{P G}=$ number of teeth in planet pinion meshing with $G$.
$N_{s}=$ number of teeth in spur sun gear.
$E=$ center distance of gears, in.
$V=$ velocity of the transmitted load, f.p.m.
$V_{S}=$ pitch-line velocity of tooth engagement on $S$, f.p.m.
$V_{G}=$ pitch-line velocity of tooth engagement on $G$, f.p.m.
$V_{A}=$ velocity of center of planet pinions, f.p.m.
$Q=$ driving torque, in. -lb .
$h p .=$ number of horsepower transmitted.
$n=$ r.p.m. of driving member.
$W=$ transmitted load, lb .
$W_{G}=$ tooth load on $G, \mathrm{lb}$.
$W_{S}=$ tooth load on $S$, lb.
$W_{A}=$ load at center of pinions, lb .
Potential power (ft.-lb. per min.) $=W_{G} V_{G}=W_{P S} V_{P S}$.
Transmitted power (ft. -lb . per min.) $=W V$.

[^44]Table A3-7.-Compound Epicyclic Gearing.-(Continued)

| Case No. | 1 | 2 | 3 | 4 | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{gathered} \overline{\text { Fixed mem- }} \\ \text { ber........ } \end{gathered}$ | A | $A$ | $G$ | $S$ | $G$ | S |
| Driving member. . | $S$ | $G$ | A | A | $S$ | $G$ |
| Driven member. . | $G$ | $S$ | $S$ | $G$ | A | A |
| Reduction ratio. | $\begin{aligned} & N_{S S N_{P G}} \\ & \hline N_{G} N_{P S} \end{aligned}$ | $\begin{aligned} & N_{G G N_{P S}} \\ & \overline{N S N} \frac{1}{P G} \end{aligned}$ | $\frac{N_{s} N_{P G}+N_{G} N_{P S}}{N_{s} N_{P G}}$ | $\frac{N_{S} N_{P G}+N_{G} N_{P S}}{N_{G} N_{P S}}$ | $\frac{N_{S} N_{P G}}{N_{S} N_{P G}+N_{O} N_{P S}}$ | $\frac{N_{G} N_{P S}}{N_{s} N_{P G}+N_{G} N_{P S}}$ |
| R.p.m. of $A$. | 0 | 0 | $n$ | $n$ | $n\left(\frac{N_{s} N_{P G}}{N_{S} N_{P G}+N_{G} N_{P S}}\right)$ | $n\left(\frac{N_{G} N_{P S}}{N_{S} N_{P G}+N_{G} N_{P S}}\right)$ |
| R.p.m. of $S$ | $n$ | $n\left(\frac{N_{G} N_{P S}}{N_{S S} N_{P G}}\right)$ | $n\left(\frac{N_{S} N_{P G}+N_{G} N_{P S}}{N_{S} N_{P G}}\right)$ | 0 | $n$ | 0 |
| $\begin{array}{r} \overline{\text { R.p.m. of } P G} \\ \text { and } P s \ldots \end{array}$ | $n\left(\frac{N_{S}}{N_{P S}}\right)$ | $n\left(\frac{N_{G}}{N_{P G}}\right)$ | . $n\left(\frac{N_{G}}{N_{P G}}\right)$ | $n\left(\frac{N_{s}}{N_{P S}}\right)$ | $n\left(\frac{N_{G} N_{S}}{N_{S} N_{P G}+N_{G} N_{P S}}\right)$ | $n\left(\frac{N_{S N} N_{G}}{N_{S} N_{P}+N_{G} N_{P S}}\right)$ |
| R.p.m. of G. | ${ }^{n}\left(\frac{N_{S S} N_{P G}}{N_{G} N_{P S}}\right)$ | $n$ | 0 | $n\left(\frac{N_{S} N_{P G}+N_{G} N_{P S}}{N_{G} N_{P S}}\right)$ | 0 | $n$ |
|  | $0.5236 n E\left(\frac{N_{s}}{N_{S}+N_{P S}}\right)$ | $0.5236 n E\left(\frac{\overline{N G}}{N_{G}-N_{P G}}\right)$ | $0.5236 n E$ | $0.5236 n E$ | $0.5236 \mathrm{nE}\left(\frac{N_{S}}{N_{S}+N_{P S}}\right)$ | $0.5236 n E\left(\frac{N_{G}}{N_{G}-N_{P G}}\right)$ |
|  | $0.5236 n E\left(\frac{N S}{N s+N_{P S}}\right)$ | $\begin{gathered} 0.5236 n E \\ {\left[\frac{N_{G} N_{P S}}{N_{P G}\left(N_{S}+N_{P S}\right)}\right]} \end{gathered}$ | $\begin{aligned} & 0.5236 n E \\ & {\left[\frac{N_{G N} N_{P S}}{N_{P G}\left(N_{s}+N_{P S}\right)}\right]} \end{aligned}$ | $\left(\frac{N s}{N s+N_{P S}}\right)$ | $\left(\frac{N_{G} N_{P S}}{N_{S} N_{P G}+N_{G} N_{P S}}\right)\left(\frac{N_{s}}{N_{s}+N_{P S}}\right)$ | $\left(\frac{N_{G} N_{P S}}{N_{s} N_{P G}+N_{G} N_{P S}}\right)\left(\frac{N s}{N s+N_{P S}}\right)$ |
|  | 0 | 0 | $0.5236 n E$ | $0.5236 n E$ | $0.5236 n E\left(\frac{N_{S} N_{P G}}{N_{S} N_{P Q}+N_{G} N_{P S}}\right)$ | $0.5236 \mathrm{nE}\left(\frac{N_{G} N_{P S}}{N_{S S} N_{P G}+N_{G} N_{P S}}\right)$ |
| Va. | $\left[\frac{N_{S} N_{P G}}{N_{P S}\left(N_{G}-N_{P G}\right)}\right]$ | $\left(\frac{N a}{N_{G}-N P G}\right)$ | $\left(\frac{N_{G}}{N_{G}-N_{P}}\right)$ | $\left[\begin{array}{l} 0.5236 \mathrm{nE} \\ {\left[\frac{N_{S} N_{P G}}{N_{P S}\left(N_{G}-N_{P G}\right)}\right]} \end{array}\right.$ | $\left(\frac{N_{S} N_{P G}}{N_{S} N_{P G}+N_{G} N_{P S}}\right)\left(\frac{N_{G}}{N_{Q}-N_{P G}}\right)$ | $\left(\frac{N_{S} N_{P G}}{N_{s} N_{P G}+N_{G} N_{P S}}\right)\left(\frac{N_{G}}{N_{G}-N_{P G}}\right)$ |
| $\begin{gathered} \hline= \\ \frac{33,000 \mathrm{hp}}{V} \\ \text { or } \rightarrow \ldots \ldots \\ \hline \end{gathered}$ | $\frac{Q}{E}\left(\frac{N s+N_{P S}}{N_{s}}\right)$ | $\frac{Q}{E}\left(\frac{N_{G}-N_{P G}}{N_{G}}\right)$ | $\frac{Q}{E}$ | $\frac{Q}{E}$ | $\frac{Q}{E}\left(\frac{N s+N_{P s}}{N s}\right)$ | $\frac{Q}{E}\left(\frac{N_{G}-N_{P G}}{N_{G}}\right)$ |
| Ws.... | W | $\left[\frac{N_{P G}\left(N_{S}+N_{P S}\right)}{N_{P S}\left(N_{g}-N_{P G}\right)}\right]$ | $\left[\frac{N_{P Q}\left(N_{S}+N_{P S}\right)}{N_{s} N_{P G}+N_{G} N_{P S}}\right]$ | $\left[\frac{N_{S}\left(N_{S}+N_{P S}\right)}{N_{S} N_{P G}+N_{G} N_{P S}}\right]$ | W | $W\left[\frac{N_{P G}\left(N_{s}+N_{P s}\right)}{N_{P S}\left(N_{G}-N_{P G}\right)}\right]$ |
| $\overline{W_{\text {A }} \ldots \ldots \ldots .}$ | $\left[\frac{N_{S S} N_{P G}+N_{G} N_{P S}}{N_{P G}\left(N_{S}+N_{P S}\right)}\right]$ | $\left[\frac{N_{S} N_{P G}+N_{G} N_{P S}}{N_{P S}\left(N_{G}-N_{P G}\right)}\right]$ | W | IT | $W\left[\frac{N S N_{P G}+N_{G} N_{P S}}{N_{P G}\left(N_{S}+N_{P S}\right)}\right]$ | $W\left[\frac{\left.N_{S S} N_{P G}+N_{G} N_{P S}\right)}{N_{P S}\left(N_{G}-N_{P G}\right)}\right]$ |
| WG...... | $\left[\begin{array}{l} \left.\frac{N_{P S}\left(N_{G}-N_{P G}\right)}{N_{P G}\left(N_{S}+N_{P S}\right)}\right] \end{array}\right.$ | W | $\left[\begin{array}{l} \mathbb{W} \\ {\left[\frac{N_{P S}\left(N_{G}-N_{P G}\right)}{N_{S} N_{P G}+N_{G} N_{P S}}\right]} \end{array}\right.$ | $\left.\left\lvert\, \begin{array}{l}\bar{W} \\ {\left[\frac{N_{P S}\left(N_{G}-N_{P G}\right)}{N_{S S} N_{P G}+N_{G} N_{P S}}\right]}\end{array}\right.\right]$ | $W\left[\frac{N_{P S}\left(N_{G}-N_{P G}\right)}{N_{P G}\left(N_{S}+N_{P S}\right)}\right]$ | W |

## Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing

(From data of Foote Brothers Gear and Machine Company)
The elements to be considered in the design and selection of bevel gearing, calculation of tooth strengths and horsepower ratings are very similar to those already covered in Tables A3-2 and A3-3 on spur gearing, with the exception that we must consider here pitch angles, face angles, cutting angles, etc.

The following table and diagrams define the various elements that are generally used in the solution of bevel and miter-gear problems, where shafts run at 90-deg. angles.
$N=$ number of teeth.
$P=$ diarnetral pitch.
$P^{\prime}=$ circular pitch.
$\cdot \pi=3.1416$.
$\alpha=$ pitch cone angle and edge angle.
$\gamma=$ center angle.
$D=$ pitch diameter.
$S=$ addendum.
$S+A=$ dedendum ( $A=$ clearance).
$W=$ whole depth of tooth space.
$T=$ thickness of tooth at pitch line.
$C=$ pitch cone radius.
$F=$ width of face.
$s=$ addendum at small end of tooth.
$t=$ thickness of tooth at pitch line at small end.
$\theta=$ addendum angle.
$\phi=$ dedendum angle .
$\delta=$ face angle.

$\zeta=$ cutting angle.
$K=$ angular addendum.
$O=$ outside diameter (edge diameter for internal gears).
$J=$ vertex distance.
$j=$ vertex distance at small end.
$N^{\prime}=$ number of teeth for which to select cutter, also called "number of teeth in equivalent spur gear."

Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued)

$\alpha_{p}=$ Pitch cone
angle of pinion;
$\alpha_{g}=$ Pitch cone
angle of gear;
$N_{p}=$ Number of feeth
in pinion, etc.


Use rules and formulas 1 to 21 in order given.

| No. | To find | Rule | Formula |
| :---: | :---: | :---: | :---: |
| 1 | Pitch-cone angle (or edge angle) of pinion | Divide the number of teeth in the pinion by the number of teeth in the gear to get the tangent | $\tan \alpha_{p}=\frac{N_{p}}{N_{o}}$ |
| 2 | Pitch-cone angle (or edge angle) of gear | Divide the number of teeth in the gear by the number of teeth in the pinion to get the tangent | $\tan \alpha_{g}=\frac{N_{g}}{N_{p}}$ |
| 3 | Proof of calculations for pitchcone angles | The sum of the pitch-cone angles of the pinion and gear equals 90 deg. | $\alpha_{p}+\alpha_{d}=90^{\circ}$ |
| 4 | Pitch diameter | Divide the number of teeth by the diametral pitch; or multiply the number of teeth by the circular pitch and divide by 3.1416 | $D=\frac{N}{P}=\frac{N P^{\prime}}{\pi}$ |
| 5* | Addendum | Divide 1.0 by the diametral pitch; or multiply the circular pitch by 0.318 | $\begin{aligned} S & =\frac{1.0}{P} \\ & =0.318 P^{\prime} \end{aligned}$ |
| 6 | Dedendum | Divide 1.157 by the diametral pitch; or multiply the circular pitch by 0.368 | $\begin{gathered} S+A=\frac{1.157}{P} \\ =0.368 P^{\prime} \end{gathered}$ |
| 7 | Whole depth of tooth space | Divide 2.157 by the diametral pitch; or multiply the circular pitch by 0.687 | $\begin{aligned} W & =\frac{2.157}{P} \\ & =0.687 P^{\prime} \end{aligned}$ |

* Nos. 5 to 13 are the same for both gear and pinion.

Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued)

| No. | To find | Rule | Formula |
| :---: | :---: | :---: | :---: |
| 8 | Thickness of tooth at pitch line | Divide 1.571 by the diametral pitch; or divide the circular pitch by 2 | $T=\frac{1.571}{P}=\frac{P^{\prime}}{2}$ |
| 9 | Pitch-cone radius | Divide the pitch diameter by twice the sine of the pitchcone angle | $C=\frac{D}{2 \times \sin \alpha}$ |
| 10 | Addendum of small end of tooth | Subtract the width of face from the pitch-cone radius, divide the remainder by the pitch-cone radius, and multiply by.the addendum | $s=S \times \frac{C-F}{C}$ |
| 11 | Thickness of tooth at pitch line at small end | Subtract the width of face from the pitch-cone radius, divide the remainder by the pitch-cone radius, and multiply by the thickness of the tooth at the pitch line | $t=T \times \frac{C-F}{C}$ |
| 12 | Addendum angle | Divide the addendum by the pitch-cone radius to get the tangent | $\tan \theta=\frac{S}{C}$ |
| 13 | Dedendum angle | Divide the dedendum by the pitch-cone radius to get the tangent | $\tan \phi=\frac{S+A}{C}$ |
| 14 | Face angle | Subtract the sum of the pitch-cone and addendum angles from 90 deg. | $\delta=90^{\circ}-(\alpha+\theta)$ |
| 15 | Cutting angle | Subtract the dedendum angle from the pitch-cone angle | $\zeta=\alpha-\phi$ |
| 16 | Angular addendum | Multiply the addendum by the cosine of the pitch-cone angle | $K=S \times \cos \alpha$. |
| 17 | Outside diameter | Add twice the angular addendum to the pitch diameter | $O=D+2 K$ |
| 18 | Vertex distance | Multiply one-half the outside diameter by the tangent of the face angle | $J=\frac{O}{2} \times \tan \delta$ |

Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued)

| No. | To find | Rule | Formula |
| :--- | :---: | :---: | :---: |
| 19 | Vertex distance at <br> small end of <br> tooth | Subtract the width of face <br> from the pitch-cone radius, <br> divide the remainder by the <br> pitch-cone radius, and mul- <br> tiply by the vertex distance | $j=J \times \frac{C-F}{C}$ |
| 20 | Number of teeth <br> for which to se- <br> lect cutter | Divide the number of teeth <br> by the cosine of the pitch- <br> cone angle | $N^{\prime}=\frac{N}{\cos \alpha}$ |
| Proof of calcula- <br> tions by rules 9, <br> $12,14,16$ and 17 | The outside diameter equals <br> twice the pitch-cone radius <br> multiplied by the cosine of <br> the face angle and divided <br> by the cosine of the adden- <br> dum angle | $O=\frac{2 C \times \cos \delta}{\cos \theta}$ |  |

Recommended Practice for Bevel Gearing
The American Gear Manufacturers Association has adopted as recommended practice the following rules:

The maximum length of face of bevel gears should not be over one-third of the cone distance for gears up to 3 -in. pitch diameter and not over onefourth of the cone distance for gears from $3-$ to $20-\mathrm{in}$. pitch diameter, assuming that the pitch in every case will be in proper proportion to the size of the gears. A safe rule is to make the face $11 / 2$ to $21 / 2$ times the circular pitch.

The minimum length of bearing along the face is to be at least one-half the length of the face when the gears are held in correct alignment.

Bevel gears with generated involute teeth of standard addendurm having a pressure angle of $141 / 2 \mathrm{deg}$. may be used according to the following rule:

| $\quad$ Ratio | No. of Tecth |
| :--- | :---: |
| $1: 1$ | 14 and over |
| $11 / 2: 1$ | 18 and over |
| $2: 1$ | 19 and over |
| $3: 1$ and over | 21 and over |

This rule is given applying mainly to gears up to $20-\mathrm{in}$. pitch diameter and to average industrial machine design as distinguished from automobiles. Recommended Practice for Backing Dimensions of Bevel and Miter (iears

The following formulas are recommended for the calculation of backing dimensions of bevel and miter gears.

Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued) Bevel Gears and Pinions
Backing in inches of pinion $=\frac{\text { pitch diameter of gear } \times 0.250}{(\text { ratio of gear to pinion })+1}$ Backing in inches of gear $=$ (pitch diameter of gear $\times 0.250$ ) - backing of pinion

## Miter Gears

Backing in inches of gear $=$ pitch diameter $\times 0.125$
This does not allow for set screws in pinions below 4 in. pitch diameter.

## Strength of Bevel and Miter Gears

The method for the calculation of strength of bevel gearing is based on the Lewis formula for the strength of gear teeth and is practically the same as is used for spur gears.

The accompanying tables of rules and formulas for the strength of bevel gears with the tables "Working Stresses Used in the Lewis Formula for the Strength of Gear Teeth" in tables on Spur Gearing give all necessary data for calculating the strength of bevel gears.

The following tables and formulas are based on the use of the diametral pitch of the gears, and if the circular pitch is given it should be transformed into diametral pitch by dividing 3.1416 by the circular pitch.

## Rules and Formulas for the Strength of Bevel Gears

$D=$ pitch diameter of gear, in.
$R=$ r.p.m.
$V=$ velocity, ft. per min. at pitch diameter.
$S_{s}=$ allowable static unit stress for material.
$S=$ allowable unit stress for material at given velocity.
$F=$ width of face.
$N^{\prime}=$ number of teeth in equivalent spur gear (see diagram in table, page 475).
$Y=$ outline factor (see table, page 475). .
$P=$ diametral pitch (if circular pitch is given, divide 3.1416 by circular pitch to obtain diametral pitch).
$C=$ pitch-cone radius.
$W$. maximum safe tangential load in pounds at pitch diameter.
hp. = maximum safe horsepower.

Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued) Use rules and formulas 1 to 4 in the order given.

| No. | To find | Rule | Formula |
| :---: | :---: | :---: | :---: |
| 1 | Velocity in feet per minute at the pitch diameter | Multiply the product of the diameter in inches and the number of revolutions per minute by 0.262 | $V=0.262 D R$ |
| 2 | Allowable unit stress at given velocity | Multiply the allowable static stress by 600 , and divide the result by the velocity in feet per minute plus 600 | $S=S_{s} \times \frac{600}{600+V}$ |
| 3 | Maximum safe tangential load at pitch diameter | Multiply together the allowable stress for the given velocity, the width of face, the tooth outline factor, and the difference between the pitch-cone radius and the width of face; divide the result by the product of the diametral pitch and the pitchcone radius | $W=\frac{S F Y(C-F)}{P C}$ |
| 4 | Maximum safe horsepower | Multiply the safe load at the pitch line by the velocity in feet per minute, and divide the result by 33,000 | $\mathrm{hp} .=\frac{W V}{33,000}$ |

## Table A3-8.-Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued) Factors for Calculating Strength of Bevel Gears



End Thrust on Bevel Gears
In designing bearings to be used with bevel and miter gears, it is important to know the end thrust exerted by the bevel gears and pinions so that proper end-thrust bearings may be provided.

The method of calculation of end thrusts is as follows:
$A=$ pressure angle of the gear teeth.
$P=$ tooth pressure at middle of tooth face.
$F^{\prime}=$ separating force $=P \times \tan A$.
$B=$ pitch angle of pinion.
$T=$ thrust on pinion $=P \times \tan A \times \sin B$.
$T_{1}=$ thrust on gear $=P \times \tan A \times \cos B$.
The following table gives the factors by which the tooth pressure is multiplied to find the thrust, giving practically the same values found by solving the formulas for $T$ and $T_{1}$, given above.

Table A3-8.--Engineering Information Covering the Design and Application of Bevel and Miter Gearing.-(Continued)

| Gear ratio | Pressure angle $A$ |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 141/2 deg. |  | 15 deg . |  | 20 deg . |  | 22 deg. |  |
|  | Gear | Pinion | Gear | Pinion | Gear | Pinion | Gear | Pinion |
| 1 :1 | 0.183 | 0.183 | 0.189 | 0.189 | 0.257 | 0.257 | 0.286 | 0.286 |
| 11/2:1 | 0.215 | 0.143 | 0.223 | 0.148 | 0.303 | 0.202 | 0.336 | 0.224 |
| 2 :1 | 0.232 | 0.116 | 0.239 | 0.120 | 0.325 | 0.163 | 0.361 | 0.181 |
| 21/2:1 | 0.240 | 0.096 | 0.249 | 0.100 | 0.338 | 0.135 | 0.375 | 0.150 |
| $3: 1$ | 0.246 | 0.082 | 0.254 | 0.085 | 0.345 | 0.115 | 0.383 | 0.128 |
| 31/2:1 | 0.249 | 0.071 | 0.258 | 0.074 | 0.350 | 0.100 | 0.389 | 0.111 |
| $33 / 4$ : 1 | 0.250 | 0.067 | 0.259 | 0.069 | 0.352 | 0.094 | 0.390 | 0.104 |
| 4 :1 | 0.251 | 0.062 | 0.260 | 0.065 | 0.353 | 0.088 | 0.392 | 0.097 |
| 412:1 | 0.253 | 0.056 | 0.262 | 0.058 | 0.355 | 0.079 | 0.394 | 0.087 |
| 5 :1 | 0.254 | 0.051 | 0.263 | 0.053 | 0.3574 | 0.072 | 0.396 | 0.080 |
| 51/2:1 | 0.255 | 0.046 | 0.264 | 0.048 | 0.358 | 0.065 | 0.398 | 0.072 |

Table A3-9.-Bearing Loads Due to Straight Spur Gears
(From New Departure "Handbook")
Bearing loads due to tangential and separating forces at tooth contact.


Torque input $=Q \frac{63,025 \times \mathrm{hp} \cdot \text { transmitted }}{\text { r.p.m. of driving gear }}, \mathrm{lb}$. inches.
Tangential force $=P=\frac{Q}{r}=\frac{\text { torque input, } \mathrm{lb} .-\mathrm{in} .}{\text { pitch radius of gear, in. }} \mathrm{lb}$.
Separating force $=S=P \tan \alpha, \mathrm{lb} . \quad$ ( $\alpha=$ tooth pressure angle)
$L=$ total load on both shafts due to gears

| Due to | On bearing 1 | On bearing 2 | On bearing 3 | On bearing 4 |
| :---: | :---: | :---: | :---: | :---: |
| $P$ | $P_{1}=P \frac{A}{A+B}$ | $P_{2}=P \frac{B}{A+B}$ | $P_{3}=P \frac{C}{C+D}$ | $P_{4}=P \frac{D}{C+D}$ |
| $S$ | $S_{1}=S \frac{A}{A+B}$ | $S_{2}=S \frac{B}{A+B}$ | $S_{3}=S \frac{C}{C+D}$ | $S_{4}=S \frac{D}{C+D}$ |
| $L$ | $L=\sqrt{P_{1}^{2}+S_{1}^{2}}$ | $L=\sqrt{P_{2}^{2}+S_{2}^{2}}$ | $L_{3}=\sqrt{P_{3}^{2}+S_{3}^{2}}$ | $L_{4}=\sqrt{P_{4}^{2}+S_{4}^{2}}$ |

Table A3-10.-Bearing Loads Due to Straight Spur Gears in Train


Torque input $=Q=\frac{63,025 \times \mathrm{hp} \text {. transmitted }}{\text { r.p.m. of driving gear }}$, lh. -in .
Tangential force (drive gear 1 ) $=P_{1}=\frac{Q}{r_{1}}=\frac{\text { torque input, } \mathrm{lb} .-\mathrm{in} .}{\text { pitch radius of gear, in. }} \mathrm{lb}$.
Separating force (drive gear 1) $=S_{1}=P_{1} \tan \alpha, \mathrm{lb} . \quad(\alpha=$ tooth pressure angle)
Tangential force (drive gear 2) $=P_{2}=P_{1} \times \frac{r_{3}}{r_{2}} \quad\left(r_{2}\right.$ and $r_{3}=$ pitch radii of gears 2 and 3 )
Separating force (drive gear 2) $=S_{2}=P_{2} \tan \alpha$
Bearing loads

| Due | On bearing 1 | On bearing 2 | On bearing 3 | On bearing 4 |
| :---: | :---: | :---: | :---: | :---: |
| $P_{1}$ | $P_{1}=P_{1} \frac{B}{A+B}$ | $P_{2}=P_{1} \frac{A}{A+B}$ | $\begin{aligned} & P_{3 V^{*}}=P_{1} \sin \beta \frac{D+E}{C+D+E} \\ & P_{3 B^{*}}=P_{1} \cos \beta \frac{D+E}{C+D+E} \end{aligned}$ | $\begin{aligned} & P_{4 V}=P_{1} \sin \beta \frac{C}{C+D+E} \\ & P_{4 H}=P_{1} \cos \beta \frac{C}{C+D+E} \end{aligned}$ |
| $S_{1}$ | $S_{1}=S_{1} \frac{B}{A+B}$ | $S_{2}=S_{1} \frac{A}{A+B}$ | $\begin{aligned} & S_{3 V}=S_{1} \cos \beta \frac{D+E}{C+D+E} \\ & S_{3 H}=S_{1} \sin \beta \frac{D+E}{C+D+E} \end{aligned}$ | $\begin{aligned} & S_{4 V}=S_{1} \cos \beta \frac{C}{C+D+E} \\ & S_{4 H}=S_{1} \sin \beta \frac{C}{C+D+E} \end{aligned}$ |
|  | On bearing 5 | On bearing 6 |  |  |
| $P_{2}$ | $P_{5}=P_{2} \frac{G}{P+G}$ | $P_{6}=P_{2} \frac{F}{F+G}$ | $P_{3,2}=P_{2} \frac{E}{C+D+E}$ | $P_{4,2}=P_{2} \frac{C+D}{C+D+E}$ |
| S2 | $S_{s}=S_{3} \frac{G}{F+G}$ | $S_{0}=S_{2} \frac{F}{\vec{F}+\vec{G}}$ | $S_{3,2}=\frac{E}{C+D+E}$ | $S_{4,2}=S_{2} \frac{C+D}{C+D+E}$ |

On bearing $3=\sqrt{\left(P_{3 V}+S_{3,2}-S_{3 V}\right)^{2}+\left(P_{3 I I}+S_{3 I I}+P_{3,2}\right)^{2}}$
On bearing $4=\sqrt{\left(P_{4 V}+S_{4,2}-S_{4 V}\right)^{2}+\left(P_{4 I I}+S_{4 I I}+P_{4,2}\right)^{2}}$
On bearing $5=\sqrt{P_{6}^{2}+S_{5}^{2}}, \quad$ on bearing $6=\sqrt{P_{6}^{2}+S_{6}^{2}}$

Table A3-11.-Bearing Loads Due to Planetary Gearing
(From New Departure "Handbook")


When the system employs two or more planet gears (usually three, as shown by dotted lines in diagram), the tangential and separating forces, due to the input torque, counterbalance each other in so far as they can produce appreciable loads on bearings 1, 2, 4, and 5. However, bearing 3 will be loaded because of the torque transmitted.

$$
Q=\frac{\mathrm{hp} . \times 63,025}{N}=\text { torque input, lb.-in. }
$$

where hp. $=$ horsepower transmitted
and $\quad N=r . p . m$. of driving gear.

$$
P=\frac{Q}{r}=\text { tangential force, in pounds of driving sun gear, }
$$

where $r=$ pitch radius of gear, in.

$$
S=P \tan \alpha=\text { separating force in pounds of the sun gear }
$$

where $\alpha=$ tooth pressure angle.
For three planet gears, the load on each planet pin bearing, position 3, due to driving torque and reaction, will (with equally distributed torque) be

$$
\frac{2 P}{3}
$$

When torque is transmitted through a single planet gear, the following loads are produced:

> Bearing Loads



In the process of determining bearing loads with this type of gearing, the force $E$ normal to the driving tooth contact is resolved into three forces. The first, $P$, is directed vertically, the second, $T_{G}$, horizontally, both in a plane at right angles to the pinion shaft, and the third, $T_{P}$, parallel to the pinion axis.

$$
Q=\frac{\mathrm{hp} . \times 63,025}{N}=\text { torque input, } \mathrm{lb} .-\mathrm{in} .
$$

where hp. $=$ horsepower transmitted.

$$
N=\text { r.p.m. of pinion. }
$$

$$
P=\frac{Q}{r_{1}}=\text { tangential force }
$$

where $r_{1}=$ mean pinion pitch radius in inches $=1 / 2$ (pinion pitch diameter - tooth face $\times \sin \beta$ ), angle $\beta$ being defined below.
$r_{2}=$ mean gear pitch radius $=r_{1} \times \frac{\text { number of teeth in gear }}{\text { number of teeth in pinion }}$

$$
T_{G}=P \tan \alpha \cos \beta=\text { gear thrust }
$$

where $\alpha=$ tooth pressure angle.

$$
\begin{aligned}
\beta & =1 / 2 \text { pinion pitch eone angle. } \\
& =\tan ^{-1} \frac{\text { number of teeth in pinion }}{\text { number of teeth in gear }} \\
& T_{P}=P \tan \alpha \sin \beta=\text { pinion thrust. }
\end{aligned}
$$

Note derivation from diagram.

Table A3-12.-Bearing Loads Due to Plain Bevel Gearing.(Continued) Bearing Loads

| Due to | On bearing 1 | On bearing 2 |
| :---: | :---: | :---: |
| $P$. <br> $T G$ $\qquad$ <br> $T_{P}$ <br> Total radial load Thrust load. Total load. | $\begin{gathered} P \frac{A+B}{B}=P_{1} \\ T_{G} \frac{A+B}{B}=T_{G 1} \\ T_{P} \frac{r_{1}}{B}=U_{1} \\ \sqrt{P_{1}^{2}+\left(T_{G 1}-U_{1}\right)^{2}} \\ \sqrt{P_{1}^{2}+\left(T_{G 1}-U_{1}\right)^{2}} \end{gathered}$ | $\begin{gathered} P \frac{A}{\bar{B}}=P_{2} \\ T_{G} \frac{A}{\bar{B}}=T_{G 2} \\ T_{P} \frac{r_{1}}{B} \doteq U_{2}=U_{1} \\ \sqrt{P_{2}^{2}+\left(T_{G 2}-U_{2}\right)^{2}}=R_{2} \\ \frac{T_{P}}{R_{2}^{2}+T_{P}^{2}} \end{gathered}$ |
| Due to | On bearing | On bearing 4 |
| $P$ <br> $T_{G}$ $\qquad$ <br> $T_{P}$ $\qquad$ <br> Total radial load. <br> Thrust load. <br> Total load. | $\begin{gathered} P \frac{D}{C+D}=P_{3} \\ T_{G} \frac{r_{2}}{C+D}=U_{3} \\ T_{P} \frac{D}{C+D}=T_{P 3} \\ \sqrt{P_{3}^{2}+\left(T_{P_{3}}+U_{3}\right)^{2}}=R_{3} \\ \frac{T G}{R_{3}^{2}+T_{G}^{2}} \end{gathered}$ | $\begin{gathered} P \frac{C}{C+D}=P_{4} \\ T_{G} \frac{r_{2}}{C+D}=U_{4}=U_{3} \\ T_{P} \frac{C}{C+D}=T_{P_{4}} \\ \sqrt{P_{4}^{2}+\left(U_{4}-T_{\left.P_{4}\right)^{2}}\right.} \\ \sqrt{P_{4}^{2}+\left(U_{4}-T_{\left.P_{4}\right)^{2}}\right.} \end{gathered}$ |

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Wrim tans. wan-w.


[^0]:    * Equation (1-2) gives reasonably close values of brake horsepower, but some additional minor factors should be eonsidered for precise caleulations. See reference 1, Chap. 1, reference 2, p. 122, and NACA Tech. Rept. 408.

[^1]:    * In preparing this preliminary layout, the designer may be likened io a topographer preparing a map of a little known region. The first step is $t$,

[^2]:    *This is true except in offset-cylinder engines, but the construction may be modified readily for such cases.

[^3]:    * A more complete method of analysis is to be found in reforenere 3 .

[^4]:    * The maximum force is slightly less owing to the changed angula rity ( $\beta$ ) of vector $F_{R}$ at $2,400 \mathrm{r} . \mathrm{p} . \mathrm{m}$. $F_{k}$ may be found more atenarately by first finding $F_{I T}$ at the desired speed and then scaling $F_{B}$ from the diagram.
    $\dagger$ See reference 10 for additional data.

[^5]:    * For an explanation of the S.A.F. steel-numbering system, see Table A 2-6. For detailed data on the various S.A.E. steels, see reference 8.

[^6]:    * See footnote $\ddagger$ Table 7-1.

[^7]:    * The propeller has such a high inertia that it is approximately the erquivalent of the rigid support in Fig. 7-1 ( $B$ ). This simplyfying assumpion suffices for preliminary considerations only, however.

[^8]:    * A cosine curve is the same as a sine curve displaced at an angle of 90 deg .

[^9]:    * See footnote $\ddagger$ of Table 7-1.

[^10]:    * Radial engines have some slight secondary unbalance owing to the articulated rod construction.
    $\dagger$ Unbalance is one-half of maximum unbalance for one cylinder times number of cylinders.
    $\ddagger$ In reference 12 (now out of print), Prof. Sharp has demonstrated that if the unbalance of the connecting rods is taken into account, this statement is not strictly correct.
    becomes a compromise. Usual procedure is to make the radial over-all length of the counterweights about equal to the radial

[^11]:    * See Fig. A2-1 for estimating the Brinell hardness number of the gear steel being used

[^12]:    * A discussion on liquid cooling is to be found in reference 15.

[^13]:    * Stellite-faced steel seats are frequently used for extreme service.

[^14]:    Maximum overlap $=95$ deg. Minimum overlap $=0$ deg. Average overlap $=33$ deg.

[^15]:    * See footnote, p. 265.

[^16]:    * At rated engine speed.
    $\dagger$ Wet sump crankcase.

[^17]:    * For a supercharger with a Venturi-type carburetor in the inlet, slightly greater accuracy will be had if allowance is made for carburetor drop which will reduce $P_{E}$ by 0.5 to $1.0 \mathrm{in} . \mathrm{Hg}$.
    $\dagger$ An alternate procedure for design purposes is to assume an air requirement of 0.11 to 0.12 lb . of air per b.hp. per min.

[^18]:    * This warping is analogous to the warping of propeller blades.

[^19]:    * The velocity of sound will be greater than in standard air because of the increased temperature of the air in the impeller.

[^20]:    * See footnote(*), p. 294.

[^21]:    Wright，Cyclone GR－2600－A5B．．
    Wright，Cyclone GR－1820－G202A． Wright，Cycione GR－1820－G203A

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    ## 

    Wright，＇C relone R－1820－1：＂2． Wright＇（＇rane R Wright，＇（ Wright，${ }^{i}$（＇） 1 clone R－1820－1．
    
    

[^22]:    

[^23]:    ベだに

[^24]:    

[^25]:    
    

[^26]:    

[^27]:    * Master cylinder.
    $\dagger$ Articulated cylinder.

[^28]:    * Four splines, for fits $A$ and $B$ only.

    Radii on corners of splines not to exceed 0.015 in .
    Splines small not be more than 0.006 in . per ft . out of parallel with respect to the axis of the shaft.

    No allowance is made for radii on corners or for clearness. Dimensions are intended to apply to only the soft broached hole. Allowance must be made for machining.

[^29]:    ${ }^{1}$ New Departure "Handbook."
    "S.A.E. "Handbook."

[^30]:    * Radius $r$ indicates maximum fillet radius in housing or on shaft which bearing radius will clear.

[^31]:    * Radius $r$ indicates maximum fillet radius in housing or on shaft which bearing radius will clear.

[^32]:    * Radius $r$ indicates maximum fillet radius in housing or on shaft which bearing radius

[^33]:    * Radius $r$ indicates maximum fillet radius in housing or on shaft which bearing radius will clear.

[^34]:    * Norma-Hoff mann roller bearings applicable to use in aircraft engines are also made in standard, one-lipped, and two-lipped metric types, data of Norma-Hoffmam Bearings Corporation.

[^35]:    * Viewed from the drive end.
    $\dagger$ Magneto drive shafts should be designed to transmit $1 / 2 \mathrm{hp}$.

[^36]:    * Heat-treatment symbols have been omitted since composition does not vary for different - heat-treatment practices.

[^37]:    * For aluminum alloys in the heat-treated condition.

[^38]:    * Tensile strength at $1200^{\circ} \mathrm{F}$. All other tensile properties are typical specification values.

[^39]:    ＊Brinell unless preceded by letter for appropriate Rockwell scale．

[^40]:    $\dagger$ Shearing strength at $350^{\circ} \mathrm{F}$.-Base metal, copper. $\ddagger$ Melting starts, deg. F.

[^41]:    $N=$ number of teeth.
    $P_{d}=$ diametral pitch.
    $P_{c}=$ circular pitch.
    $P_{d} \times P_{c}=\pi$.
    ${ }^{1}$ Norman, Ault, and Zarobsky, "Fundamentals of Machine Design."
    ${ }^{2}$ Data of Foote Brothers Gear and Machine Company.

[^42]:    $N=$ number of teeth.
    $P_{d}=$ diametral pitch.
    $D=$ pitch diameter.
    $P_{c}=$ circular pitch.
    $P_{d} \times P_{c}=\pi$.
    ${ }^{1}$ Norman, Ault, and Zarobsky, "Fundamentals of Machine Design."
    ${ }^{2}$ Data of Foote Brothers Gear and Machine Company.

[^43]:    ${ }^{1}$ Norman, Ault, and Zarobeky, "Fundamentals of Machine Design."
    ${ }^{2}$ Data of Foote Brothers Cear and Machine Company.

[^44]:    ${ }^{1}$ Data of Foote Brothers Gear and Machine Company.
    ${ }^{2}$ Schwamb, Merrill, and James, "Elements of Mechanism."
    ${ }^{3}$ Buckingham, "Manual of Gear Design."

